Lecture 8: Recurrent Neural Networks

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Administrative

- Discussion section tomorrow 1:30-2:20pm PT PyTorch / TensorFlow Review

- Additional optional section today between 5:30-6:45pm PT at building 460 room 429

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Training "Feedforward" Neural Networks

- **1. One time set up**: activation functions, preprocessing, weight initialization, regularization, gradient checking
- **2. Training dynamics**: babysitting the learning process, parameter updates, hyperparameter optimization

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3. Evaluation: model ensembles, test-time augmentation, transfer learning

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Today: Recurrent Neural Networks

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"Vanilla" Neural Network

one to one



Vanilla Neural Networks

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e.g. Image Captioning image -> sequence of words

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sequence of video frames -> action class

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Sequential Processing of Non-Sequence Data

Classify images by taking a series of "glimpses"

2	13	8	2	9	1	1	1	1	8
3	3	2	8	6	9	6	5	1	3
8	8	1	8		6	9	8	3	4
1	0	2	7	6	Õ	9	-	4	5
7	/	4	4	4	4	4	ų	7	9
3	1	8	9	3	4	2	7	7	3
6	6	1	6	3	- An	3	3	-	0
b	1	۵	Б	3	5	1	8	3	4
9	9	ł	1	3	0	5	9	5	4
1	1	8	7	9	00	500	2		R

Ba, Mnih, and Kavukcuoglu, "Multiple Object Recognition with Visual Attention", ICLR 2015. Gregor et al, "DRAW: A Recurrent Neural Network For Image Generation", ICML 2015 Figure copyright Karol Gregor, Ivo Danihelka, Alex Graves, Danilo Jimenez Rezende, and Daan Wierstra, 2015. Reproduced with permission.

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Sequential Processing of Non-Sequence Data

Generate images one piece at a time!





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Gregor et al, "DRAW: A Recurrent Neural Network For Image Generation", ICINE 2015 Figure copyright Karol Gregor, Ivo Danihelka, Alex Graves, Danilo Jimenez Rezende, and Daan Wierstra, 2015. Reproduced with permission.

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Recurrent Neural Network



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Recurrent Neural Network



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Unrolled RNN



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RNN hidden state update

We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:



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RNN output generation

We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:





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Recurrent Neural Network

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We can process a sequence of vectors **x** by applying a **recurrence formula** at every time step:

$$h_t = f_W(h_{t-1}, x_t)$$

Notice: the same function and the same set of parameters are used at every time step.



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(Vanilla) Recurrent Neural Network

The state consists of a single *"hidden"* vector **h**:



Sometimes called a "Vanilla RNN" or an "Elman RNN" after Prof. Jeffrey Elman

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Re-use the same weight matrix at every time-step



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RNN: Computational Graph: Many to One



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RNN: Computational Graph: Many to One



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Sequence to Sequence: Many-to-one + one-to-many

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Many to one: Encode input sequence in a single vector



Sutskever et al, "Sequence to Sequence Learning with Neural Networks", NIPS 2014

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Sequence to Sequence: Many-to-one + one-to-many

One to many: Produce output sequence from single input vector



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Example: Character-level Language Model

Vocabulary: [h,e,l,o]

Example training sequence: **"hello"**



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Example: Character-level Language Model

Vocabulary: [h,e,l,o]

Example training sequence: **"hello"**

$$h_t = anh(W_{hh}h_{t-1} + W_{xh}x_t)$$



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Example: Character-level Language Model

Vocabulary: [h,e,l,o]

Example training sequence: **"hello"**



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Vocabulary: [h,e,l,o]

At test-time sample characters one at a time, feed back to model



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Vocabulary: [h,e,l,o]

At test-time sample characters one at a time, feed back to model



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Vocabulary: [h,e,l,o]

At test-time sample characters one at a time, feed back to model



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Vocabulary: [h,e,l,o]

At test-time sample characters one at a time, feed back to model



$$\begin{bmatrix} w_{11} & w_{12} & w_{13} & w_{14} \end{bmatrix} \begin{bmatrix} 1 \end{bmatrix} = \begin{bmatrix} w_{11} \end{bmatrix} \\ \begin{bmatrix} w_{21} & w_{22} & w_{23} & w_{14} \end{bmatrix} \begin{bmatrix} 0 \end{bmatrix} = \begin{bmatrix} w_{21} \end{bmatrix} \\ \begin{bmatrix} w_{31} & w_{32} & w_{33} & w_{14} \end{bmatrix} \begin{bmatrix} 0 \end{bmatrix} = \begin{bmatrix} w_{31} \end{bmatrix} \\ \begin{bmatrix} 0 \end{bmatrix}$$

Matrix multiply with a one-hot vector just extracts a column from the weight matrix. We often put a separate **embedding** layer between input and hidden layers.



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Truncated Backpropagation through time



Run forward and backward through chunks of the sequence instead of whole sequence

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Truncated Backpropagation through time



Carry hidden states forward in time forever, but only backpropagate for some smaller number of steps

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Truncated Backpropagation through time



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min-char-rnn.py gist: 112 lines of Python

```
Minimal character-level Vanilla RNN model. Written by Andrej Karpathy (@karpathy)
3 BSD License
4 .....
 5 import numpy as np
7 # data I/0
8 data = open('input.txt', 'r').read() # should be simple plain text file
g chars = list(set(data))
18 data_size, vocab_size = len(data), len(chars)
print 'data has %d characters, %d unique.' % (data_size, vocab_size)
12 char_to_ix = { ch:i for i, ch in enumerate(chars) }
ix_to_char = { i:ch for i, ch in enumerate(chars) }
15 # hyperparameters
16 hidden_size = 100 # size of hidden layer of neurons
17 seq_length = 25 # number of steps to unroll the RNN for
18 learning rate = 1e-1
21 Wxh = np.random.randn(hidden_size, vocab_size)*0.01 # input to hidden
22 Whh = np.random.randn(hidden_size, hidden_size)*0.01 # hidden to hidden
23 Why = np.random.randn(vocab_size, hidden_size)*0.01 # hidden to output
24 bh = np.zeros((hidden_size, 1)) # hidden bias
25 by = np.zeros((vocab_size, 1)) # output bias
27 def lossFun(inputs, targets, hprev):
     .....
      inputs, targets are both list of integers.
      hprev is Hx1 array of initial hidden state
      returns the loss, gradients on model parameters, and last hidden state
      .....
     xs, hs, ys, ps = {}, {}, {}, {}
     hs[-1] = np.copy(hprev)
     loss = 0
      for t in xrange(len(inputs)):
        xs[t] = np.zeros((vocab_size.1)) # encode in 1-of-k representation
        xs[t][inputs[t]] = 1
       hs[t] = np.tanh(np.dot(Wxh, xs[t]) + np.dot(Whh, hs[t-1]) + bh) # hidden state
       ys[t] = np.dot(why, hs[t]) + by # unnormalized log probabilities for next chars
       ps[t] = np.exp(ys[t]) / np.sum(np.exp(ys[t])) # probabilities for next chars
        loss += -np.log(ps[t][targets[t],0]) # softmax (cross-entropy loss)
44 # backward pass: compute gradients going backwards
45 dwxh, dwhh, dwhy = np.zeros_like(wxh), np.zeros_like(whh), np.zeros_like(why)
46 dbh, dby = np.zeros_like(bh), np.zeros_like(by)
      dhnext = np.zeros_like(hs[0])
      for t in reversed(xrange(len(inputs))):
        dy = np.copy(ps[t])
        dy[targets[t]] -= 1 # backprop into y
        dWhy += np.dot(dy, hs[t].T)
52 dby += dy
53 dh = np.dot(Why.T, dy) + dhnext # backprop into h
54 dhraw = (1 - hs[t] * hs[t]) * dh # backprop through tanh nonlinearity
       dbb += dbraw
       dwxh += np.dot(dhraw, xs[t].T)
       dwhh += np.dot(dhraw, hs[t-1].T)
        dhnext = np.dot(Whh.T, dhraw)
      for dparam in [dWxh, dWhh, dWhy, dbh, dby]:
```

np.clip(dparam, -5, 5, out=dparam) # clip to mitigate exploding gradients
return loss, dwxh, dwhh, dwhy, dbh, dby, hs[len(inputs)-1]

```
63 def sample(h, seed_ix, n):
64 ***
      sample a sequence of integers from the model
66
      h is memory state, seed_ix is seed letter for first time step
68 x = np.zeros((vocab_size, 1))
69 x[seed_ix] = 1
70 ixes = []
71 for t in xrange(n):
       h = np.tanh(np.dot(Wxh, x) + np.dot(Whh, h) + bh)
        y = np.dot(Why, h) + by
        p = np.exp(y) / np.sum(np.exp(y))
        ix = np.random.choice(range(vocab_size), p=p.ravel())
        x = np.zeros((vocab_size, 1))
         x[ix] = 1
         ixes.append(ix)
      return ixes
81 n, p = 0, 0
82 mWxh, mWhh, mWhy = np,zeros like(Wxh), np,zeros like(Whh), np,zeros like(Why)
as mbh, mby = np.zeros like(bh), np.zeros like(by) # memory variables for Adagrad
84 smooth_loss = -np.log(1.0/vocab_size)*seq_length # loss at iteration 0
85 while True:
86 # prepare inputs (we're sweeping from left to right in steps seq_length long)
       if p+seq length+1 >= len(data) or p == 0:
       hprev = np.zeros((hidden_size,1)) # reset RNN memory
       p = 0 # go from start of data
       inputs = [char_to_ix[ch] for ch in data[p:p+seq_length]]
       targets = [char_to_ix[ch] for ch in data[p+1:p+seq_length+1]]
94 if n % 100 == 0:
         sample_ix = sample(hprev, inputs[0], 200)
95
96
         txt = ''.join(ix_to_char[ix] for ix in sample_ix)
        print '---- \n %s \n----' % (txt, )
      # forward seg length characters through the net and fetch gradient
       loss, dwxh, dwhh, dwhy, dbh, dby, hprey = lossFun(inputs, targets, hprey)
       smooth loss = smooth loss * 0,999 + loss * 0,001
      if n % 100 == 0; print 'iter %d, loss; %f' % (n, smooth loss) # print progress
      # perform parameter update with Adagrad
       for param, dparam, mem in zip([Wxh, Whh, Why, bh, by],
                                   [dwxh, dwhh, dwhy, dbh, dby],
                                   [mWxh, mWhh, mWhy, mbh, mby]):
         mem += dparam * dparam
         param += -learning_rate * dparam / np.sqrt(mem + 1e-8) # adagrad update
```

p += seq_length # move data pointer

```
112 n += 1 # iteration counter
```

(https://gist.github.com/karpathy/d4dee 566867f8291f086)

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THE SONNETS

by William Shakespeare

From fairest creatures we desire increase, That thereby beauty's rose might never die, But as the riper should by time decease, His tender heir might bear his memory: But thou, contracted to thine own bright eyes, Feed'st thy light's flame with self-substantial fuel, Making a famine where abundance lies, Thyself thy foe, to thy sweet self too cruel: Thou that art now the world's fresh ormament, And only herald to the gaudy spring, Within thine own bud buriest thy content, And tender churl mak'st waste in niggarding: Pity the world's due, by the grave and thee.

When forty winters shall besiege thy brow, And dig deep trenches in thy beauty's field, Thy youth's proud livery so gazed on now, Will be a tatter'd weed of small worth held: Then being asked, where all thy beauty lies, Where all the treasure of thy lusty days; To say, within thine own deep sunken eyes, Were an all-eating shame, and thriftless praise. How much more praise deserv'd thy beauty's use, If thou couldst answer 'This fair child of mine Shall sum my count, and make my old excuse,' Proving his beauty by succession thine! This were to be new made when thou art old, And see thy blood warm when thou feel'st it cold.



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at first:

tyntd-iafhatawiaoihrdemot lytdws e ,tfti, astai f ogoh eoase rrranbyne 'nhthnee e
plia tklrgd t o idoe ns,smtt h ne etie h,hregtrs nigtike,aoaenns lng

train more

"Tmont thithey" fomesscerliund Keushey. Thom here sheulke, anmerenith ol sivh I lalterthend Bleipile shuwy fil on aseterlome coaniogennc Phe lism thond hon at. MeiDimorotion in ther thize."

train more

Aftair fall unsuch that the hall for Prince Velzonski's that me of her hearly, and behs to so arwage fiving were to it beloge, pavu say falling misfort how, and Gogition is so overelical and ofter.

train more

"Why do what that day," replied Natasha, and wishing to himself the fact the princess, Princess Mary was easier, fed in had oftened him. Pierre aking his soul came to the packs and drove up his father-in-law women.

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PANDARUS:

Alas, I think he shall be come approached and the day When little srain would be attain'd into being never fed, And who is but a chain and subjects of his death, I should not sleep.

Second Senator:

They are away this miseries, produced upon my soul, Breaking and strongly should be buried, when I perish The earth and thoughts of many states.

DUKE VINCENTIO:

Well, your wit is in the care of side and that.

Second Lord:

They would be ruled after this chamber, and my fair nues begun out of the fact, to be conveyed, Whose noble souls I'll have the heart of the wars.

Clown:

Come, sir, I will make did behold your worship.

VIOLA: I'll drink it.

VIOLA:

Why, Salisbury must find his flesh and thought That which I am not aps, not a man and in fire, To show the reining of the raven and the wars To grace my hand reproach within, and not a fair are hand, That Caesar and my goodly father's world; When I was heaven of presence and our fleets, We spare with hours, but cut thy council I am great, Murdered and by thy master's ready there My power to give thee but so much as hell: Some service in the noble bondman here, Would show him to her wine.

KING LEAR:

O, if you were a feeble sight, the courtesy of your law, Your sight and several breath, will wear the gods With his heads, and my hands are wonder'd at the deeds, So drop upon your lordship's head, and your opinion Shall be against your honour.

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For $\bigoplus_{n=1,...,m}$ where $\mathcal{L}_{m_{\bullet}} = 0$, hence we can find a closed subset \mathcal{H} in \mathcal{H} and any sets \mathcal{F} on X, U is a closed immersion of S, then $U \to T$ is a separated algebraic space.

Proof. Proof of (1). It also start we get

 $S = \operatorname{Spec}(R) = U \times_X U \times_X U$

and the comparicoly in the fibre product covering we have to prove the lemma generated by $\coprod Z \times_U U \to V$. Consider the maps M along the set of points Sch_{fppf} and $U \to U$ is the fibre category of S in U in Section, ?? and the fact that any U affine, see Morphisms, Lemma ??. Hence we obtain a scheme S and any open subset $W \subset U$ in Sh(G) such that $Spec(R') \to S$ is smooth or an

 $U = \bigcup U_i \times_{S_i} U_i$

which has a nonzero morphism we may assume that f_i is of finite presentation over S. We claim that $\mathcal{O}_{X,x}$ is a scheme where $x, x', s'' \in S'$ such that $\mathcal{O}_{X,x'} \to \mathcal{O}'_{X',x'}$ is separated. By Algebra, Lemma ?? we can define a map of complexes $\operatorname{GL}_{S'}(x'/S'')$ and we win.

To prove study we see that $\mathcal{F}|_U$ is a covering of \mathcal{X}' , and \mathcal{T}_i is an object of $\mathcal{F}_{X/S}$ for i > 0 and \mathcal{F}_p exists and let \mathcal{F}_i be a presheaf of \mathcal{O}_X -modules on \mathcal{C} as a \mathcal{F} -module. In particular $\mathcal{F} = U/\mathcal{F}$ we have to show that

 $\widetilde{M}^{\bullet} = \mathcal{I}^{\bullet} \otimes_{\mathrm{Spec}(k)} \mathcal{O}_{S,s} - i_X^{-1} \mathcal{F})$

is a unique morphism of algebraic stacks. Note that

Arrows = $(Sch/S)_{fppf}^{opp}, (Sch/S)_{fppf}$

and

 $V = \Gamma(S, \mathcal{O}) \longmapsto (U, \operatorname{Spec}(A))$

is an open subset of X. Thus U is affine. This is a continuous map of X is the inverse, the groupoid scheme S.

Proof. See discussion of sheaves of sets.

The result for prove any open covering follows from the less of Example ??. It may replace S by $X_{spaces, \acute{e}tale}$ which gives an open subspace of X and T equal to S_{Zar} , see Descent, Lemma ??. Namely, by Lemma ?? we see that R is geometrically regular over S.

Lemma 0.1. Assume (3) and (3) by the construction in the description.

Suppose $X = \lim |X|$ (by the formal open covering X and a single map $\underline{Proj}_X(\mathcal{A}) = \operatorname{Spec}(B)$ over U compatible with the complex

 $Set(\mathcal{A}) = \Gamma(X, \mathcal{O}_{X, \mathcal{O}_X}).$

When in this case of to show that $\mathcal{Q} \to C_{Z/X}$ is stable under the following result in the second conditions of (1), and (3). This finishes the proof. By Definition ?? (without element is when the closed subschemes are catenary. If T is surjective we may assume that T is connected with residue fields of S. Moreover there exists a closed subspace $Z \subset X$ of X where U in X' is proper (some defining as a closed subset of the uniqueness it suffices to check the fact that the following theorem

(1) f is locally of finite type. Since S = Spec(R) and Y = Spec(R).

Proof. This is form all sheaves of sheaves on X. But given a scheme U and a surjective étale morphism $U \to X$. Let $U \cap U = \coprod_{i=1,...,n} U_i$ be the scheme X over S at the schemes $X_i \to X$ and $U = \lim_i X_i$.

The following lemma surjective restrocomposes of this implies that $\mathcal{F}_{x_0} = \mathcal{F}_{x_0} = \mathcal{F}_{\mathcal{X},\dots,0}$.

Lemma 0.2. Let X be a locally Noetherian scheme over S, $E = \mathcal{F}_{X/S}$. Set $\mathcal{I} = \mathcal{J}_1 \subset \mathcal{I}'_n$. Since $\mathcal{I}^n \subset \mathcal{I}^n$ are nonzero over $i_0 \leq \mathfrak{p}$ is a subset of $\mathcal{J}_{n,0} \circ \overline{A}_2$ works.

Lemma 0.3. In Situation ??. Hence we may assume q' = 0.

Proof. We will use the property we see that \mathfrak{p} is the mext functor (??). On the other hand, by Lemma ?? we see that

 $D(\mathcal{O}_{X'}) = \mathcal{O}_X(D)$

where K is an F-algebra where δ_{n+1} is a scheme over S.

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Proof. Omitted.

Lemma 0.1. Let C be a set of the construction.

Let C be a gerber covering. Let F be a quasi-coherent sheaves of O-modules. We have to show that

$$\mathcal{O}_{\mathcal{O}_X} = \mathcal{O}_X(\mathcal{L})$$

Proof. This is an algebraic space with the composition of sheaves \mathcal{F} on $X_{\acute{e}tale}$ we have

$$\mathcal{O}_X(\mathcal{F}) = \{morph_1 \times_{\mathcal{O}_X} (\mathcal{G}, \mathcal{F})\}$$

where \mathcal{G} defines an isomorphism $\mathcal{F} \to \mathcal{F}$ of \mathcal{O} -modules.

Lemma 0.2. This is an integer Z is injective.

Proof. See Spaces, Lemma ??.

Lemma 0.3. Let S be a scheme. Let X be a scheme and X is an affine open covering. Let $U \subset X$ be a canonical and locally of finite type. Let X be a scheme. Let X be a scheme which is equal to the formal complex.

The following to the construction of the lemma follows.

Let X be a scheme. Let X be a scheme covering. Let

 $b: X \to Y' \to Y \to Y \to Y' \times_X Y \to X.$

be a morphism of algebraic spaces over S and Y.

Proof. Let X be a nonzero scheme of X. Let X be an algebraic space. Let \mathcal{F} be a quasi-coherent sheaf of \mathcal{O}_X -modules. The following are equivalent

(1) \mathcal{F} is an algebraic space over S.

(2) If X is an affine open covering.

Consider a common structure on X and X the functor $\mathcal{O}_X(U)$ which is locally of finite type. \Box



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arch	Merge branch 'x86-urgent-for-lin	Graphs								
block	block: discard bdi_unregister() i	days ago	Grapi							
Crypto	Merge git://git.kernel.org/pub/sc	days ago	HTTPS clone URL							
drivers	Merge branch 'drm-fixes' of git:/	/people.freedesktop.org/~airlied	linux	9 h	ours ago	https	://github.	6		
in firmware	firmware/lhex2fw.c: restore mis-	sing default in switch statement		2 mo	nths ago	You car	n clone with H	TTPS		
🖿 fs	vfs: read file_handle only once	days ago	SSH, or	SSH, or Subversion. 3						
include	Merge branch 'perf-urgent-for-lin	nus' of git://git.kernel.org/pub/sc	π/	а	day ago	۵.	Clone in Desktop			
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ina ina	Morris branch Nor linue! of alt-lin	it komol oroloubloom/linux/kom	ol	0.00	anth ana					

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```
static void do command(struct seg file *m, void *v)
{
 int column = 32 << (cmd[2] & 0x80);</pre>
 if (state)
    cmd = (int)(int state ^ (in 8(&ch->ch flags) & Cmd) ? 2 : 1);
 else
    seq = 1;
  for (i = 0; i < 16; i++) {</pre>
    if (k & (1 << 1))
      pipe = (in use & UMXTHREAD UNCCA) +
        ((count & 0x0000000fffffff8) & 0x000000f) << 8;
    if (count == 0)
      sub(pid, ppc md.kexec handle, 0x2000000);
    pipe set bytes(i, 0);
  /* Free our user pages pointer to place camera if all dash */
  subsystem info = &of changes[PAGE SIZE];
  rek controls(offset, idx, &soffset);
  /* Now we want to deliberately put it to device */
 control check polarity(&context, val, 0);
  for (i = 0; i < COUNTER; i++)</pre>
```

seq_puts(s, "policy ");

}

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Generated

C code

```
14
   Copyright (c) 2006-2010, Intel Mobile Communications. All rights reserved.
    This program is free software; you can redistribute it and/or modify it
* under the terms of the GNU General Public License version 2 as published by
 * the Free Software Foundation.
         This program is distributed in the hope that it will be useful,
 * but WITHOUT ANY WARRANTY; without even the implied warranty of
     MERCHANTABILITY OF FITNESS FOR A PARTICULAR PURPOSE. See the
   GNU General Public License for more details.
    You should have received a copy of the GNU General Public License
     along with this program; if not, write to the Free Software Foundation,
* Inc., 675 Mass Ave, Cambridge, MA 02139, USA.
*/
#include <linux/kexec.h>
#include <linux/errno.h>
#include <linux/io.h>
#include <linux/platform device.h>
#include <linux/multi.h>
#include <linux/ckevent.h>
#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
```

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Lecture 8 - 56

```
#include <asm/io.h>
#include <asm/prom.h>
#include <asm/e820.h>
#include <asm/system info.h>
#include <asm/setew.h>
#include <asm/pgproto.h>
#define REG PG vesa slot addr pack
#define PFM NOCOMP AFSR(0, load)
#define STACK DDR(type) (func)
#define SWAP ALLOCATE(nr)
                             (e)
#define emulate sigs() arch get unaligned child()
#define access rw(TST) asm volatile("movd %%esp, %0, %3" :: "r" (0)); \
 if ( type & DO READ)
static void stat PC SEC read mostly offsetof(struct seq argsqueue, \
          pC>[1]);
static void
os_prefix(unsigned long sys)
{
#ifdef CONFIG PREEMPT
 PUT_PARAM_RAID(2, sel) = get_state_state();
  set pid sum((unsigned long)state, current_state_str(),
           (unsigned long)-1->lr full; low;
}
```

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OpenAI Codex



/* &dd this image of a
rocketship:
https://i1.sndcdn.com/artworks
-j8xjG7zc1wmTeO7b-06183wt500x500.jpg */
var rocketship =
document.createElement('img');
rocketship.src =
'https://i1.sndcdn.com/artwork
s-j8xjG7zc1wmTeO7b-06183wt500x500.jpg';
document.body.appendChild(rock
etship);

Add this image of a <u>rocketship</u>: https://i1.sndcdn.com/artworks-j8xjG7zc1wmTeO7b-06l83w-t500x500.jpg



https://openai.com/blog/openai-codex/

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quote detection cell

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Cell sensitive to position in line:

The sole importance of the crossing of the Be zina that it plainly and indubitably proved the fallacy of all the plans for cutting off the enemy's retreat and the soundness of the only possible line of action--the one Kutuzov and the general mass of the army demanded -- namely, simply to follow the enemy up. The French crowd fled a continually increasing speed and all its energy was directed to reaching its goal. It fled like a wounded animal and it was impossible to block its path. This was shown not so much by the arrangements made for crossing as by what took place at the bridges. When the bridges broke down, unarmed soldiers, people from Moscow and women with children o were with the French transport, all--carried on by vis inertiae-pressed forward into boats and into the ice-covered water and did not, surrender.

line length tracking cell

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Cell that turns on inside comments and quotes:

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code depth cell

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RNN tradeoffs

RNN Advantages:

- Can process any length input
- Computation for step *t* can (in theory) use information from many steps back
- Model size doesn't increase for longer input
- Same weights applied on every timestep, so there is symmetry in how inputs are processed.

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RNN Disadvantages:

- Recurrent computation is slow
- In practice, difficult to access information from many steps back

Image Captioning



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Explain Images with Multimodal Recurrent Neural Networks, Mao et al.

Deep Visual-Semantic Alignments for Generating Image Descriptions, Karpathy and Fei-Fei

Show and Tell: A Neural Image Caption Generator, Vinyals et al.

Long-term Recurrent Convolutional Networks for Visual Recognition and Description, Donahue et al.

Learning a Recurrent Visual Representation for Image Caption Generation, Chen and Zitnick

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Recurrent Neural Network



Convolutional Neural Network

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image

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conv-256 maxpool

conv-256

image

conv-64 conv-64 maxpool

conv-128 conv-128 maxpool

conv-512 conv-512

maxpool

conv-512

conv-512

maxpool

FC-4096 FC-4096

x0 <START>

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test image

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test image

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test image



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Lecture 8 - 76



test image

Lecture 8 - 77



Lecture 8 - 78

Image Captioning: Example Results

Captions generated using <u>neuraltalk2</u> All images are <u>CC0 Public domain</u>: <u>cat suitcase</u>, <u>cat tree</u>, <u>dog</u>, <u>bear</u>, <u>surfers</u>, <u>tennis</u>, <u>giraffe</u>, <u>motorcycle</u>





A cat sitting on a suitcase on the floor

A cat is sitting on a tree branch



A dog is running in the grass with a frisbee



A white teddy bear sitting in the grass



Two people walking on the beach with surfboards



A tennis player in action on the court



Two giraffes standing in a grassy field



A man riding a dirt bike on a dirt track

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Image Captioning: Failure Cases





A woman is holding a cat in her hand



A person holding a computer mouse on a desk



A woman standing on a beach holding a surfboard



A bird is perched on a tree branch



A man in a baseball uniform throwing a ball

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Visual Question Answering (VQA)



- Q: What endangered animal is featured on the truck?
- A: A bald eagle.
- A: A sparrow.
- A: A humming bird.
- A: A raven.



- Q: Where will the driver go if turning right?
- A: Onto 24 ³/₄ Rd. A: Onto 25 ³/₄ Rd.
- A: Onto 23 ³/₄ Rd.
 - . Onto 25 74 Ru.
- A: Onto Main Street.



- Q: When was the picture taken?
- A: During a wedding.
- A: During a bar mitzvah.
- A: During a funeral.
- A: During a Sunday church



- Q: Who is under the umbrella?
- A: Two women.
- A: A child.
- A: An old man.
- A: A husband and a wife.

Agrawal et al, "VQA: Visual Question Answering", ICCV 2015 Zhu et al, "Visual 7W: Grounded Question Answering in Images", CVPR 2016 Figure from Zhu et al, copyright IEEE 2016. Reproduced for educational purposes.

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Visual Question Answering (VQA)



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Visual Dialog: Conversations about images



Das et al, "Visual Dialog", CVPR 2017 Figures from Das et al, copyright IEEE 2017. Reproduced with permission.

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Visual Language Navigation: Go to the living room

Agent encodes instructions in language and uses an RNN to generate a series of movements as the visual input changes after each move.

Wang et al, "Reinforced Cross-Modal Matching and Self-Supervised Imitation Learning for Vision-Language Navigation", CVPR 2018 Figures from Wang et al, copyright IEEE 2017. Reproduced with permission.

Instruction

Turn right and head towards the *kitchen*. Then turn left, pass a *table* and enter the *hallway*. Walk down the hallway and turn into the *entry way* to your right *without doors*. Stop in front of the *toilet*.



Initial Position Target Position

Demonstration Path A
 Executed Path B
 Executed Path C

Local visual scene



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Visual Question Answering: Dataset Bias



Jabri et al. "Revisiting Visual Question Answering Baselines" ECCV 2016

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Multilayer RNNs



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Long Short Term Memory (LSTM)

Vanilla RNN

LSTM

$$h_t = \tanh\left(W\begin{pmatrix}h_{t-1}\\x_t\end{pmatrix}\right)$$

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

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Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation 1997

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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$
$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$
$$= \tanh\left(W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$

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y_t

Backpropagation from h_t to h_{t-1} multiplies by W (actually W_{hh}^{T})



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$$h_{t} = \tanh(W_{hh}h_{t-1} + W_{xh}x_{t})$$
$$= \tanh\left(\left(W_{hh} \quad W_{hx}\right) \begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$
$$= \tanh\left(W\begin{pmatrix}h_{t-1}\\x_{t}\end{pmatrix}\right)$$

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tanh

Backpropagation from h_t to h_{t-1} multiplies by W (actually W_{hh}^{T})

stack



Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

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$$rac{\partial h_t}{\partial h_{t-1}} = tanh'(W_{hh}h_{t-1}+W_{xh}x_t)W_{hh}$$

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h_{t-1}

Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013



$$rac{\partial L}{\partial W} = \sum_{t=1}^T rac{\partial L_t}{\partial W}$$

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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

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Gradients over multiple time steps:



$$\frac{\partial L}{\partial W} = \sum_{t=1}^{T} \frac{\partial L_t}{\partial W}$$
$$\frac{\partial L_T}{\partial W} = \frac{\partial L_T}{\partial h_T} \frac{\partial h_t}{\partial h_{t-1}} \dots \frac{\partial h_t}{\partial W}$$

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Gradients over multiple time steps:



$$rac{\partial L}{\partial W} = \sum_{t=1}^T rac{\partial L_t}{\partial W}$$

$$rac{\partial L_T}{\partial W} = rac{\partial L_T}{\partial h_T} rac{\partial h_t}{\partial h_{t-1}} \dots rac{\partial h_1}{\partial W} = rac{\partial L_T}{\partial h_T} (\prod_{t=2}^T rac{\partial h_t}{\partial h_{t-1}}) rac{\partial h_1}{\partial W}$$

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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

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Gradients over multiple time steps:



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Bengio et al, "Learning long-term dependencies with gradient descent is difficult", IEEE Transactions on Neural Networks, 1994 Pascanu et al, "On the difficulty of training recurrent neural networks", ICML 2013

Gradients over multiple time steps:



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Gradients over multiple time steps:



 $rac{\partial L}{\partial W} = \sum_{t=1}^T rac{\partial L_t}{\partial W}$ What if we assumed no non-linearity?

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Gradients over multiple time steps:



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Gradients over multiple time steps:



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Gradients over multiple time steps:



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Long Short Term Memory (LSTM)

Vanilla RNN

LSTM

$$h_t = \tanh\left(W\begin{pmatrix}h_{t-1}\\x_t\end{pmatrix}\right)$$

$$\begin{pmatrix} i \\ f \\ o \\ g \end{pmatrix} = \begin{pmatrix} \sigma \\ \sigma \\ \sigma \\ \tanh \end{pmatrix} W \begin{pmatrix} h_{t-1} \\ x_t \end{pmatrix}$$

$$c_t = f \odot c_{t-1} + i \odot g$$

$$h_t = o \odot \tanh(c_t)$$

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Hochreiter and Schmidhuber, "Long Short Term Memory", Neural Computation 1997

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Long Short Term Memory (LSTM)

Vanilla RNN

LSTM

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vector from

i: Input gate, whether to write to cell

g: Gate gate (?), How much to write to cell



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vector from

i: Input gate, whether to write to cell

f: Forget gate, Whether to erase cell

g: Gate gate (?), How much to write to cell



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- i: Input gate, whether to write to cell
- f: Forget gate. Whether to erase cell
- **o**: <u>Output gate</u>, How much to reveal cell

g: Gate gate (?), How much to write to cell



$$c_t = f \odot c_{t-1} + i \odot g$$
$$h_t = 0 \odot \tanh(c_t)$$

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Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]



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Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

Uninterrupted gradient flow!



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Do LSTMs solve the vanishing gradient problem?

The LSTM architecture makes it easier for the RNN to preserve information over many timesteps

- e.g. **if the f = 1 and the i = 0**, then the information of that cell is preserved indefinitely.
- By contrast, it's harder for vanilla RNN to learn a recurrent weight matrix Wh that preserves info in hidden state

LSTM **doesn't guarantee** that there is no vanishing/exploding gradient, but it does provide an easier way for the model to learn long-distance dependencies

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Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

Uninterrupted gradient flow!



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Long Short Term Memory (LSTM): Gradient Flow [Hochreiter et al., 1997]

Uninterrupted gradient flow!



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Other RNN Variants

GRU [*Learning phrase representations using rnn encoder-decoder for statistical machine translation*, Cho et al. 2014]

$$r_t = \sigma(W_{xr}x_t + W_{hr}h_{t-1} + b_r)$$

$$z_t = \sigma(W_{xz}x_t + W_{hz}h_{t-1} + b_z)$$

$$\tilde{h}_t = \tanh(W_{xh}x_t + W_{hh}(r_t \odot h_{t-1}) + b_h)$$

$$h_t = z_t \odot h_{t-1} + (1 - z_t) \odot \tilde{h}_t$$

[*LSTM: A Search Space Odyssey*, Greff et al., 2015]

[An Empirical Exploration of Recurrent Network Architectures, Jozefowicz et al., 2015]

MUT1:

$$z = \operatorname{sigm}(W_{xx}x_t + b_x)$$

$$r = \operatorname{sigm}(W_{xr}x_t + W_{hr}h_t + b_r)$$

$$h_{t+1} = \operatorname{tanh}(W_{hh}(r \odot h_t) + \operatorname{tanh}(x_t) + b_h) \odot z$$

$$+ h_t \odot (1 - z)$$

MUT2:

 $\begin{aligned} z &= \operatorname{sigm}(W_{\mathrm{xx}}x_t + W_{\mathrm{hx}}h_t + b_{\mathrm{z}}) \\ r &= \operatorname{sigm}(x_t + W_{\mathrm{hr}}h_t + b_{\mathrm{r}}) \\ h_{t+1} &= \operatorname{tanh}(W_{\mathrm{hh}}(r \odot h_t) + W_{xh}x_t + b_{\mathrm{h}}) \odot z \\ &+ h_t \odot (1 - z) \end{aligned}$

MUT3:

$$z = \operatorname{sigm}(W_{xx}x_t + W_{hx}\tanh(h_t) + b_z)$$

$$r = \operatorname{sigm}(W_{xr}x_t + W_{hr}h_t + b_r)$$

$$h_{t+1} = \operatorname{tanh}(W_{hh}(r \odot h_t) + W_{xh}x_t + b_h) \odot z$$

$$+ h_t \odot (1 - z)$$

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Neural Architecture Search for RNN architectures



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Zoph et Le, "Neural Architecture Search with Reinforcement Learning", ICLR 2017 Figures copyright Zoph et al, 2017. Reproduced with permission.

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Summary

- RNNs allow a lot of flexibility in architecture design
- Vanilla RNNs are simple but don't work very well
- Common to use LSTM or GRU: their additive interactions improve gradient flow
- Backward flow of gradients in RNN can explode or vanish.
 Exploding is controlled with gradient clipping. Vanishing is controlled with additive interactions (LSTM)
- Better/simpler architectures are a hot topic of current research, as well as new paradigms for reasoning over sequences
- Better understanding (both theoretical and empirical) is needed.

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Next time: Attention and Transformers

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