Lecture 7: Training Neural Networks

Fei-Fei Li, Jiajun Wu, Ruohan Gao

Lecture 7 - 1

Administrative: A2

A2 is out, due Monday May 2nd, 11:59pm

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Neural Networks

Linear score function:

2-layer Neural Network



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Convolutional Neural Networks



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Convolutional Layer



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Convolutional Layer

activation maps 32 28 **Convolution Layer** 28 32 6

We stack these up to get a "new image" of size 28x28x6!

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For example, if we had 6 5x5 filters, we'll

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get 6 separate activation maps:

CNN Architectures









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Learning network parameters through optimization





Vanilla Gradient Descent

while True:

Landscape image is <u>CC0 1.0</u> public domain Walking man image is <u>CC0 1.0</u> public domain weights_grad = evaluate_gradient(loss_fun, data, weights)
weights += - step_size * weights_grad # perform parameter update

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Mini-batch SGD

Loop:

- 1. Sample a batch of data
- **2. Forward** prop it through the graph (network), get loss
- 3. Backprop to calculate the gradients
- 4. Update the parameters using the gradient

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Today: Training Neural Networks

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Overview

- **1. One time set up**: activation functions, preprocessing, weight initialization, regularization, gradient checking
- **2. Training dynamics**: babysitting the learning process, parameter updates, hyperparameter optimization

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3. Evaluation: model ensembles, test-time augmentation, transfer learning

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Leaky ReLU $\max(0.1x, x)$



 $\begin{array}{l} \textbf{Maxout} \\ \max(w_1^T x + b_1, w_2^T x + b_2) \end{array}$



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 $\sigma(x)=1/(1+e^{-x})$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

Sigmoid

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Sigmoid

 $\sigma(x) = 1/(1+e^{-x})$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems:

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1. Saturated neurons "kill" the gradients

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$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x)\right)$$

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What happens when x = -10?

 $\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x)\right)$

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What happens when x = -10?

 $\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x)\right)$

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$$\sigma(x) = -0$$

$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) (1 - \sigma(x)) = 0(1 - 0) = 0$$

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What happens when x = -10? What happens when x = 0? $\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x)\right)$

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What happens when x = -10? What happens when x = 0? What happens when x = 10?

$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x)\right)$$

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$$\sigma(x) = \sim 1 \qquad \frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x)\right) = 1(1 - 1) = 0$$

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Why is this a problem? If all the gradients flowing back will be zero and weights will never change

$$\frac{\partial \sigma(x)}{\partial x} = \sigma(x) \left(1 - \sigma(x)\right)$$

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Sigmoid

 $\sigma(x) = 1/(1+e^{-x})$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems:

- 1. Saturated neurons "kill" the gradients
- 2. Sigmoid outputs are not zero-centered

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$$f\left(\sum_i w_i x_i + b
ight)$$



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What can we say about the gradients on w?

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$$f\left(\sum_i w_i x_i + b
ight)$$



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What can we say about the gradients on w?

$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b))x imes upstream_gradient$$

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$$f\left(\sum_i w_i x_i + b
ight)$$



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What can we say about the gradients on w?

We know that local gradient of sigmoid is always positive

$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b)) x imes upstream_gradient)$$

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$$f\left(\sum_i w_i x_i + b
ight)$$



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What can we say about the gradients on w?

We know that local gradient of sigmoid is always positive We are assuming x is always positive

$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b))x imes upstream_gradient$$

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$$f\left(\sum_i w_i x_i + b
ight)$$



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What can we say about the gradients on w?

We know that local gradient of sigmoid is always positive We are assuming x is always positive

So!! Sign of gradient for all w_i is the same as the sign of upstream scalar gradient!

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$$rac{\partial L}{\partial w} = \sigma(\sum_i w_i x_i + b)(1 - \sigma(\sum_i w_i x_i + b))x imes upstream_gradient$$

$$f\left(\sum_{i} w_{i}x_{i} + b\right)$$



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What can we say about the gradients on **w**? Always all positive or all negative :(

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$$f\left(\sum_{i} w_{i}x_{i} + b
ight)$$



31

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What can we say about the gradients on **w**? Always all positive or all negative :((For a single element! Minibatches help)

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Sigmoid

 $\sigma(x) = 1/(1+e^{-x})$

- Squashes numbers to range [0,1]
- Historically popular since they have nice interpretation as a saturating "firing rate" of a neuron

3 problems:

- 1. Saturated neurons "kill" the gradients
- 2. Sigmoid outputs are not zero-centered
- 3. exp() is a bit compute expensive

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- Squashes numbers to range [-1,1]

- zero centered (nice)
- still kills gradients when saturated :(

tanh(x)

[LeCun et al., 1991]

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Computes f(x) = max(0,x)

- Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)

ReLU (Rectified Linear Unit)

[Krizhevsky et al., 2012]

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Computes f(x) = max(0,x)

- Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)

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- Not zero-centered output

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ReLU (Rectified Linear Unit)



ReLU (Rectified Linear Unit)

Computes f(x) = max(0,x)

- Does not saturate (in +region)
- Very computationally efficient
- Converges much faster than sigmoid/tanh in practice (e.g. 6x)

- Not zero-centered output
- An annoyance:

hint: what is the gradient when x < 0?

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What happens when x = -10? What happens when x = 0? What happens when x = 10?

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Activation Functions

[Mass et al., 2013] [He et al., 2015]



- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
 will not "die".

Leaky ReLU $f(x) = \max(0.01x, x)$

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Activation Functions





Leaky ReLU $f(x) = \max(0.01x, x)$

- Does not saturate
- Computationally efficient
- Converges much faster than sigmoid/tanh in practice! (e.g. 6x)
 will not "die".

Parametric Rectifier (PReLU) $f(x) = \max(\alpha x, x)$ backprop into α (parameter)

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Activation Functions

[Clevert et al., 2015]

Exponential Linear Units (ELU)



- All benefits of ReLU
- Closer to zero mean outputs
- Negative saturation regime compared with Leaky ReLU adds some robustness to noise

$$f(x) = \begin{cases} x & \text{if } x > 0\\ \alpha (\exp(x) - 1) & \text{if } x \le 0 \end{cases}$$

- Computation requires exp()

(Alpha default = 1)

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Scaled Exponential Linear Units (SELU)



- Scaled version of ELU that works better for deep networks
- "Self-normalizing" property;
- Can train deep SELU networks without BatchNorm

 $f(x) = \begin{cases} \lambda x & \text{if } x > 0\\ \lambda \alpha (e^x - 1) & \text{otherwise} \end{cases}$ $\alpha = 1.6732632423543772848170429916717$ $\lambda = 1.0507009873554804934193349852946$

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Maxout "Neuron"

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- Does not have the basic form of dot product -> nonlinearity
- Generalizes ReLU and Leaky ReLU
- Linear Regime! Does not saturate! Does not die!

$$\max(w_1^Tx+b_1,w_2^Tx+b_2)$$

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Problem: doubles the number of parameters/neuron :(

TLDR: In practice:

- Use ReLU. Be careful with your learning rates
- Try out Leaky ReLU / Maxout / ELU / SELU
 - To squeeze out some marginal gains
- Don't use sigmoid or tanh

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(Assume X [NxD] is data matrix, each example in a row)

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Remember: Consider what happens when the input to a neuron is always positive...

$$f\left(\sum_i w_i x_i + b
ight)$$

allowed gradient update directions zig zag path allowed gradient update directions hypothetical optimal w vector

What can we say about the gradients on **w**? Always all positive or all negative :((this is also why you want zero-mean data!)

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(Assume X [NxD] is data matrix, each example in a row)

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In practice, you may also see **PCA** and **Whitening** of the data



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Before normalization: classification loss very sensitive to changes in weight matrix; hard to optimize After normalization: less sensitive to small changes in weights; easier to optimize



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TLDR: In practice for Images: center only

e.g. consider CIFAR-10 example with [32,32,3] images

- Subtract the mean image (e.g. AlexNet) (mean image = [32,32,3] array)
- Subtract per-channel mean (e.g. VGGNet) (mean along each channel = 3 numbers)
- Subtract per-channel mean and
 Divide by per-channel std (e.g. ResNet)
 (mean along each channel = 3 numbers)

Not common to do PCA or whitening

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Weight Initialization

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- Q: what happens when W=constant init is used?



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- First idea: Small random numbers

(gaussian with zero mean and 1e-2 standard deviation)

W = 0.01 * np.random.randn(Din, Dout)

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- First idea: Small random numbers

(gaussian with zero mean and 1e-2 standard deviation)

W = 0.01 * np.random.randn(Din, Dout)

Works ~okay for small networks, but problems with deeper networks.

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```
dims = [4096] * 7 Forward pass for a 6-layer
hs = [] net with hidden size 4096
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = 0.01 * np.random.randn(Din, Dout)
    x = np.tanh(x.dot(W))
    hs.append(x)
```

What will happen to the activations for the last layer?

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```
dims = [4096] * 7 Forward pass for a 6-layer
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W = 0.01 * np.random.randn(Din, Dout)
x = np.tanh(x.dot(W))
hs.append(x)
All a
for d
All a
for d
f
```

All activations tend to zero for deeper network layers

Q: What do the gradients dL/dW look like?

A: All zero, no learning =(

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What will happen to the activations for the last layer?

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Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

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0

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0

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0

```
"Xavier" initialization:
dims = [4096] * 7
hs = []
                          std = 1/sqrt(Din)
x = np.random.randn(16, dims[0])
for Din. Dout in zip(dims[:-1], dims[1:]):
    W = np.random.randn(Din, Dout) / np.sqrt(Din)
    x = np.tanh(x.dot(W))
    hs.append(x)
```

"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter size² * input channels

Let: $y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}$

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"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter_size² * input_channels

Let: $y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}$ Assume: $Var(x_1) = Var(x_2) = ... = Var(x_{Din})$

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"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter_size² * input_channels

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Let: $y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}$ Assume: $Var(x_1) = Var(x_2) = ... = Var(x_{Din})$ We want: $Var(y) = Var(x_i)$

Glorot and Bengio, "Understanding the difficulty of training deep feedforward neural networks", AISTAT 2010

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"Just right": Activations are nicely scaled for all layers!

For conv layers, Din is filter_size² * input_channels

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Let: $y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}$ Assume: $Var(x_1) = Var(x_2) = ... = Var(x_{Din})$ We want: $Var(y) = Var(x_i)$ $Var(y) = Var(x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din})$ [substituting value of y]

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Let: $y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}$ Assume: $Var(x_1) = Var(x_2) = ... = Var(x_{Din})$ We want: $Var(y) = Var(x_i)$

$$Var(y) = Var(x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din})$$

= Din Var(x_iw_i)
[Assume all x_i, w_i are iid]

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Let: $y = x_1 w_1 + x_2 w_2 + \dots + x_{Din} w_{Din}$ Va Assume: $Var(x_1) = Var(x_2) = \dots = Var(x_{Din})$ We want: $Var(y) = Var(x_i)$ [A

 $Var(y) = Var(x_1w_1 + x_2w_2 + ... + x_{Din}w_{Din})$ = Din Var(x_iw_i) = Din Var(x_i) Var(w_i) [Assume all x_i, w_i are zero mean]

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Let:
$$y = x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din}$$

Assume: $Var(x_1) = Var(x_2) = ... = Var(x_{Din})$
We want: $Var(y) = Var(x_i)$
Var(y) = $Var(x_1 w_1 + x_2 w_2 + ... + x_{Din} w_{Din})$
 $= Din Var(x_i w_i)$
 $= Din Var(x_i) Var(w_i)$
[Assume all x_i , w_i are iid]

So, $Var(y) = Var(x_i)$ only when $Var(w_i) = 1/Din$

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Weight Initialization: What about ReLU?

```
dims = [4096] * 7 Change from tanh to ReLU
hs = []
x = np.random.randn(16, dims[0])
for Din, Dout in zip(dims[:-1], dims[1:]):
    W = np.random.randn(Din, Dout) / np.sqrt(Din)
    x = np.maximum(0, x.dot(W))
    hs.append(x)
```

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Weight Initialization: What about ReLU?





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Weight Initialization: Kaiming / MSRA Initialization





He et al, "Delving Deep into Rectifiers: Surpassing Human-Level Performance on ImageNet Classification", ICCV 2015

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Proper initialization is an active area of research...

Understanding the difficulty of training deep feedforward neural networks by Glorot and Bengio, 2010

Exact solutions to the nonlinear dynamics of learning in deep linear neural networks by Saxe et al, 2013

Random walk initialization for training very deep feedforward networks by Sussillo and Abbott, 2014

Delving deep into rectifiers: Surpassing human-level performance on ImageNet classification by He et al., 2015

Data-dependent Initializations of Convolutional Neural Networks by Krähenbühl et al., 2015

All you need is a good init, Mishkin and Matas, 2015

Fixup Initialization: Residual Learning Without Normalization, Zhang et al, 2019

The Lottery Ticket Hypothesis: Finding Sparse, Trainable Neural Networks, Frankle and Carbin, 2019

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Training vs. Testing Error

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Beyond Training Error



help reduce training loss

But we really care about error on new data - how to reduce the gap?

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78

Early Stopping: Always do this



Stop training the model when accuracy on the validation set decreases Or train for a long time, but always keep track of the model snapshot that worked best on val

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79

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Model Ensembles

- 1. Train multiple independent models
- 2. At test time average their results

(Take average of predicted probability distributions, then choose argmax)

Enjoy 2% extra performance

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80

How to improve single-model performance?



Regularization

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81

Regularization: Add term to loss

$$L = rac{1}{N} \sum_{i=1}^{N} \sum_{j
eq y_i} \max(0, f(x_i; W)_j - f(x_i; W)_{y_i} + 1) + \lambda R(W)$$

In common use:L2 regularization $R(W) = \sum_k \sum_l W_{k,l}^2$ (Weight decay)L1 regularization $R(W) = \sum_k \sum_l |W_{k,l}|$ Elastic net (L1 + L2) $R(W) = \sum_k \sum_l \beta W_{k,l}^2 + |W_{k,l}|$

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82

In each forward pass, randomly set some neurons to zero Probability of dropping is a hyperparameter; 0.5 is common

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83

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Srivastava et al, "Dropout: A simple way to prevent neural networks from overfitting", JMLR 2014

p = 0.5 # probability of keeping a unit active. higher = less dropout

```
def train_step(X):
    """ X contains the data """
```

```
# forward pass for example 3-layer neural network
H1 = np.maximum(0, np.dot(W1, X) + b1)
U1 = np.random.rand(*H1.shape)
```

backward pass: compute gradients... (not shown)
perform parameter update... (not shown)

Example forward pass with a 3-layer network using dropout



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How can this possibly be a good idea?



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Forces the network to have a redundant representation; Prevents co-adaptation of features



85

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How can this possibly be a good idea?



Another interpretation:

Dropout is training a large **ensemble** of models (that share parameters).

Each binary mask is one model

An FC layer with 4096 units has $2^{4096} \sim 10^{1233}$ possible masks! Only ~ 10^{82} atoms in the universe...

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Dropout makes our output random!



87

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Want to "average out" the randomness at test-time

$$y = f(x) = E_z \left[f(x, z) \right] = \int p(z) f(x, z) dz$$

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But this integral seems hard ...

Want to approximate the integral

$$y = f(x) = E_z \left[f(x, z) \right] = \int p(z) f(x, z) dz$$

Consider a single neuron.



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Want to approximate the integral

$$y = f(x) = E_z [f(x, z)] = \int p(z) f(x, z) dz$$

89

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Consider a single neuron.



At test time we have:
$$E[a] = w_1 x + w_2 y_3$$

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Want to approximate the integral

$$y = f(x) = E_z \left[f(x, z) \right] = \int p(z) f(x, z) dz$$

90

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Consider a single neuron.



At test time we have: $E[a] = w_1 x + w_2 y$ During training we have: $E[a] = \frac{1}{4}(w_1 x + w_2 y) + \frac{1}{4}(w_1 x + 0y) + \frac{1}{4}(0x + w_2 y) + \frac{1}{4}(0x + w_2 y) = \frac{1}{2}(w_1 x + w_2 y)$

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Want to approximate the integral

$$y = f(x) = E_z \left[f(x, z) \right] = \int p(z) f(x, z) dz$$

91

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Consider a single neuron.



At test time we have: $E[a] = w_1 x + w_2 y$ During training we have: $E[a] = \frac{1}{4}(w_1 x + w_2 y) + \frac{1}{4}(w_1 x + 0y)$ At test time, **multiply** by dropout probability $= \frac{1}{2}(w_1 x + w_2 y)$

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def predict(X):

```
# ensembled forward pass
H1 = np.maximum(0, np.dot(W1, X) + b1) * p # NOTE: scale the activations
H2 = np.maximum(0, np.dot(W2, H1) + b2) * p # NOTE: scale the activations
out = np.dot(W3, H2) + b3
```

At test time all neurons are active always => We must scale the activations so that for each neuron: <u>output at test time</u> = <u>expected output at training time</u>

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92

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""" Vanilla Dropout: Not recommended implementation (see notes below) """

p = 0.5 # probability of keeping a unit active. higher = less dropout



Dropout Summary

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93

More common: "Inverted dropout"

p = 0.5 # probability of keeping a unit active. higher = less dropout



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Regularization: A common pattern

Training: Add some kind of randomness

$$y = f_W(x, z)$$

Testing: Average out randomness (sometimes approximate)

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95

$$y = f(x) = E_z \left[f(x, z) \right] = \int p(z) f(x, z) dz$$

Regularization: A common pattern

Training: Add some kind of randomness

$$y = f_W(x, z)$$

Testing: Average out randomness (sometimes approximate)

$$y = f(x) = E_z \left[f(x, z) \right] = \int p(z) f(x, z) dz$$

Example: Batch Normalization

Training: Normalize using stats from random minibatches

Testing: Use fixed stats to normalize

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96

Regularization: Data Augmentation



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97

Regularization: Data Augmentation



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98

Data Augmentation Horizontal Flips





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Data Augmentation Random crops and scales

Training: sample random crops / scales ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



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100

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Data Augmentation Random crops and scales

Training: sample random crops / scales ResNet:

- 1. Pick random L in range [256, 480]
- 2. Resize training image, short side = L
- 3. Sample random 224 x 224 patch



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101

Testing: average a fixed set of crops ResNet:

- 1. Resize image at 5 scales: {224, 256, 384, 480, 640}
- 2. For each size, use 10 224 x 224 crops: 4 corners + center, + flips

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Data Augmentation Color Jitter

Simple: Randomize contrast and brightness



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102

Data Augmentation Color Jitter

Simple: Randomize contrast and brightness



More Complex:

- 1. Apply PCA to all [R, G, B] pixels in training set
- 2. Sample a "color offset" along principal component directions
- 3. Add offset to all pixels of a training image

(As seen in [Krizhevsky et al. 2012], ResNet, etc)

103

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Data Augmentation

- Get creative for your problem!
 - Examples of data augmentations:
 - translation
 - rotation
 - stretching
 - shearing,
 - lens distortions, ... (go crazy)

104

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Automatic Data Augmentation



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105

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Cubuk et al., "AutoAugment: Learning Augmentation Strategies from Data", CVPR 2019

Regularization: A common pattern

Training: Add random noise **Testing**: Marginalize over the noise

Examples:

Dropout Batch Normalization Data Augmentation

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106

Regularization: DropConnect

Training: Drop connections between neurons (set weights to 0) **Testing**: Use all the connections

Examples:

Dropout Batch Normalization Data Augmentation DropConnect



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107

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Wan et al, "Regularization of Neural Networks using DropConnect", ICML 2013

Regularization: Fractional Pooling Training: Use randomized pooling regions Testing: Average predictions from several regions

Examples:

Dropout Batch Normalization Data Augmentation DropConnect Fractional Max Pooling



108

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Graham, "Fractional Max Pooling", arXiv 2014
Regularization: Stochastic Depth

Training: Skip some layers in the network **Testing**: Use all the layer

Examples:

Dropout Batch Normalization Data Augmentation DropConnect Fractional Max Pooling Stochastic Depth



109

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Huang et al, "Deep Networks with Stochastic Depth", ECCV 2016

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Regularization: Cutout Training: Set random image regions to zero Testing: Use full image

Examples:

Dropout Batch Normalization Data Augmentation DropConnect Fractional Max Pooling Stochastic Depth Cutout / Random Crop

DeVries and Taylor, "Improved Regularization of Convolutional Neural Networks with Cutout", arXiv 2017



Works very well for small datasets like CIFAR, less common for large datasets like ImageNet

110

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Regularization: Mixup Training: Train on random blends of images Testing: Use original images



Examples:

Dropout Batch Normalization Data Augmentation DropConnect Fractional Max Pooling Stochastic Depth Cutout / Random Crop Mixup







CNN Target label: cat: 0.4 dog: 0.6

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Randomly blend the pixels of pairs of training images, e.g. 40% cat, 60% dog

Zhang et al, "mixup: Beyond Empirical Risk Minimization", ICLR 2018

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Regularization - In practice Training: Add random noise Testing: Marginalize over the noise

Examples:

Dropout Batch Normalization Data Augmentation DropConnect Fractional Max Pooling Stochastic Depth Cutout / Random Crop Mixup

- Consider dropout for large fully-connected layers
- Batch normalization and data augmentation almost always a good idea
- Try cutout and mixup especially for small classification datasets

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112

Choosing Hyperparameters (without tons of GPUs)

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Step 1: Check initial loss

Turn off weight decay, sanity check loss at initialization e.g. log(C) for softmax with C classes

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114

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Step 1: Check initial loss
Step 2: Overfit a small sample

Try to train to 100% training accuracy on a small sample of training data (~5-10 minibatches); fiddle with architecture, learning rate, weight initialization

Loss not going down? LR too low, bad initialization Loss explodes to Inf or NaN? LR too high, bad initialization

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Step 1: Check initial lossStep 2: Overfit a small sampleStep 3: Find LR that makes loss go down

Use the architecture from the previous step, use all training data, turn on small weight decay, find a learning rate that makes the loss drop significantly within ~100 iterations

Good learning rates to try: 1e-1, 1e-2, 1e-3, 1e-4

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Step 1: Check initial loss
Step 2: Overfit a small sample
Step 3: Find LR that makes loss go down
Step 4: Coarse grid, train for ~1-5 epochs

Choose a few values of learning rate and weight decay around what worked from Step 3, train a few models for \sim 1-5 epochs.

Good weight decay to try: 1e-4, 1e-5, 0

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Step 1: Check initial loss

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- Step 2: Overfit a small sample
- Step 3: Find LR that makes loss go down
- Step 4: Coarse grid, train for ~1-5 epochs
- Step 5: Refine grid, train longer

Pick best models from Step 4, train them for longer (~10-20 epochs) without learning rate decay

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- Step 1: Check initial loss
- Step 2: Overfit a small sample
- Step 3: Find LR that makes loss go down
- **Step 4**: Coarse grid, train for ~1-5 epochs
- Step 5: Refine grid, train longer
- Step 6: Look at loss and accuracy curves

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Look at learning curves!



Losses may be noisy, use a scatter plot and also plot moving average to see trends better

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Cross-validation

We develop "command centers" to visualize all our models training with different hyperparameters

check out weights and biases



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You can plot all your loss curves for different hyperparameters on a single plot



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Don't look at accuracy or loss curves for too long!



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- Step 1: Check initial loss
- Step 2: Overfit a small sample
- Step 3: Find LR that makes loss go down
- **Step 4**: Coarse grid, train for ~1-5 epochs
- Step 5: Refine grid, train longer
- Step 6: Look at loss and accuracy curves

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-127

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Step 7: GOTO step 5

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Random Search vs. Grid Search

Random Search for Hyper-Parameter Optimization Bergstra and Bengio, 2012

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Grid Layout

<u>Random Layout</u>



Illustration of Bergstra et al., 2012 by Shayne Longpre, copyright CS231n 2017

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Summary

- Improve your training error:
 - Optimizers
 - Learning rate schedules
- Improve your test error:
 - Regularization
 - Choosing Hyperparameters

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129

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Summary We looked in detail at:



- Activation Functions (use ReLU)
- Data Preprocessing (images: subtract mean)
- Weight Initialization (use Xavier/He init)
- Batch Normalization (use this!)
- Transfer learning (use this if you can!)

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Next time: Visualizing and Understanding

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