

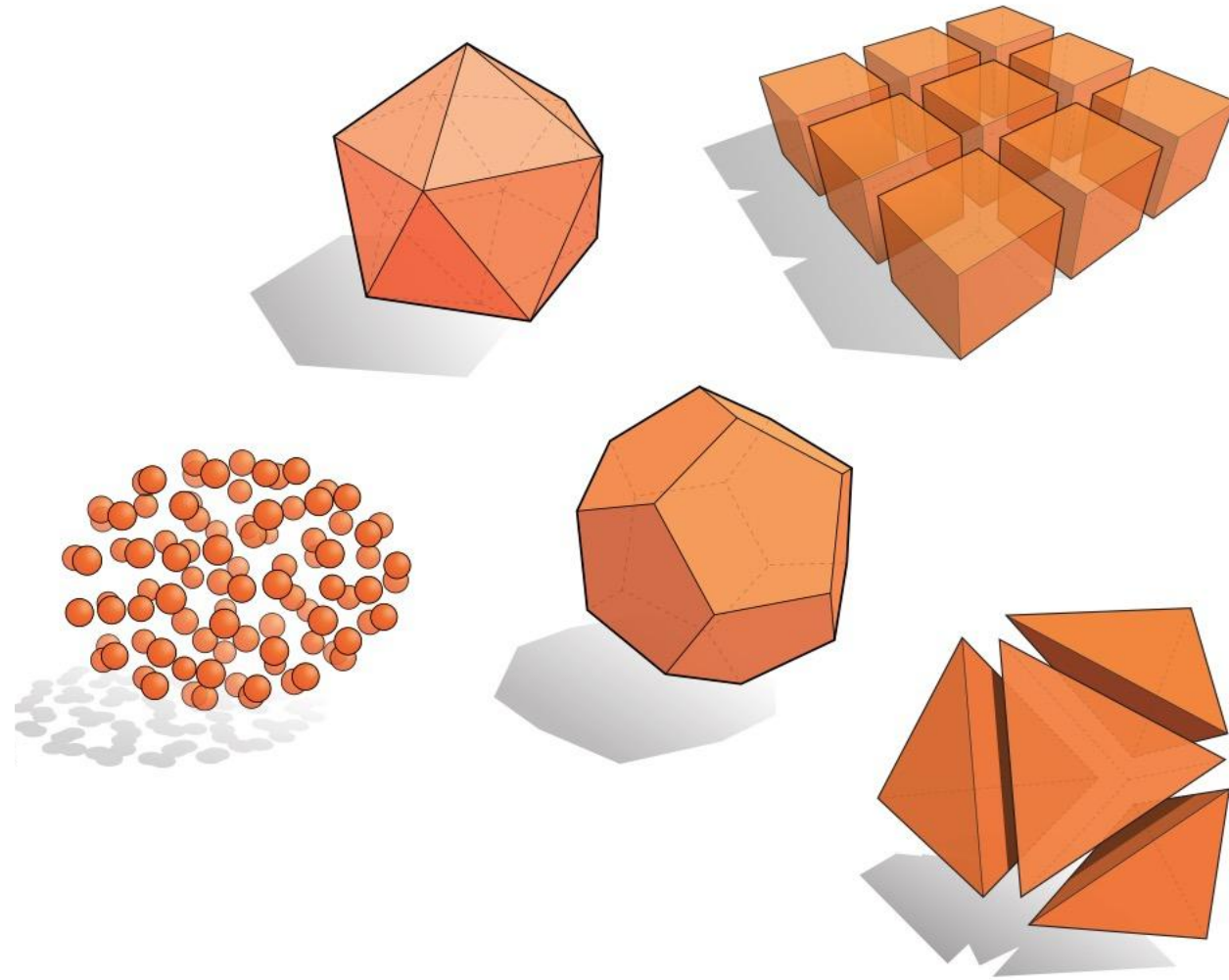
CS 231N Lecture 16: 3D Vision







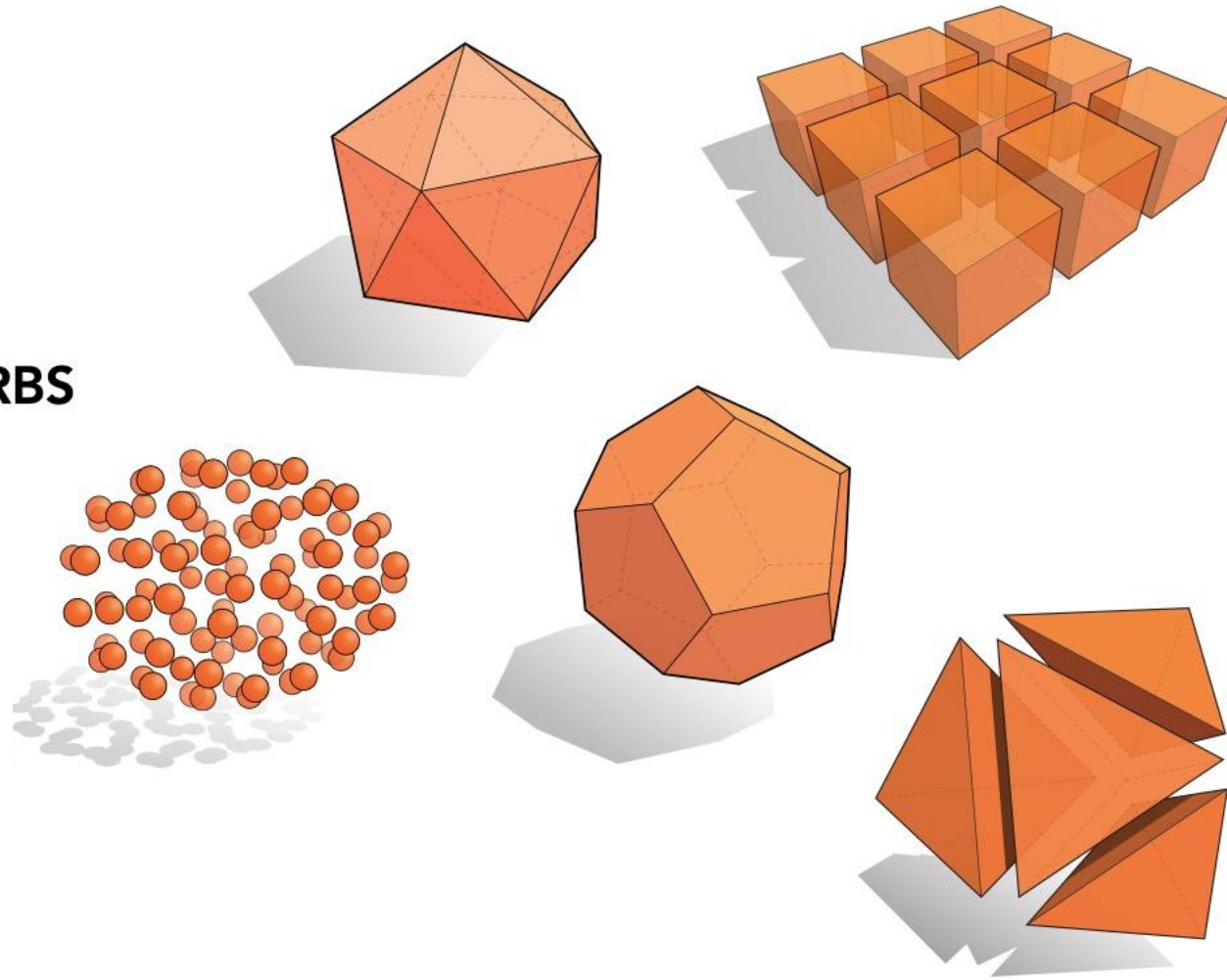
Many Ways to Represent Geometry



Many Ways to Represent Geometry

Explicit

- point cloud
- polygon mesh
- subdivision, NURBS
- ...



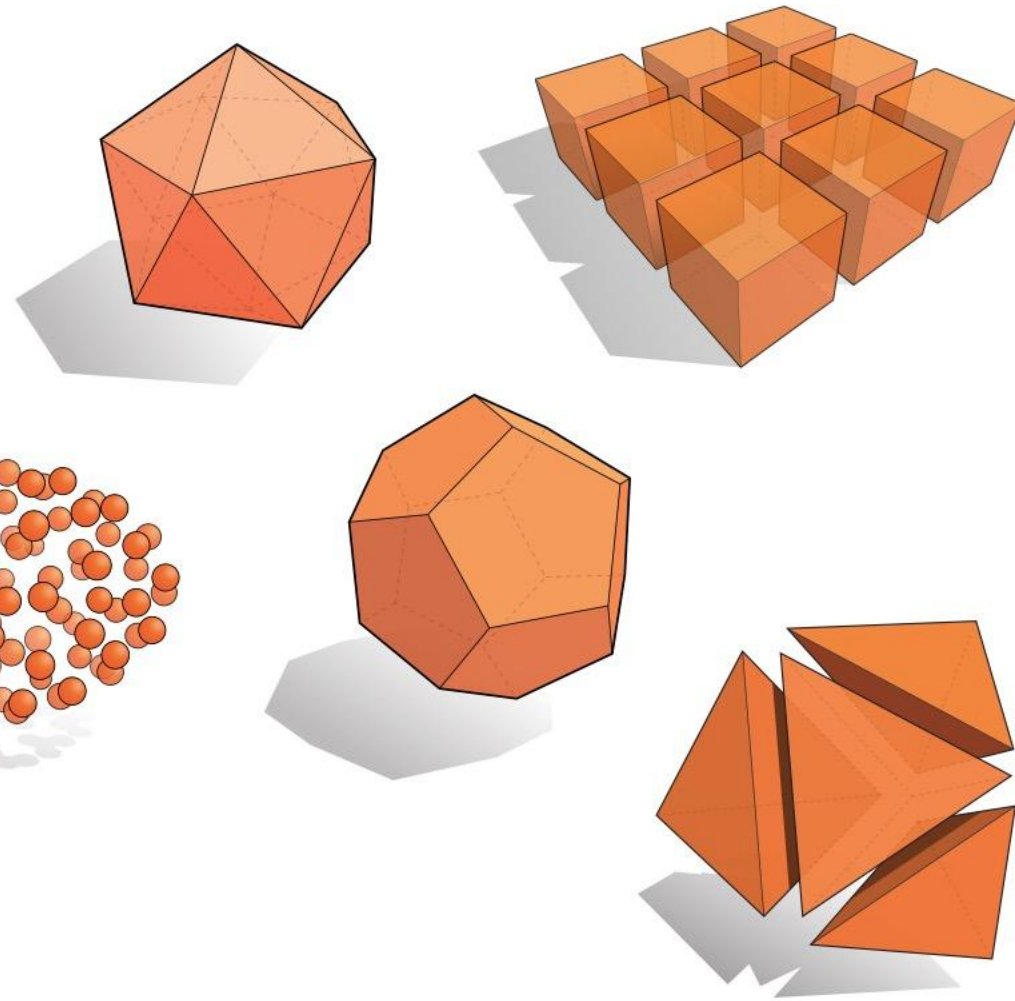
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Implicit

- level sets
- algebraic surface
- distance functions
- ...



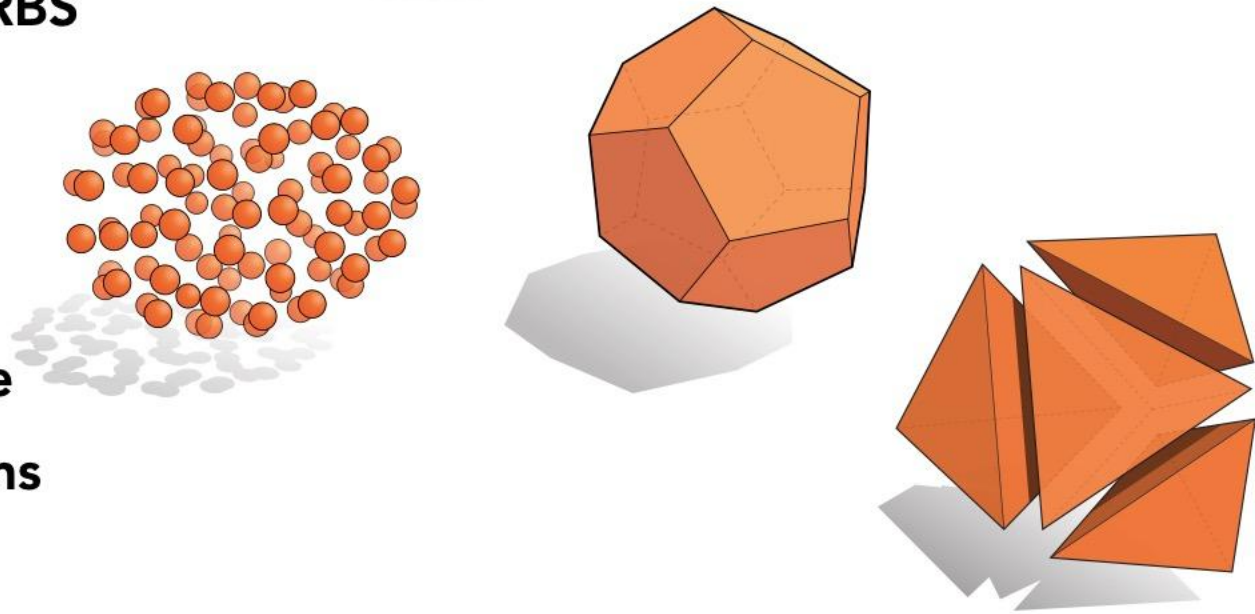
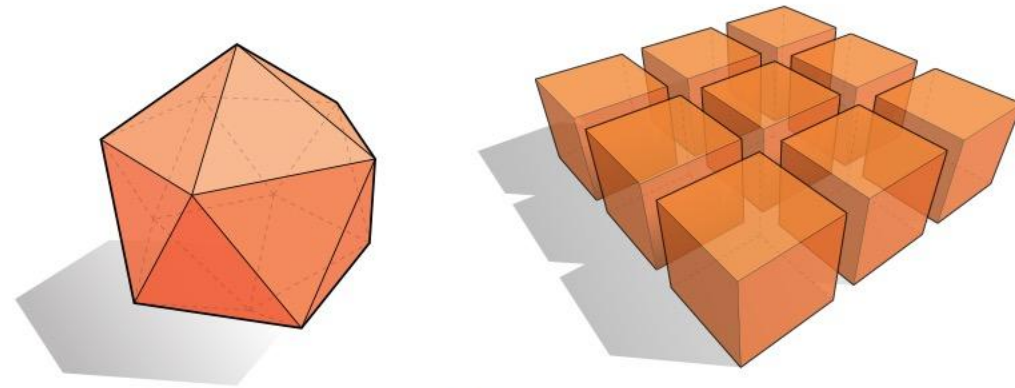
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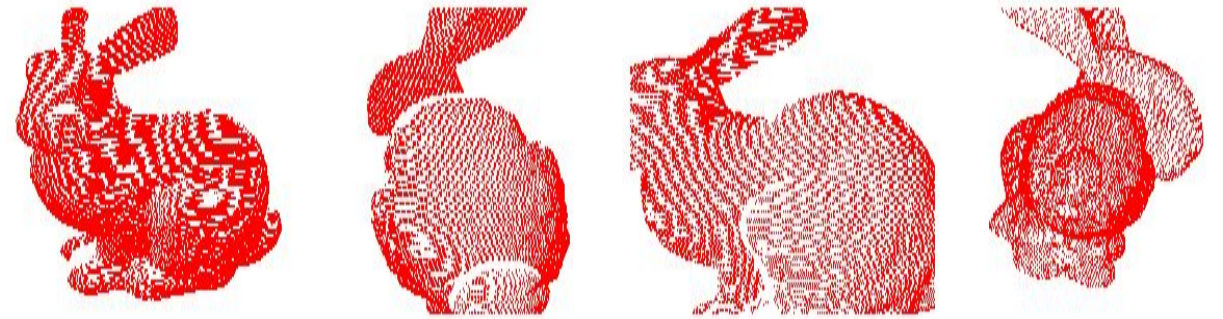


Each choice best suited to a different task/type of geometry

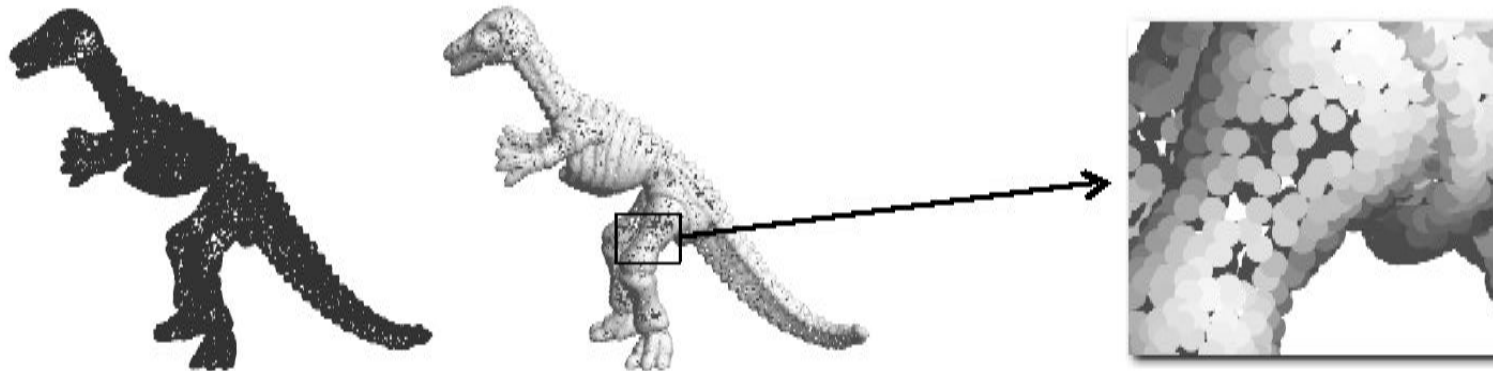
Representation Considerations

- Needs to be stored in the computer
- Creation of new shapes
 - Input metaphors, interfaces...
- Operations
 - Editing, simplification, smoothing, filtering, repairing...
- Rendering
 - Rasterization, ray tracing...
- Animation

Point Clouds

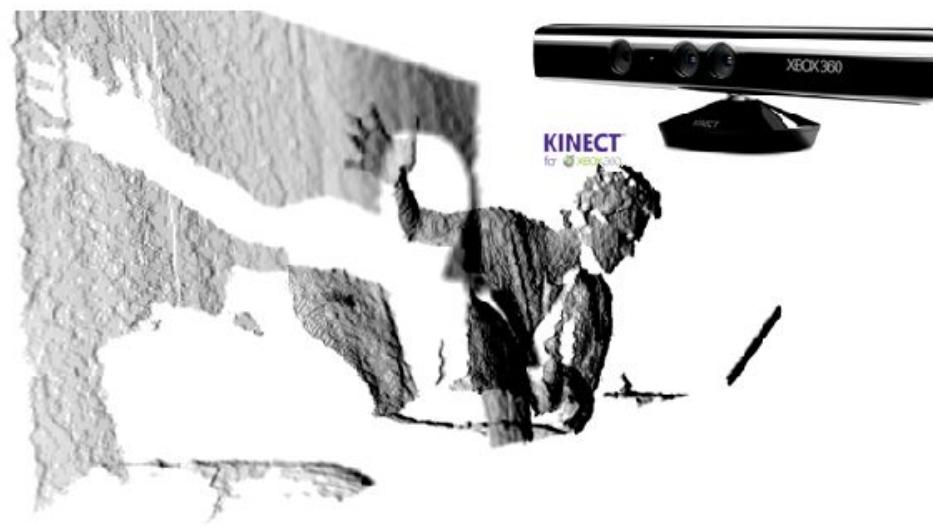
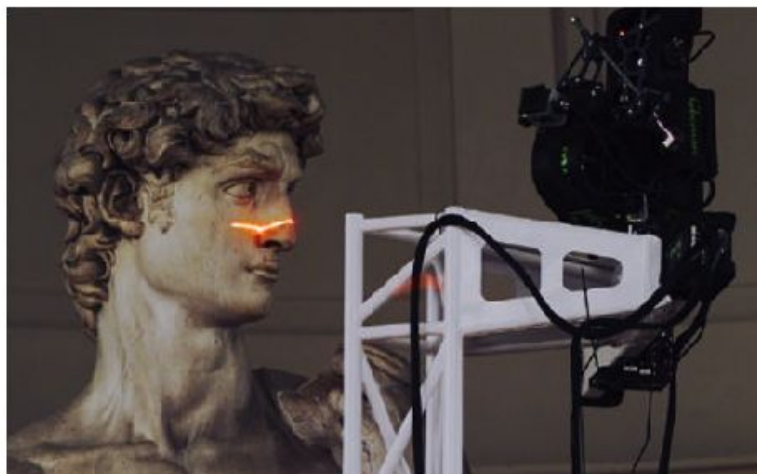


- Simplest representation: **only points**, no connectivity
- Collection of (x,y,z) coordinates, possibly with normal
- Points with orientation are called **surfels**

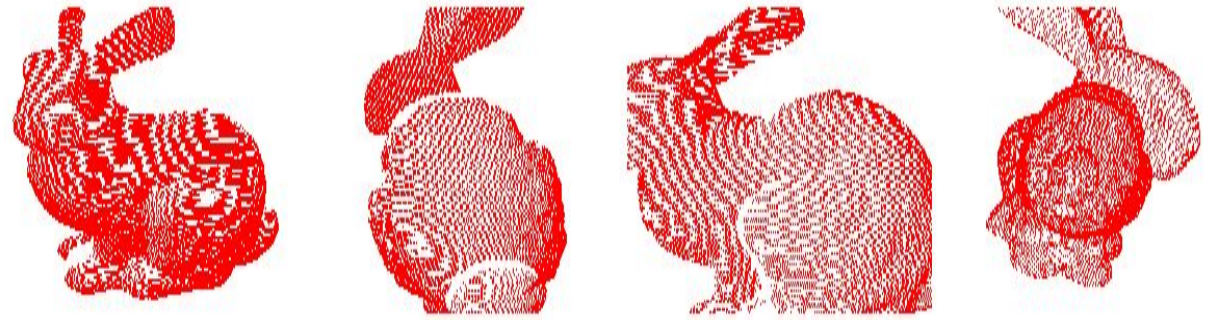


shading needs normals!

Output of Acquisition



Point Clouds



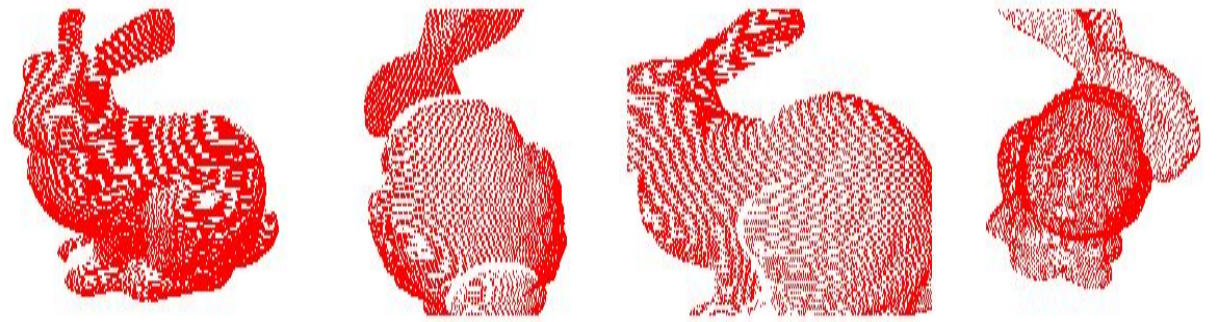
- Simplest representation: **only points**, no connectivity
- Collection of (x,y,z) coordinates, possibly with normal
- Points with orientation are called **surfels**

- Often results from scanners
- Potentially noisy
- Registration of multiple images

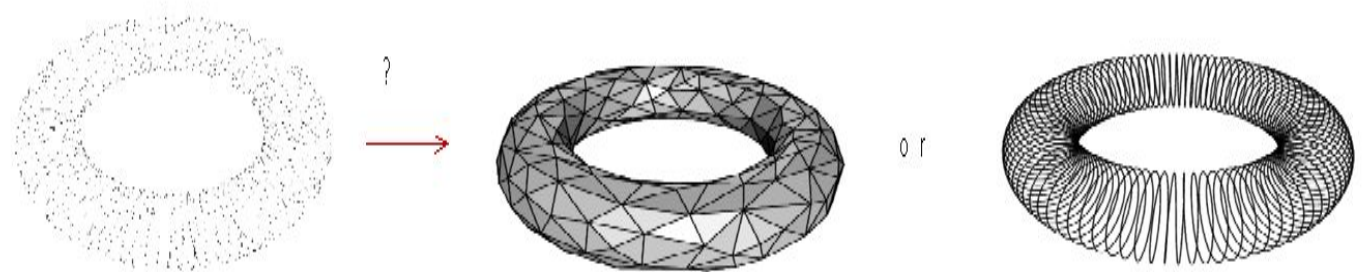


set of raw scans

Point Clouds

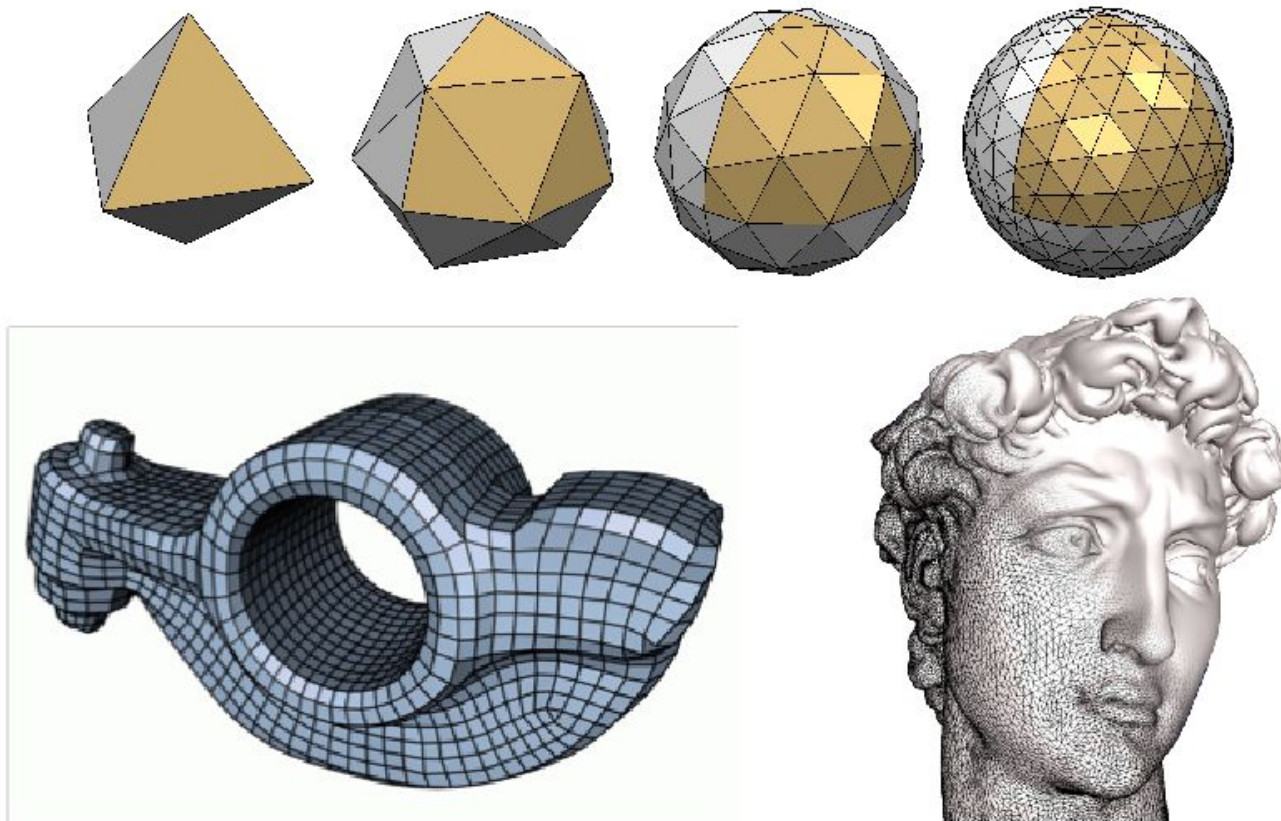


- Easily represent any kind of geometry
- Useful for large datasets
- Difficult to draw in undersampled regions
- Other limitations:
 - No simplification or subdivision
 - No direction smooth rendering
 - No topological information



Polygonal Meshes

- Boundary representations of objects



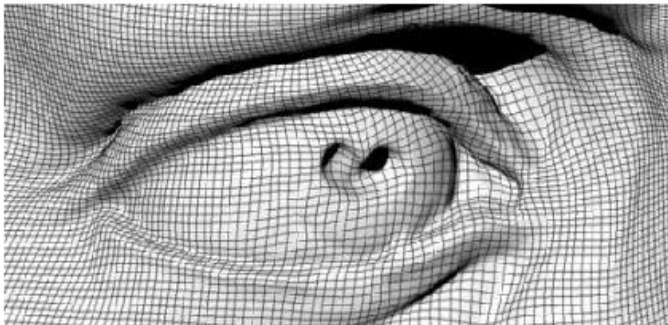
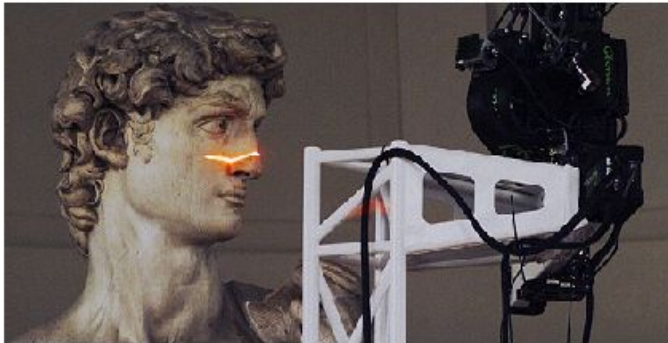
A Large Triangle Mesh

David

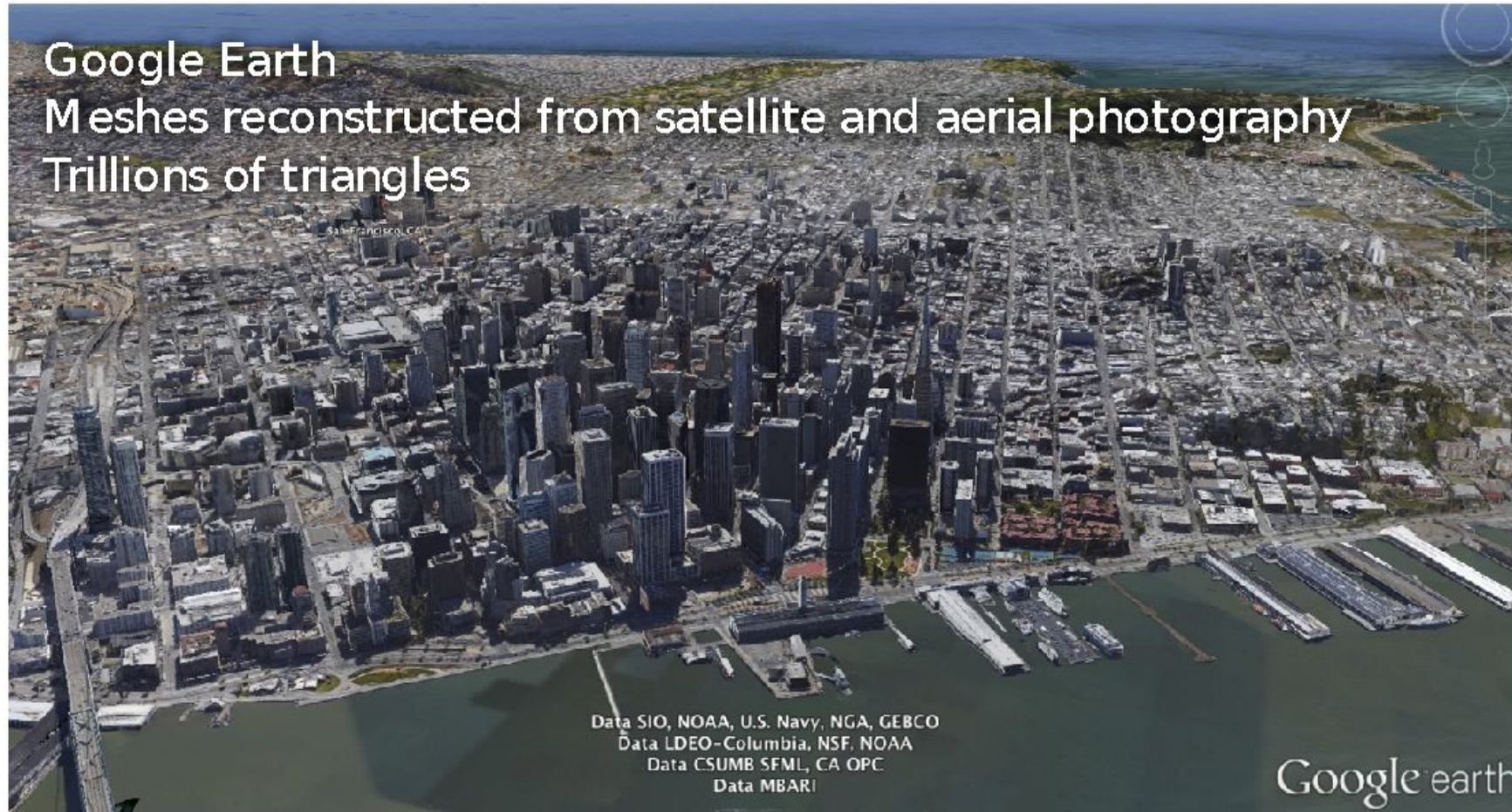
Digital Michelangelo Project

28,184,526 vertices

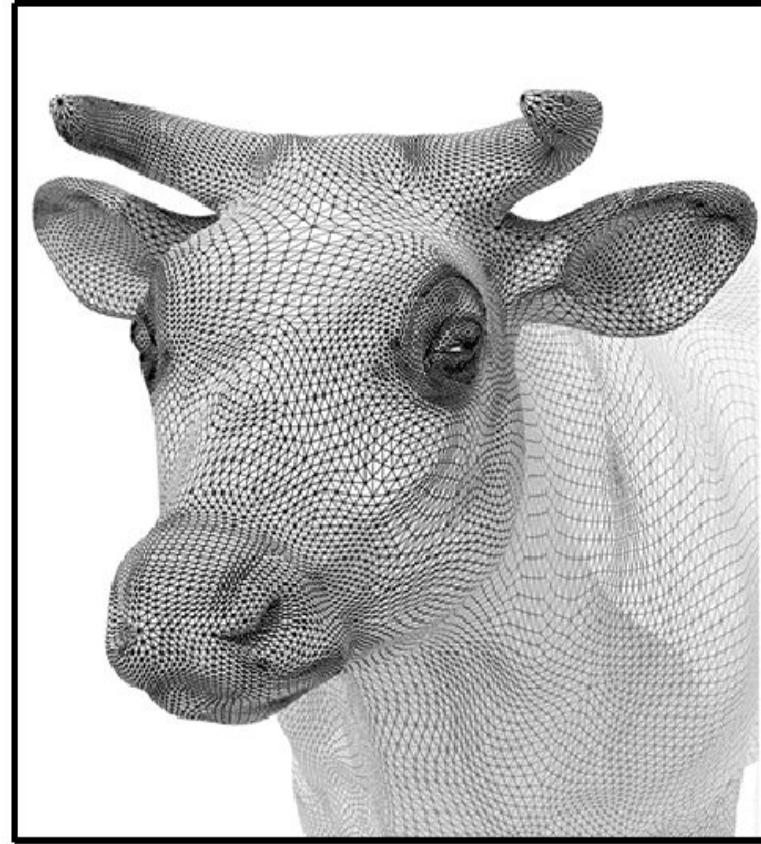
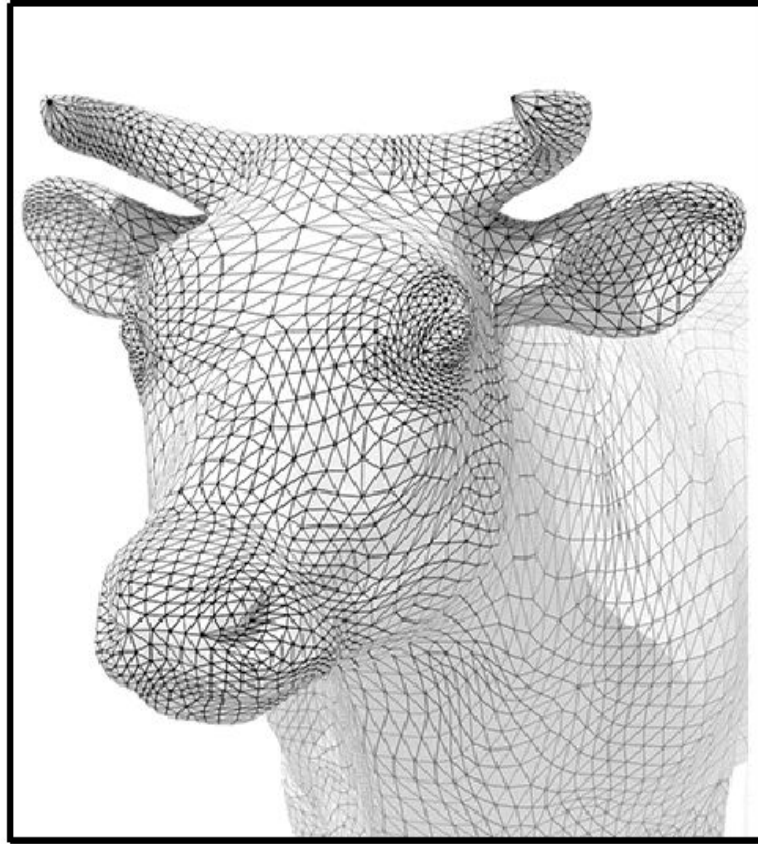
56,230,343 triangles



A Very Large Triangle Mesh

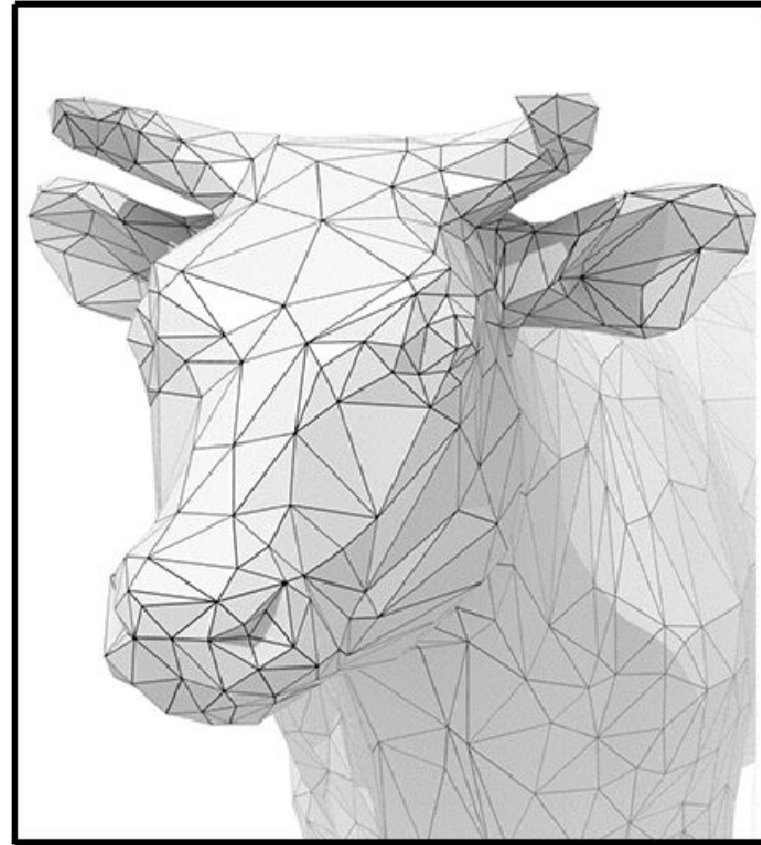
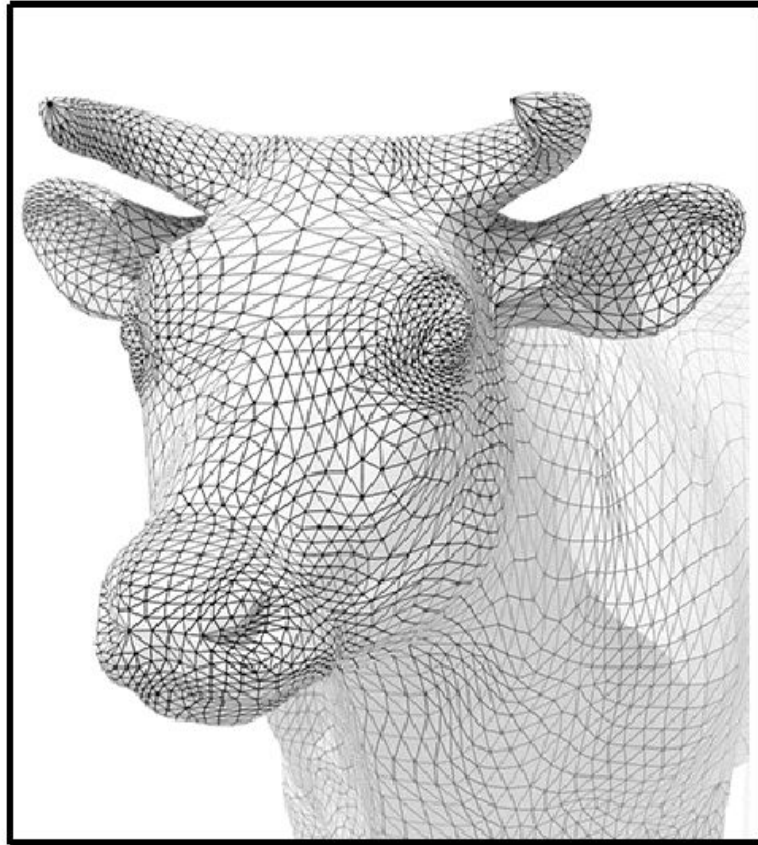


Mesh Upsampling – Subdivision



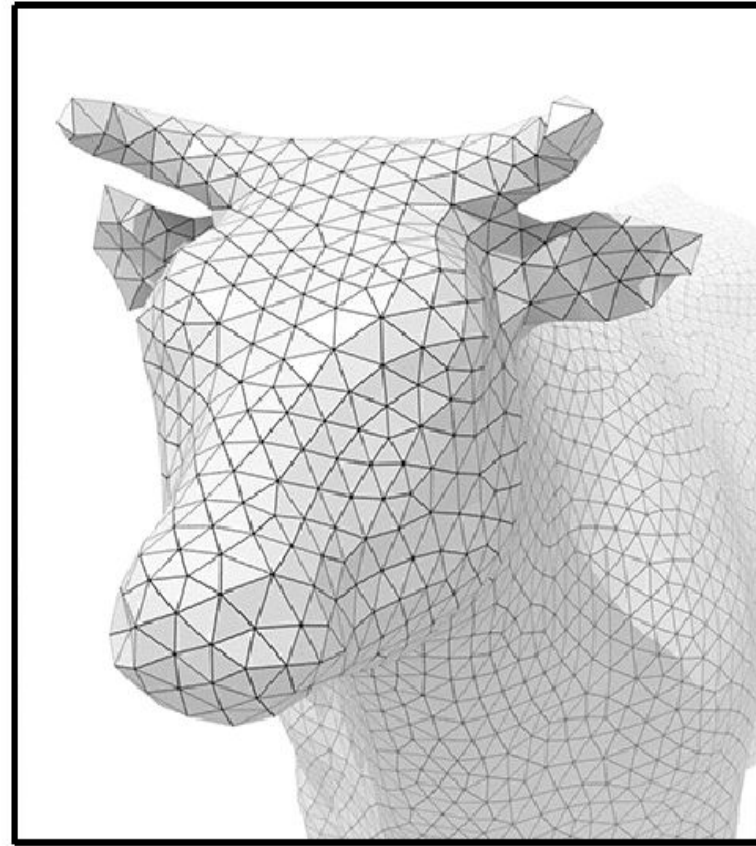
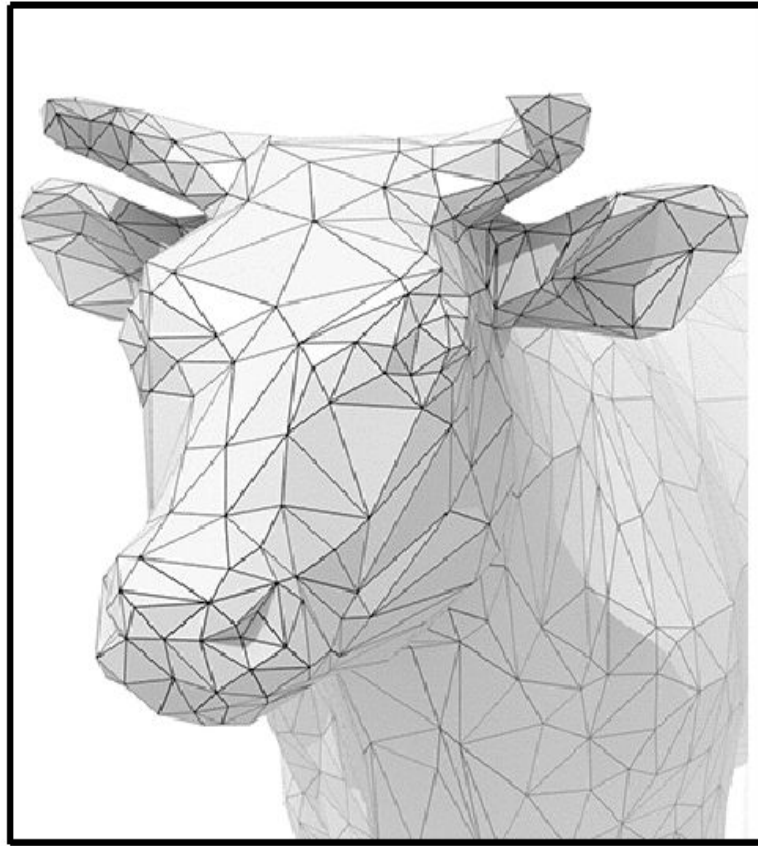
Increase resolution via interpolation

Mesh Downsampling – Simplification



Decrease resolution; try to preserve shape/appearance

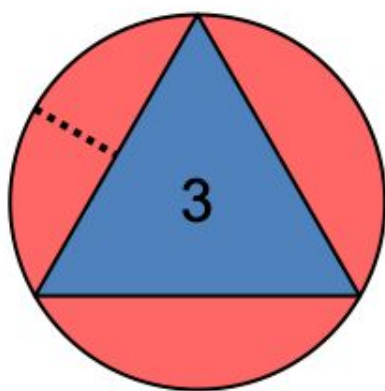
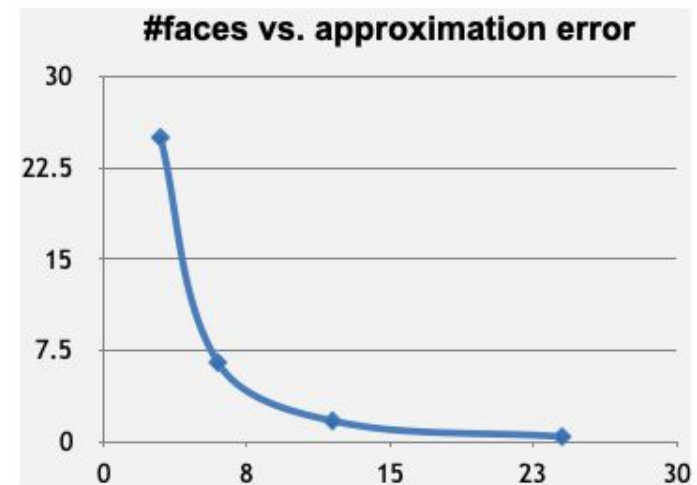
Mesh Regularization



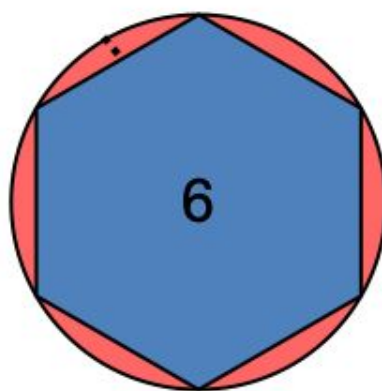
Modify sample distribution to improve quality

Meshes as Approximations of Smooth Surfaces

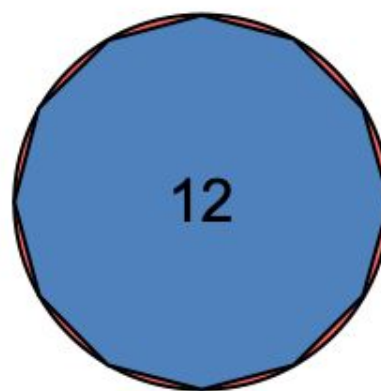
- Piecewise linear approximation
- Error is $O(h^2)$



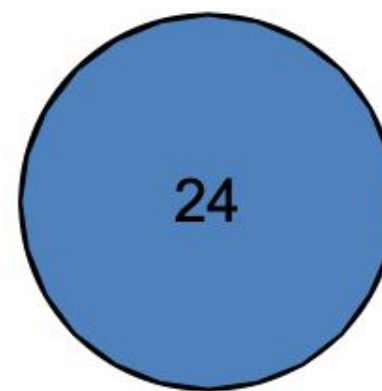
25%



6.5%



1.7%



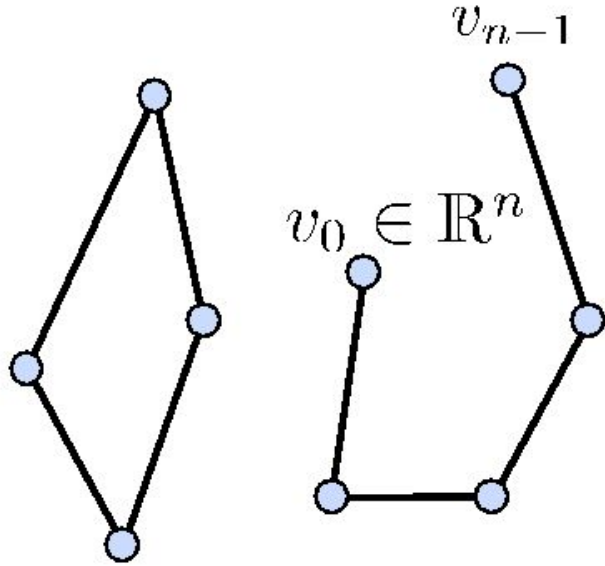
0.4%

Polygonal Meshes

- Polygonal meshes are a good representation
 - approximation $O(h^2)$
 - arbitrary topology
 - adaptive refinement
 - efficient rendering

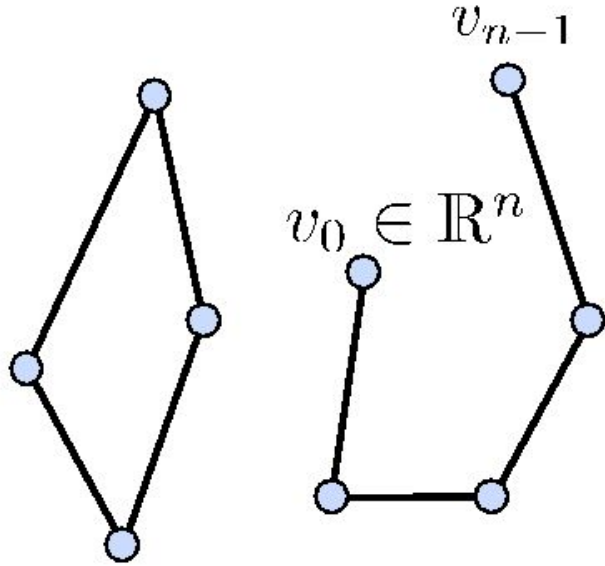


Polygon



- Vertices: v_0, v_1, \dots, v_{n-1}
- Edges: $\{(v_0, v_1), \dots, (v_{n-2}, v_{n-1})\}$

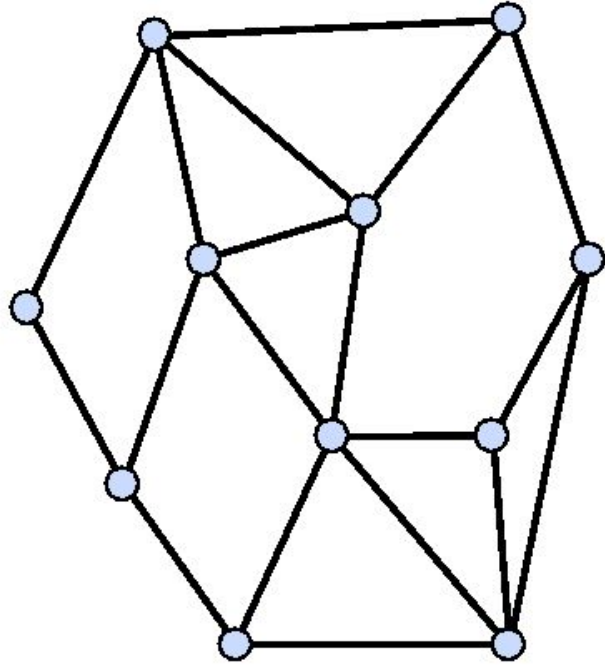
Polygon



- Vertices: v_0, v_1, \dots, v_{n-1}
- Edges: $\{(v_0, v_1), \dots, (v_{n-2}, v_{n-1})\}$
- Closed: $v_0 = v_{n-1}$
- Planar: all vertices on a plane
- Simple: not self-intersecting

Polygonal Mesh

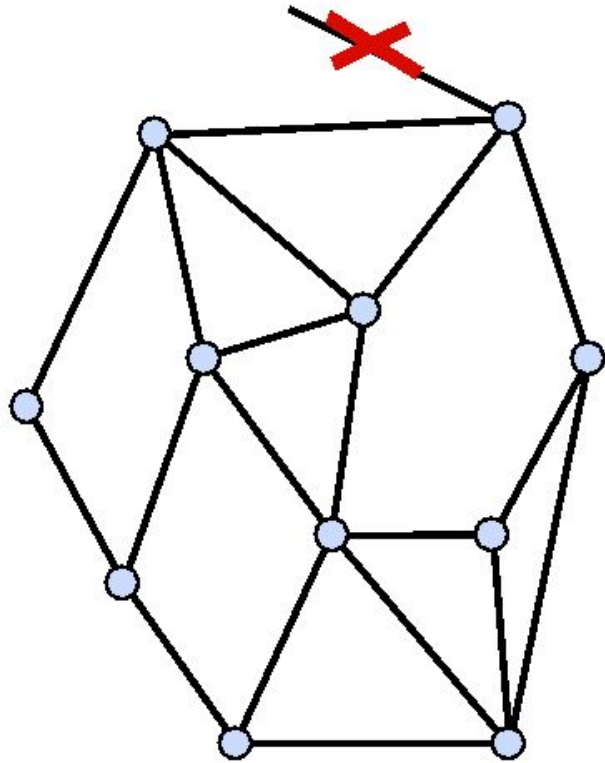
- A finite set M of closed, simple polygons Q_i is a polygonal mesh
- The intersection of two polygons in M is either empty, a vertex, or an edge



$$M = \langle V, E, F \rangle$$

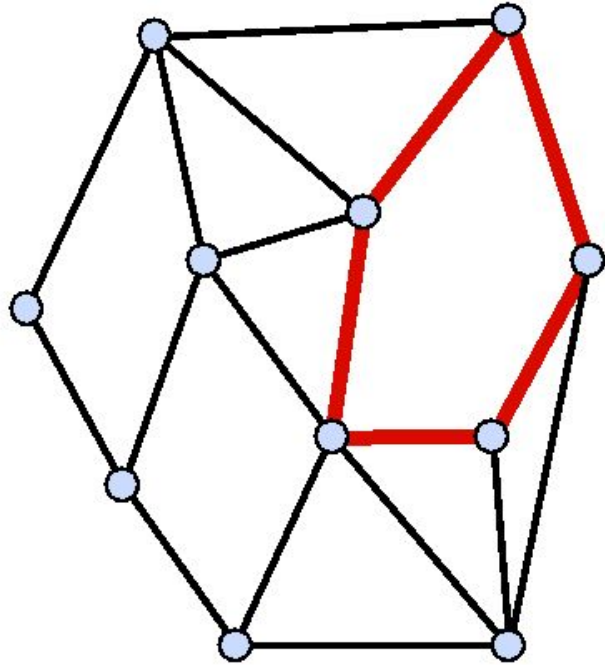
vertices edges faces

Polygonal Mesh



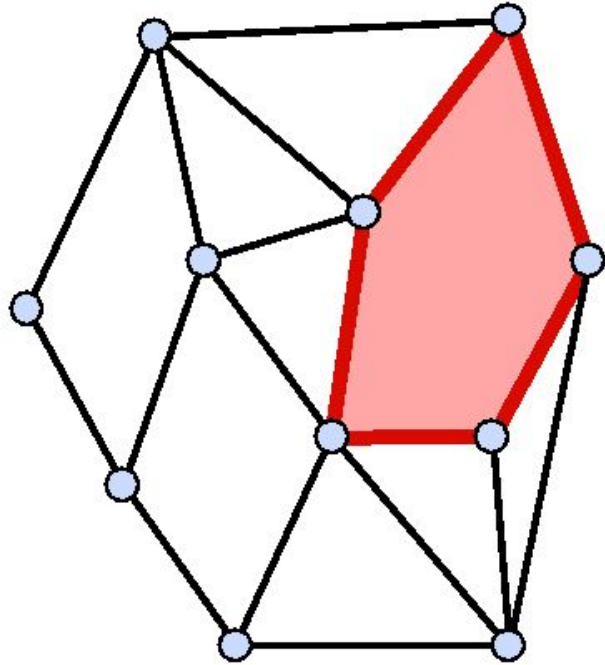
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- Each Q_i defines a **face** of the polygonal mesh

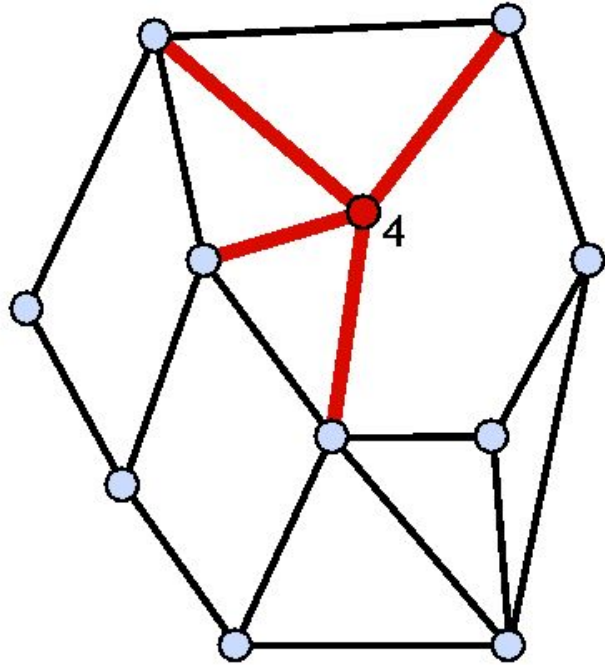
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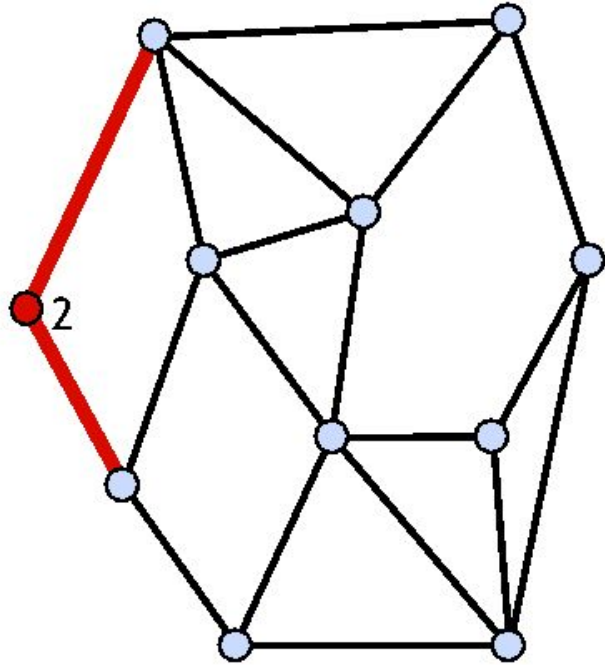
Polygonal Mesh

- Vertex **degree** or **valence** = number of incident edges



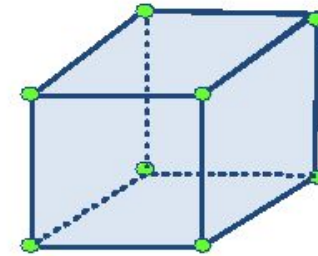
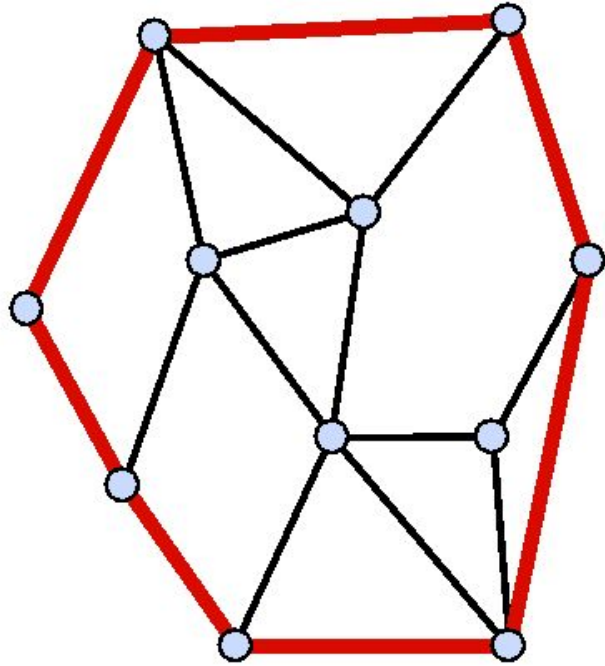
Polygonal Mesh

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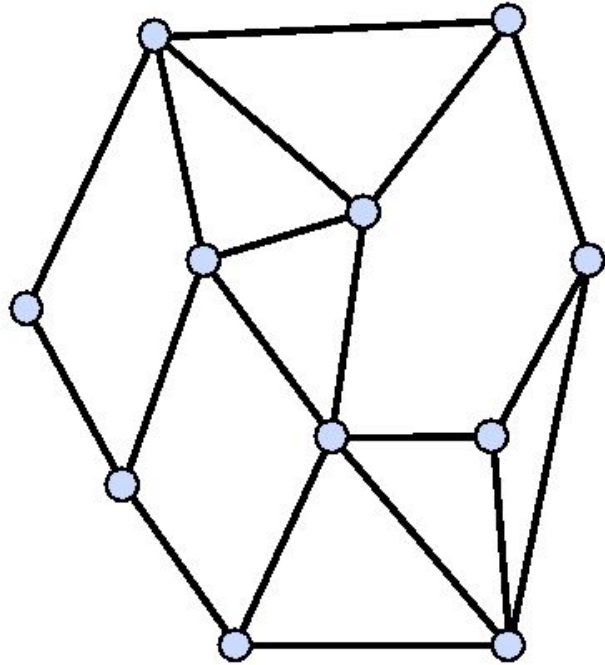
Polygonal Mesh

- Boundary: the set of all edges that belong to only one polygon
 - Either empty or forms closed loops
 - If empty, then the polygonal mesh is closed



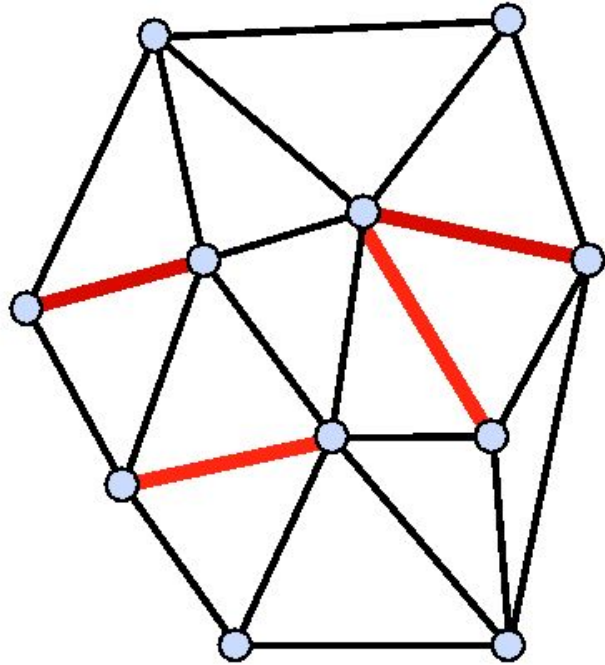
Triangulation

- Polygonal mesh where every face is a triangle



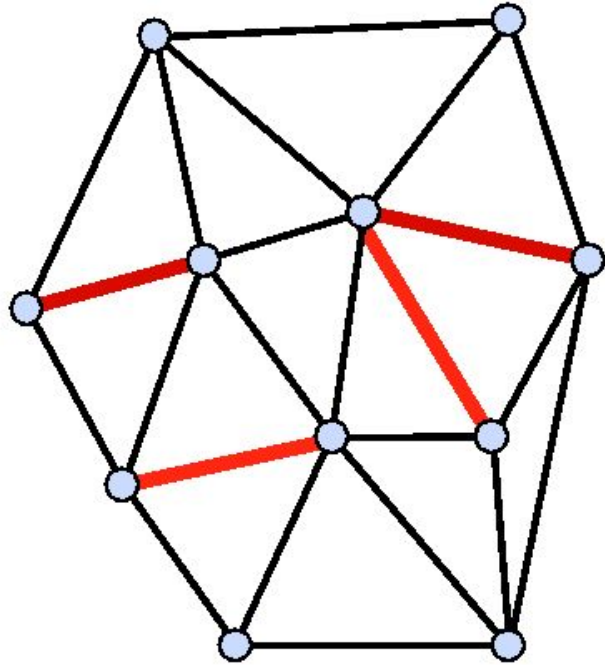
Triangulation

- Polygonal mesh where every face is a triangle



Triangulation

- Polygonal mesh where every face is a triangle



- Simplifies data structures
- Simplifies rendering
- Simplifies algorithms
- Each face planar and convex
- Any polygon can be triangulated

Data Structures

- What should be stored?
 - Geometry: 3D coordinates



Data Structures



- What should be stored?
 - Geometry: 3D coordinates
 - Connectivity
 - Adjacency relationships

Data Structures



- What should be stored?
 - Geometry: 3D coordinates
 - Connectivity
 - Adjacency relationships
 - Attributes
 - Normal, color, texture coordinates
 - Per vertex, face, edge

Simple Data Structures: Indexed Face Set

- Used in formats
 - OBJ , OFF, WRL
- Storage
 - Vertex: position
 - Face: vertex indices
 - 12 bytes per vertex
 - 12 bytes per face
 - $36*v$ bytes for the mesh
- No explicit neighborhood info

Vertices			
v0	x0	y0	z0
v1	x1	x1	z1
v2	x2	y2	z2
v3	x3	y3	z3
v4	x4	y4	z4
v5	x5	y5	z5
v6	x6	y6	z6
...

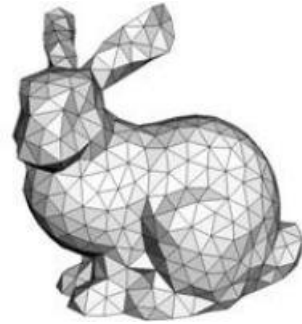
Triangles			
t0	v0	v1	v2
t1	v0	v1	v3
t2	v2	v4	v3
t3	v5	v2	v6
...

Shape Representations

Non-parametric



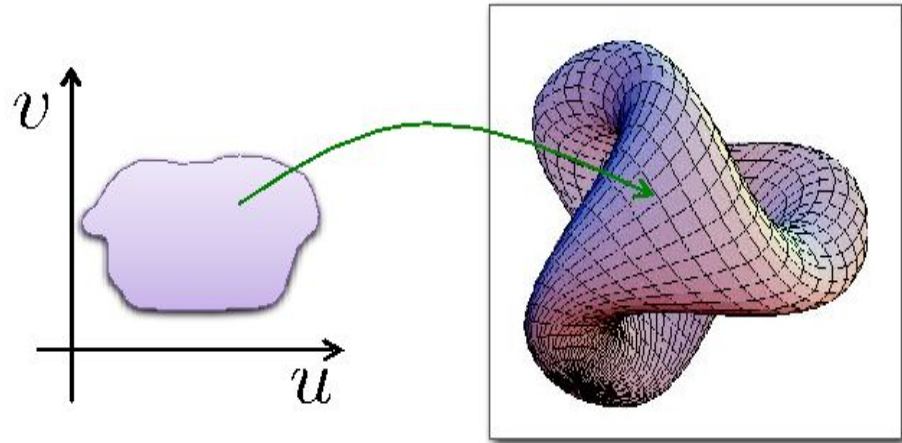
Points



Meshes

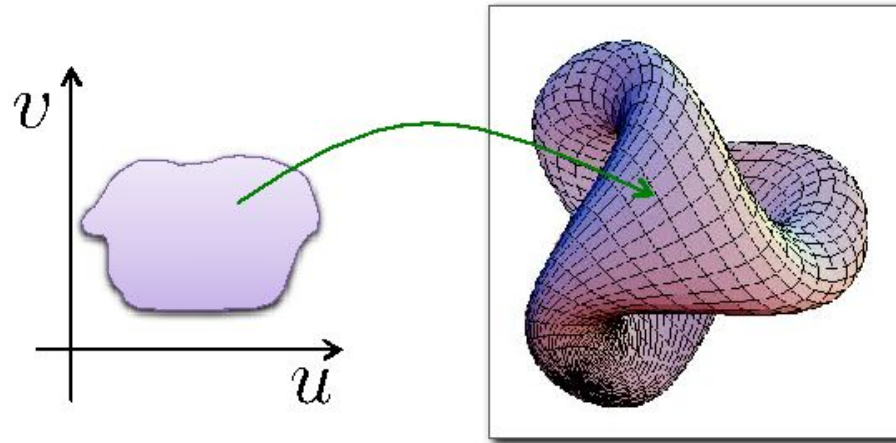
Parametric Representation

- Range of a function $f : X \rightarrow Y, X \subseteq \mathbb{R}^m, Y \subseteq \mathbb{R}^n$
- Surface in 3D: $m = 2, n = 3$



Parametric Representation

- Range of a function $f : X \rightarrow Y, X \subseteq \mathbb{R}^m, Y \subseteq \mathbb{R}^n$
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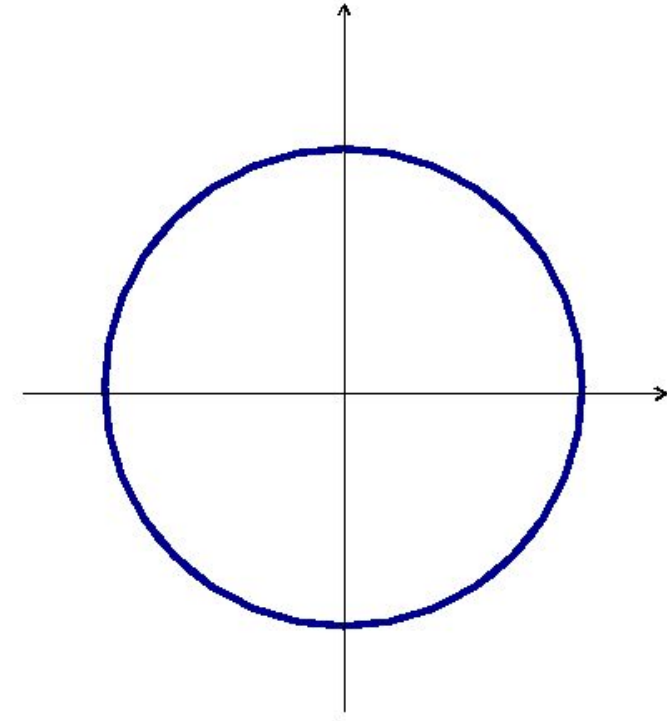
$$s(u, v) = (x(u, v), y(u, v), z(u, v))$$

Parametric Curves

- Example: Explicit curve/circle in 2D

$$\mathbf{p} : \mathbb{R} \rightarrow \mathbb{R}^2$$

$$t \mapsto \mathbf{p}(t) = (x(t), y(t))$$



Parametric Curves

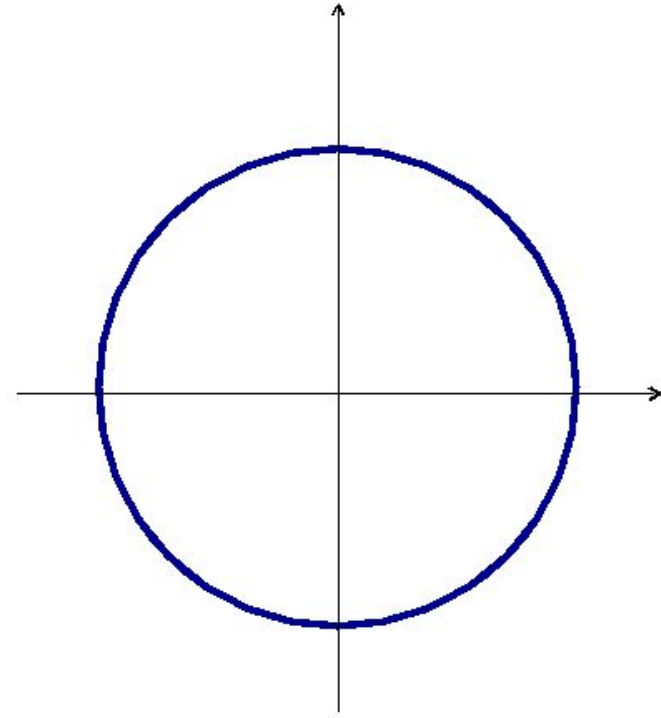
- Example: Explicit curve/circle in 2D

$$\mathbf{p} : \mathbb{R} \rightarrow \mathbb{R}^2$$

$$t \mapsto \mathbf{p}(t) = (x(t), y(t))$$

$$\mathbf{p}(t) = r (\cos(t), \sin(t))$$

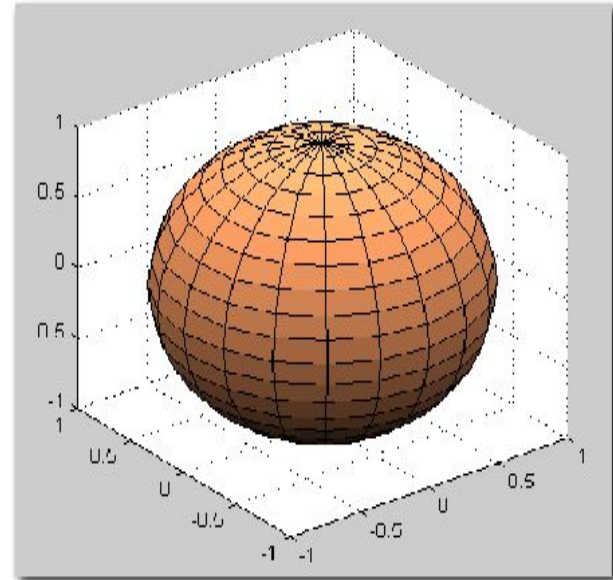
$$t \in [0, 2\pi)$$



Parametric Surfaces

- Sphere in 3D

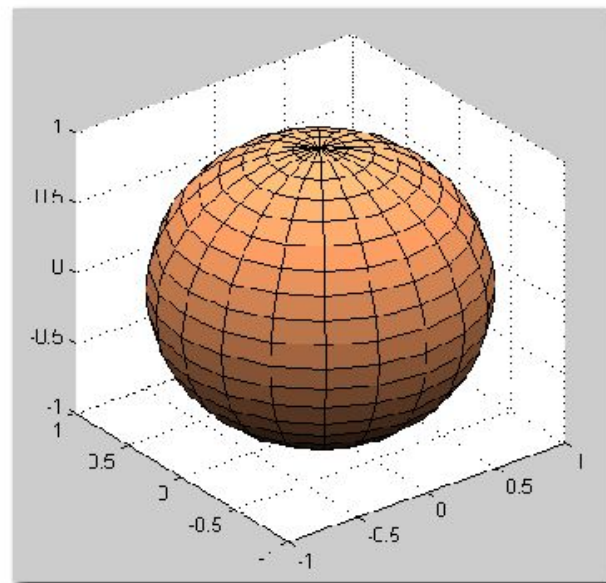
$$s : \mathbb{R}^2 \rightarrow \mathbb{R}^3$$



Parametric Surfaces

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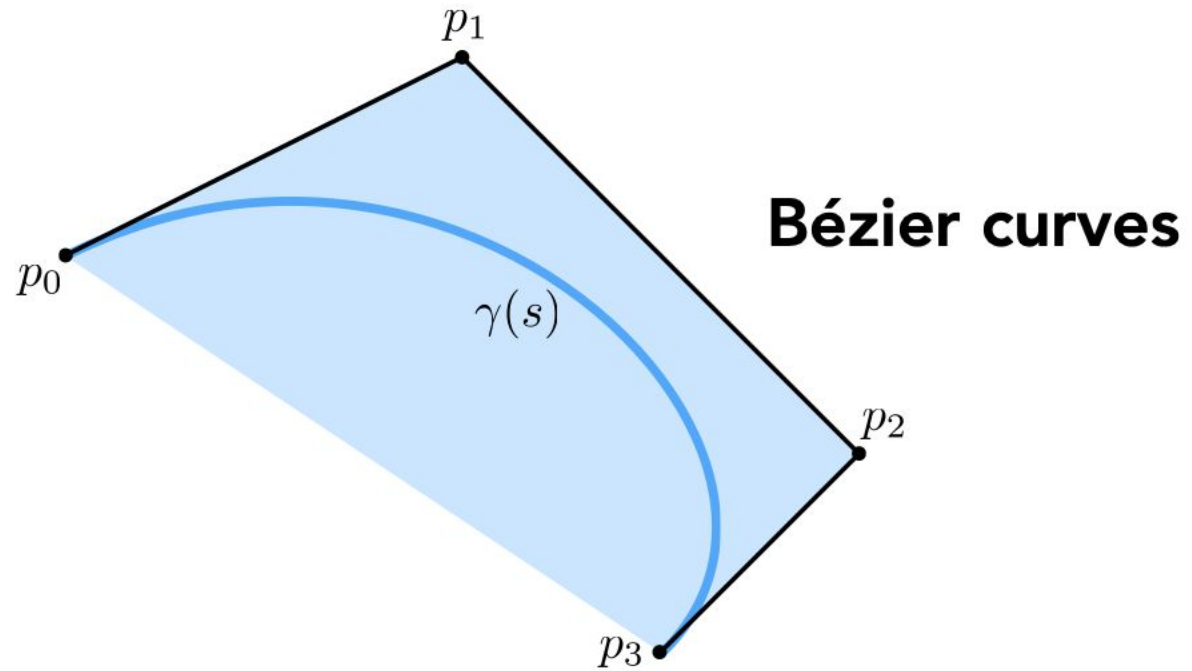
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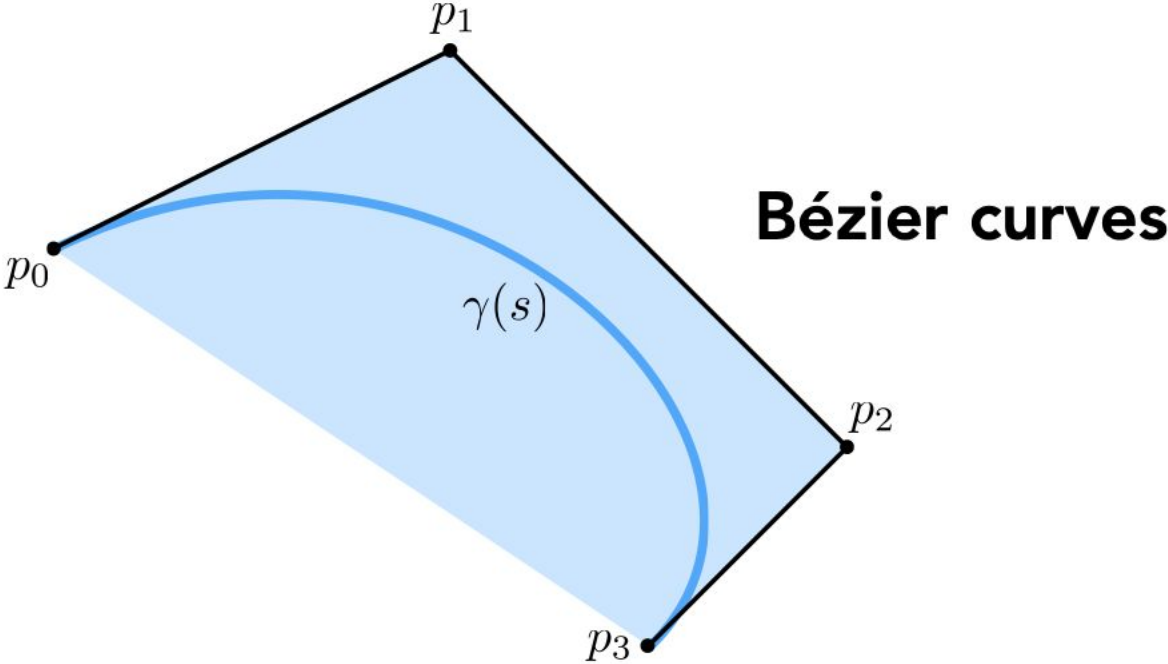
$$s(u, v) = r (\cos(u) \cos(v), \sin(u) \cos(v), \sin(v))$$

$$(u, v) \in [0, 2\pi) \times [-\pi/2, \pi/2]$$

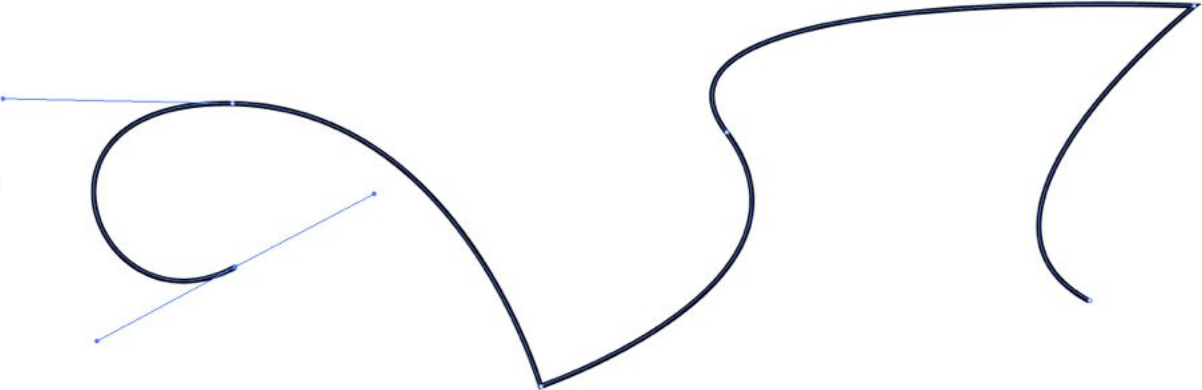
Bézier Curves



Bézier Curves

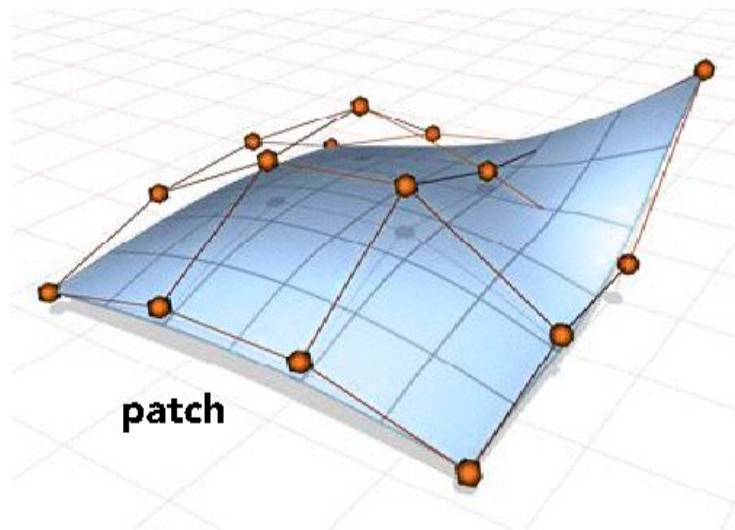


Piecewise Bézier



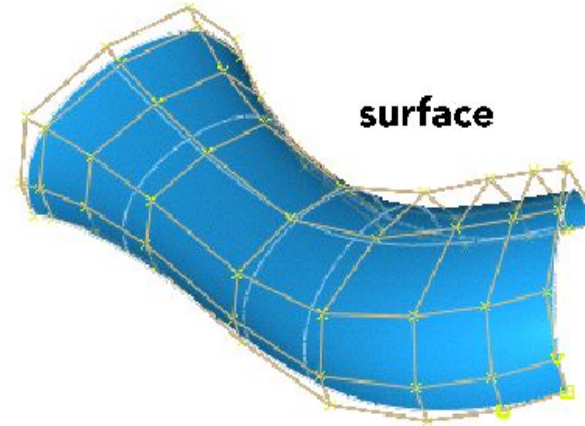
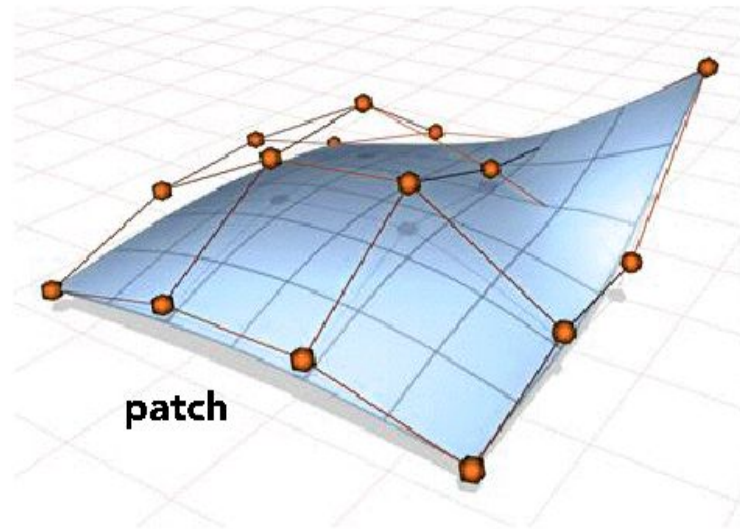
Bézier Surfaces

Use tensor product of Bézier curves to get a patch:



Bézier Surfaces

Use tensor product of Bézier curves to get a patch:



Multiple Bézier patches form a surface

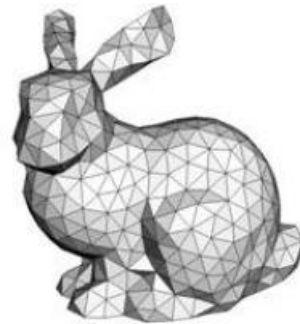
Shape Representations

Explicit

Non-parametric

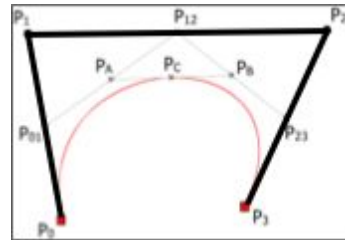


Points

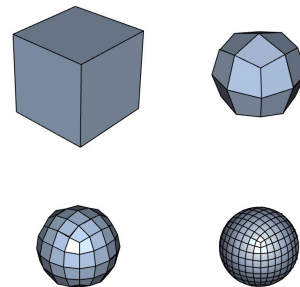


Meshes

Parametric



Splines



Subdivision
Surfaces

“Explicit” Representations of Geometry

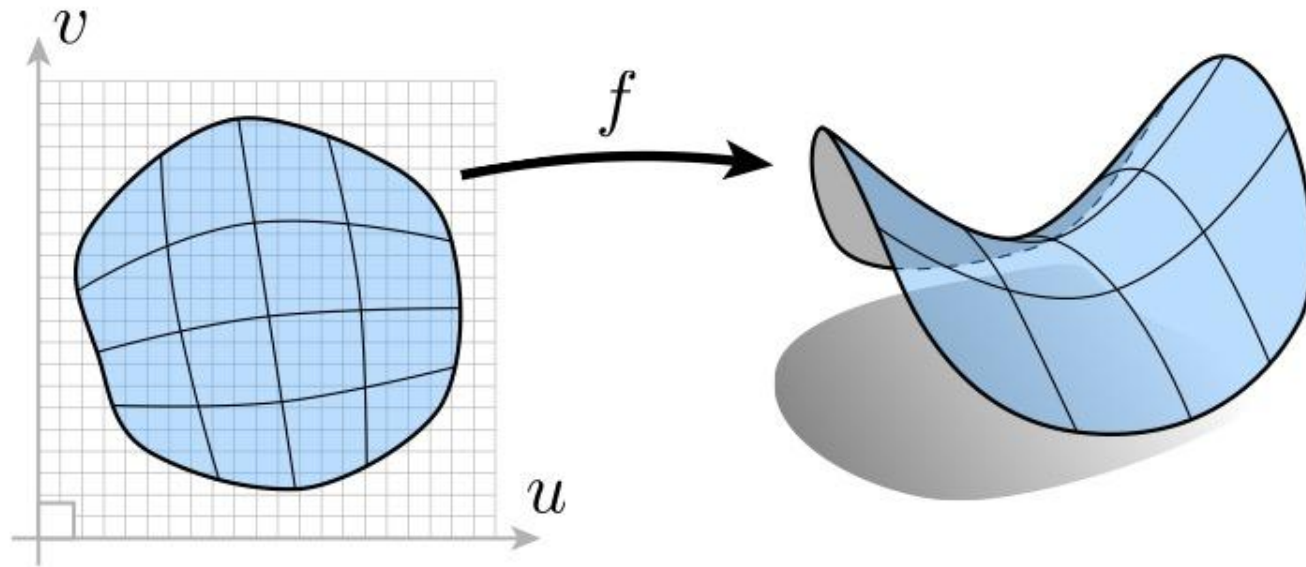
All points are given directly

"Explicit" Representations of Geometry

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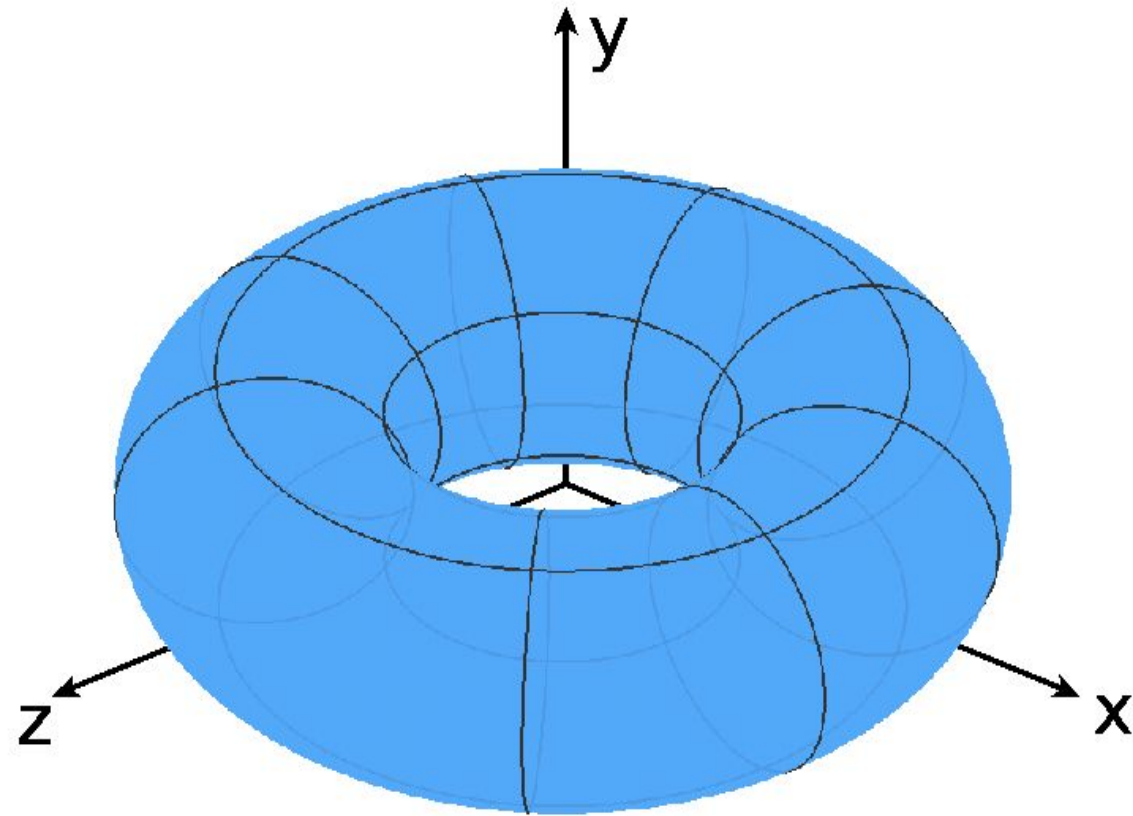
Generally:

$$f : \mathbb{R}^2 \rightarrow \mathbb{R}^3; (u, v) \mapsto (x, y, z)$$



Explicit Surface – Sampling Is Easy

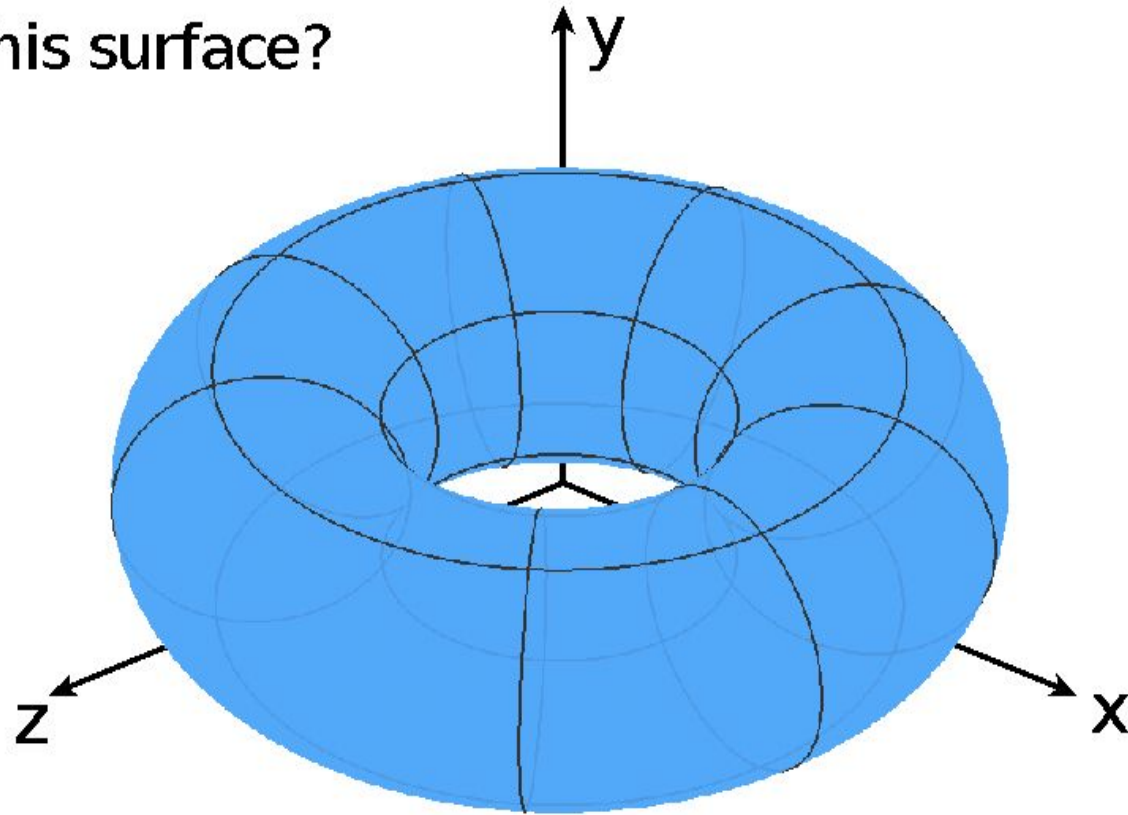
$$f(u, v) = ((2 + \cos u) \cos v, (2 + \cos u) \sin v, \sin u)$$



Explicit Surface – Sampling Is Easy

$$f(u, v) = ((2 + \cos u) \cos v, (2 + \cos u) \sin v, \sin u)$$

What points lie on this surface?

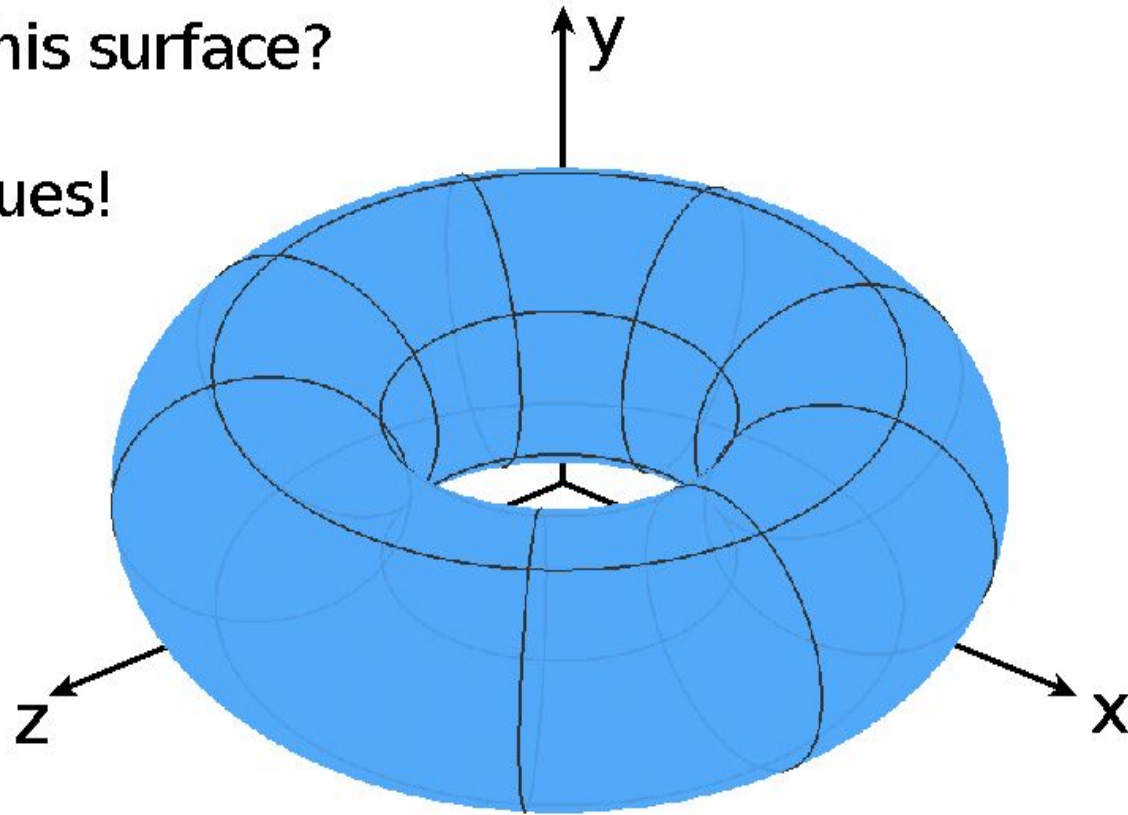


Explicit Surface – Sampling Is Easy

$$f(u, v) = ((2 + \cos u) \cos v, (2 + \cos u) \sin v, \sin u)$$

What points lie on this surface?

Just plug in (u, v) values!

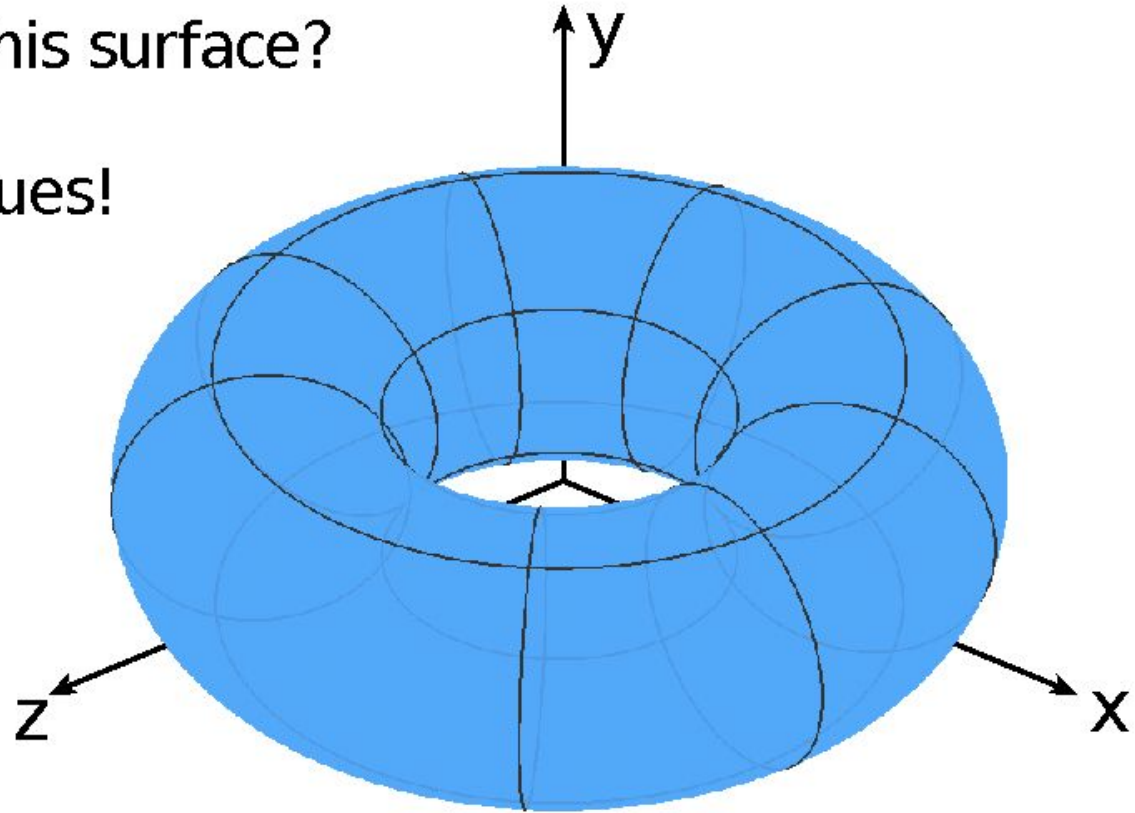


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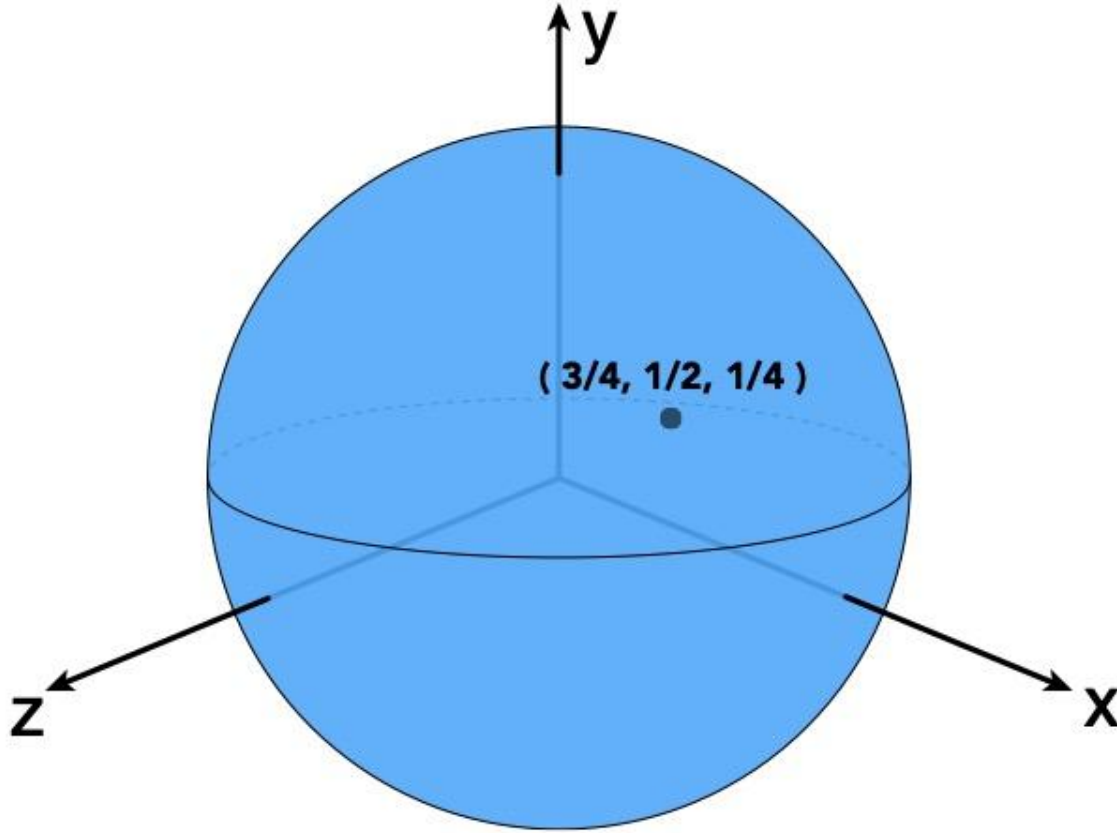
Just plug in (u, v) values!



Explicit representations make some tasks easy

Explicit Surface – Inside/Outside Test Hard

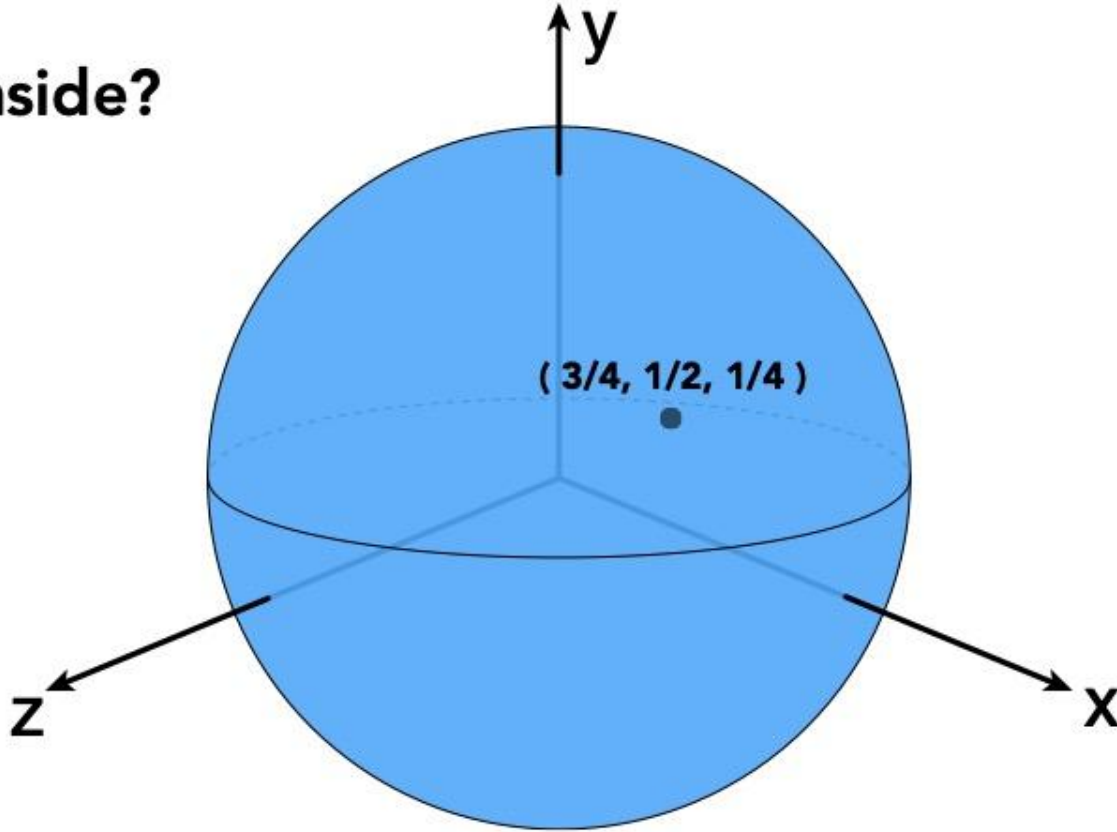
$$f(u, v) = (\cos u \sin v, \sin u \sin v, \cos v)$$



Explicit Surface – Inside/Outside Test Hard

$$f(u, v) = (\cos u \sin v, \sin u \sin v, \cos v)$$

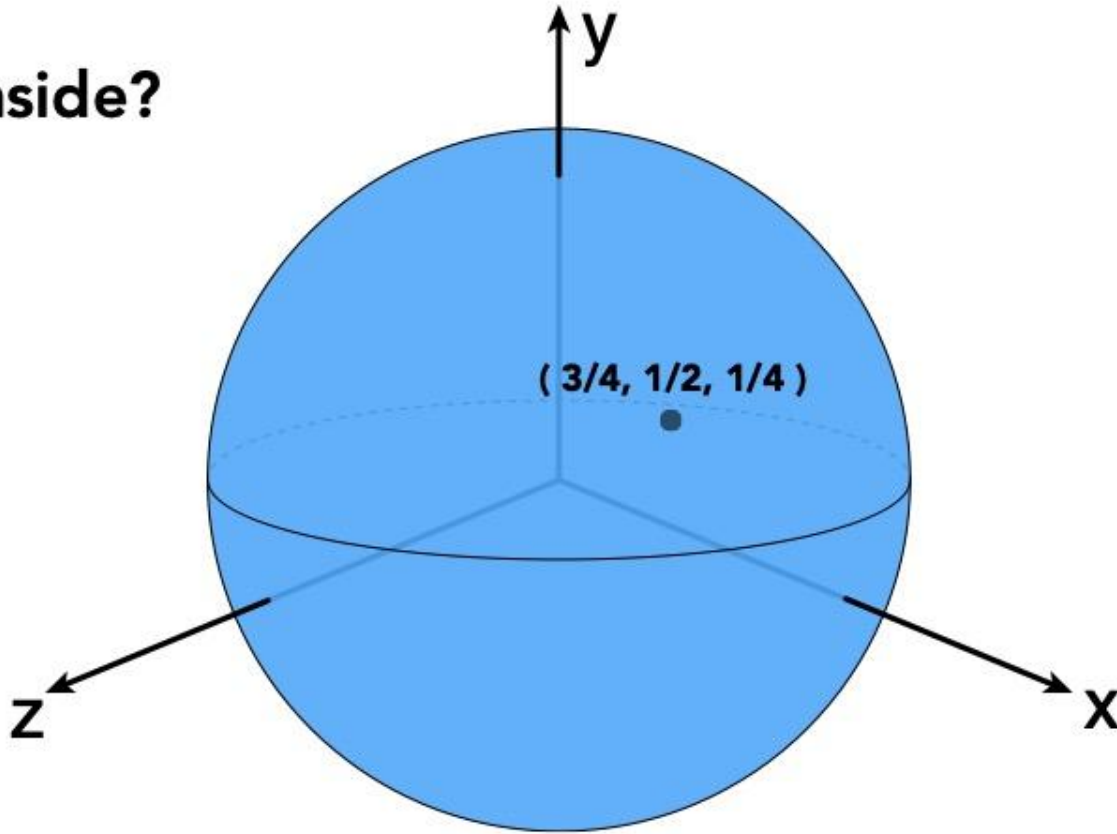
Is $(3/4, 1/2, 1/4)$ inside?



Explicit Surface – Inside/Outside Test Hard

$$f(u, v) = (\cos u \sin v, \sin u \sin v, \cos v)$$

Is $(3/4, 1/2, 1/4)$ inside?



Some tasks are hard with explicit representations

“Implicit” Representations of Geometry

Based on classifying points

- Points satisfy some specified relationship

"Implicit" Representations of Geometry

Based on classifying points

- Points satisfy some specified relationship

E.g. sphere: all points in 3D, where $x^2+y^2+z^2 = 1$

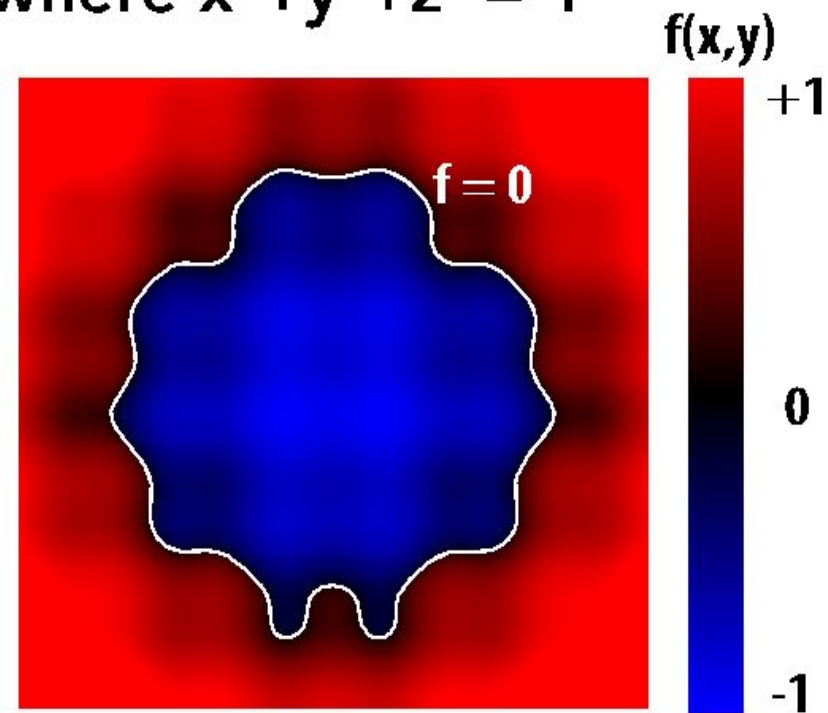
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Based on classifying points

- Points satisfy some specified relationship

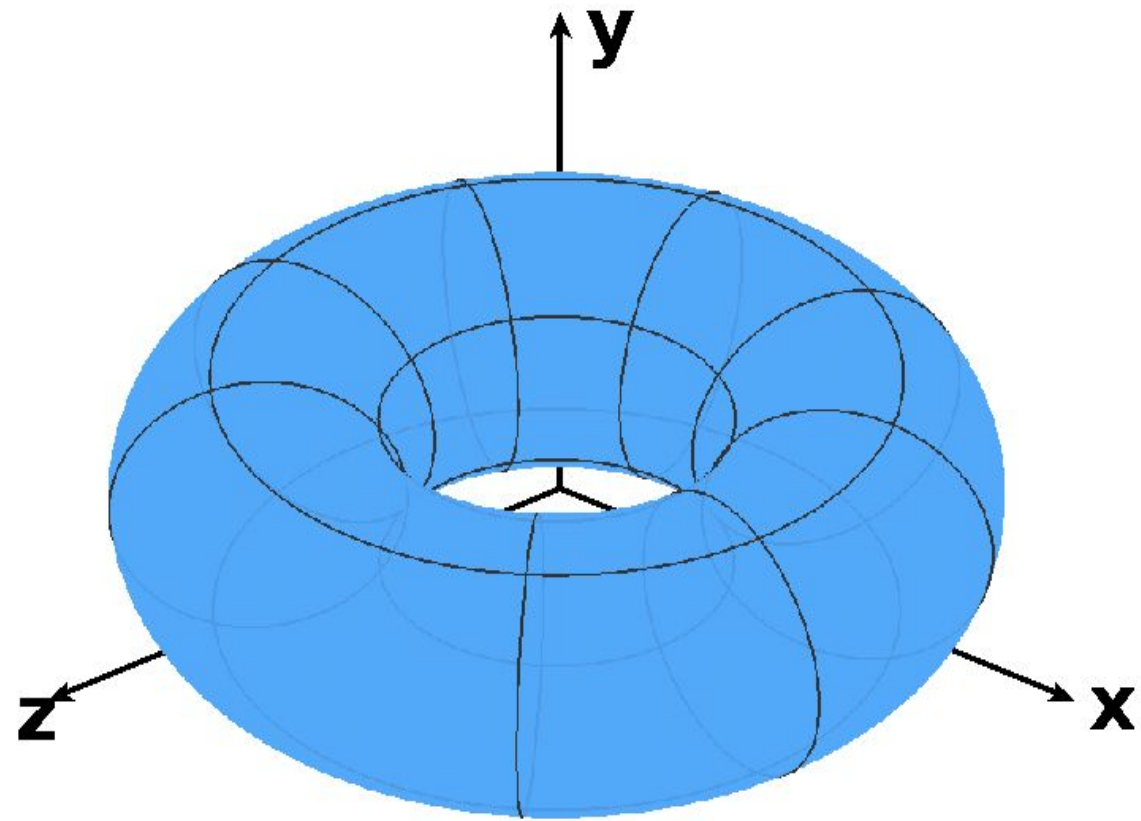
E.g. sphere: all points in 3D, where $x^2+y^2+z^2 = 1$

More generally, $f(x,y,z) = 0$



Implicit Surface - Sampling Can Be Hard

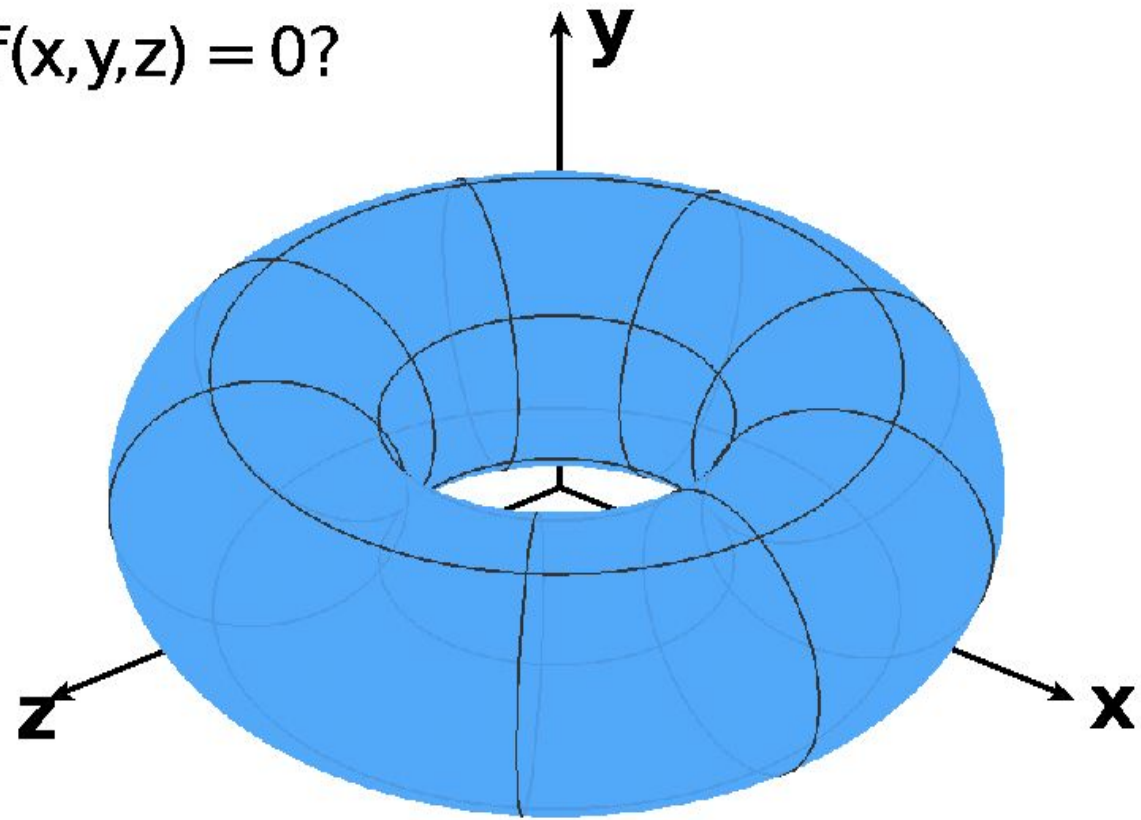
$$f(x, y, z) = (2 - \sqrt{x^2 + y^2})^2 + z^2 - 1$$



Implicit Surface - Sampling Can Be Hard

$$f(x, y, z) = (2 - \sqrt{x^2 + y^2})^2 + z^2 - 1$$

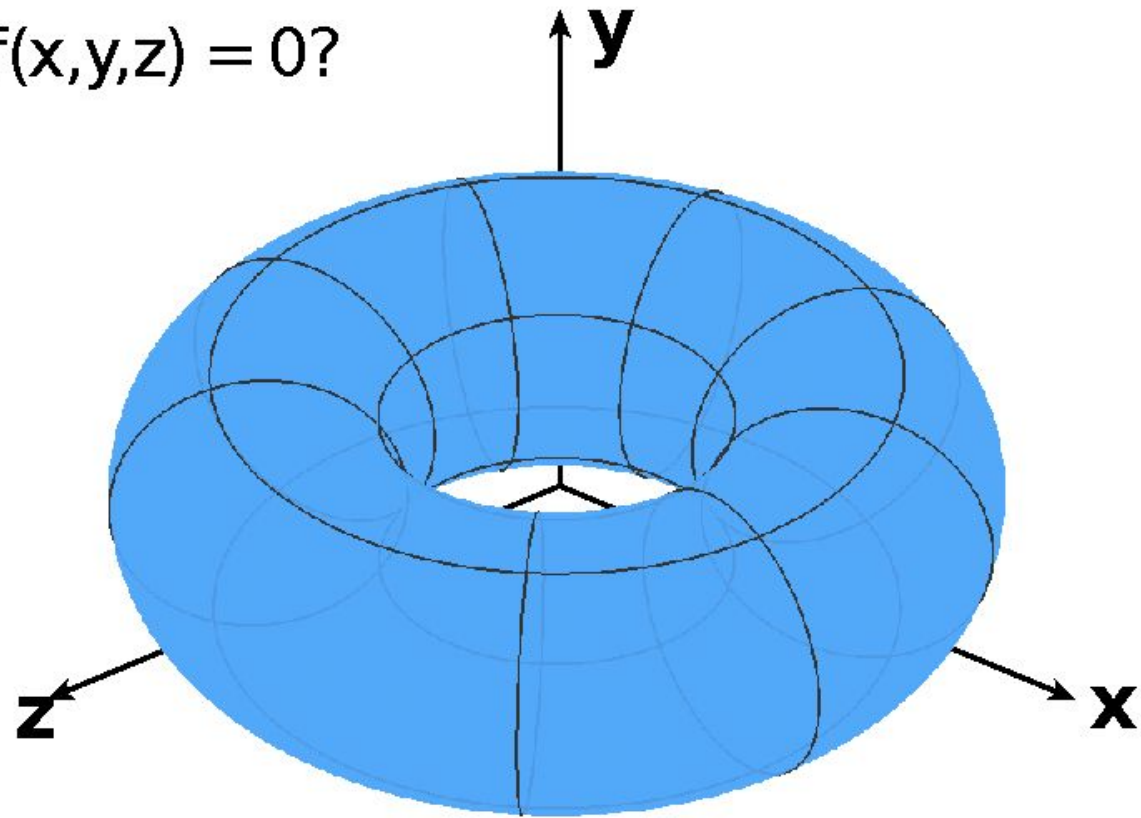
What points lie on $f(x, y, z) = 0$?



Implicit Surface – Sampling Can Be Hard

$$f(x, y, z) = (2 - \sqrt{x^2 + y^2})^2 + z^2 - 1$$

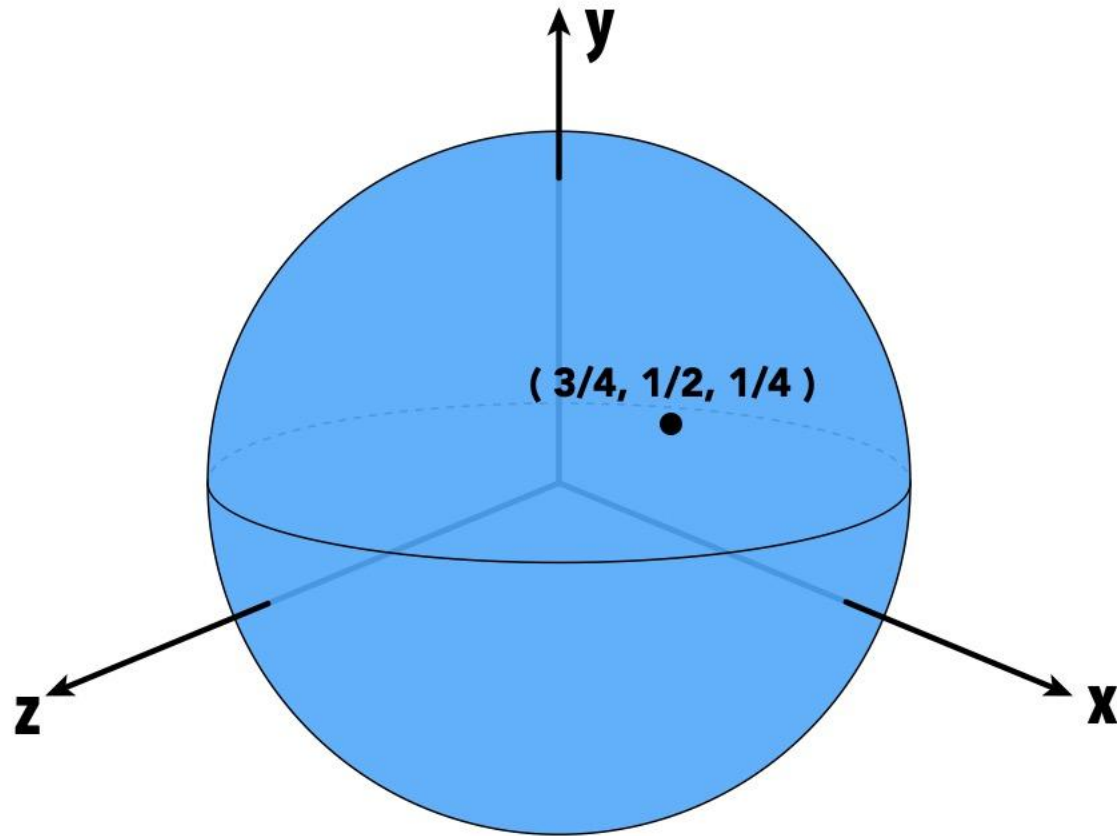
What points lie on $f(x, y, z) = 0$?



Some tasks are hard with implicit representations

Implicit Surface – Inside/Outside Tests Easy

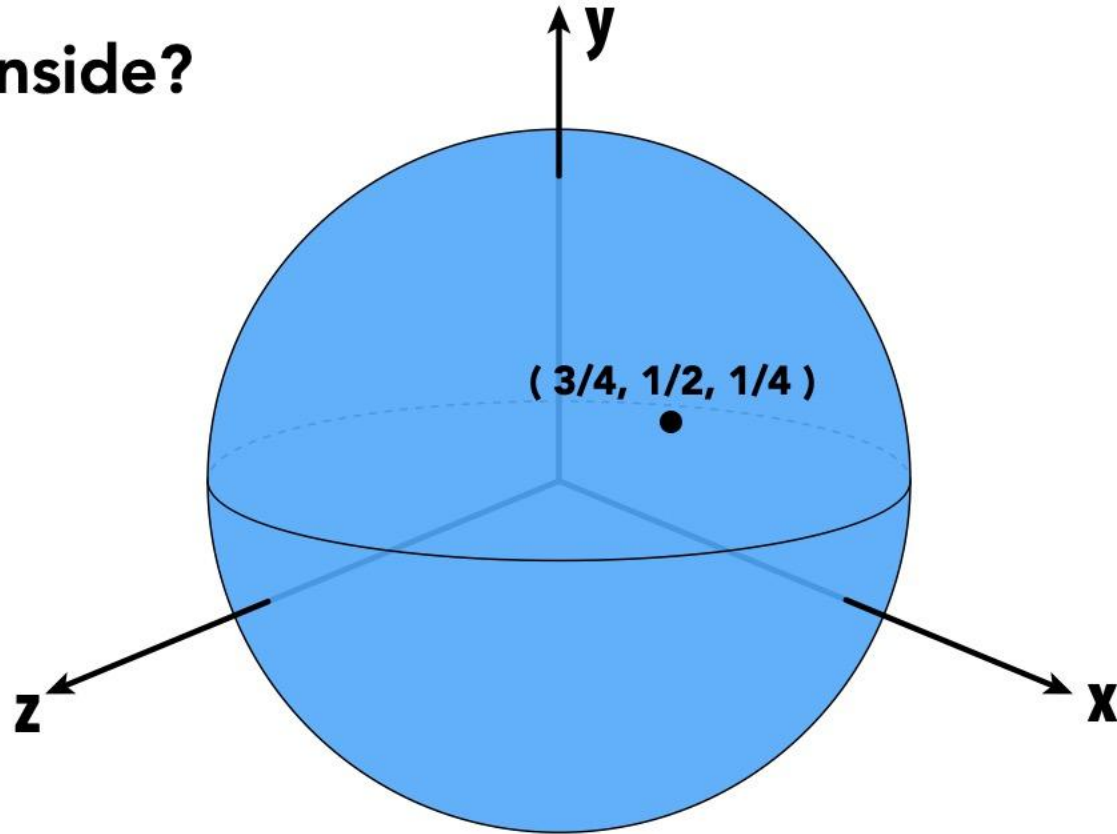
$$f(x, y, z) = x^2 + y^2 + z^2 - 1$$



Implicit Surface – Inside/Outside Tests Easy

$$f(x, y, z) = x^2 + y^2 + z^2 - 1$$

Is $(3/4, 1/2, 1/4)$ inside?



Implicit Surface – Inside/Outside Tests Easy

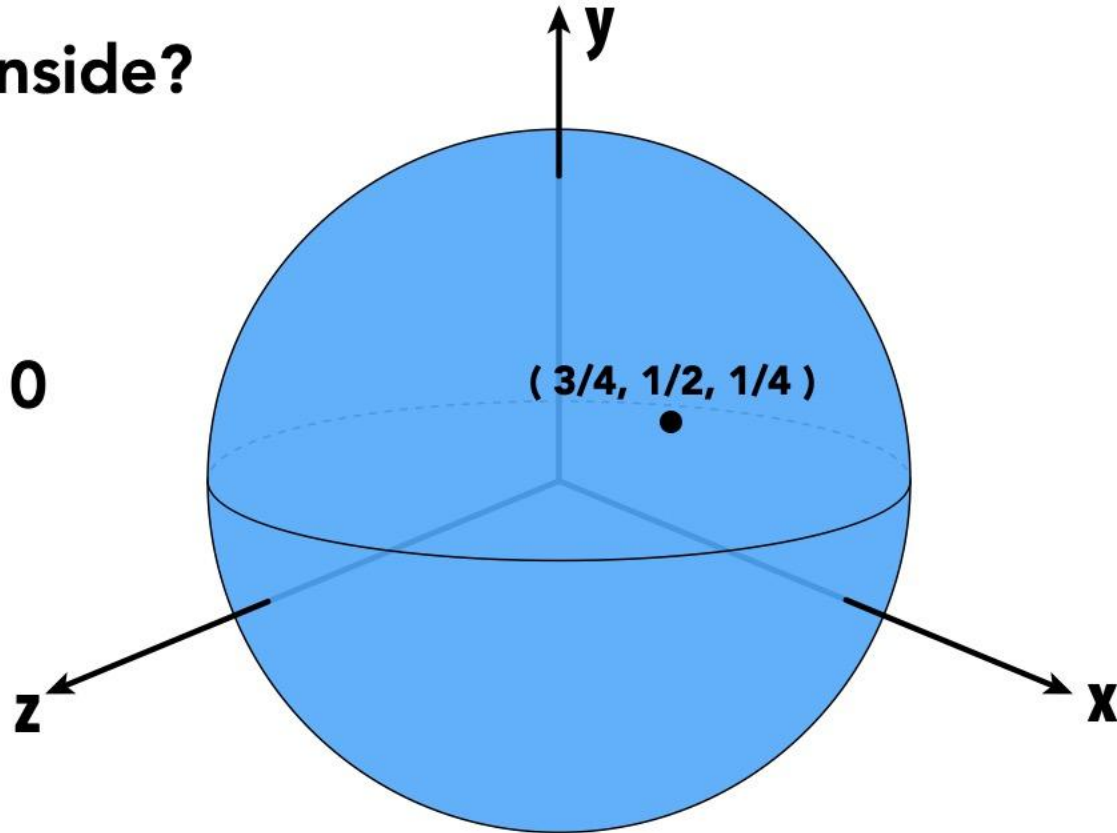
$$f(x, y, z) = x^2 + y^2 + z^2 - 1$$

Is $(3/4, 1/2, 1/4)$ inside?

Just plug it in:

$$f(x, y, z) = -1/8 < 0$$

Yes, inside.



Implicit Surface – Inside/Outside Tests Easy

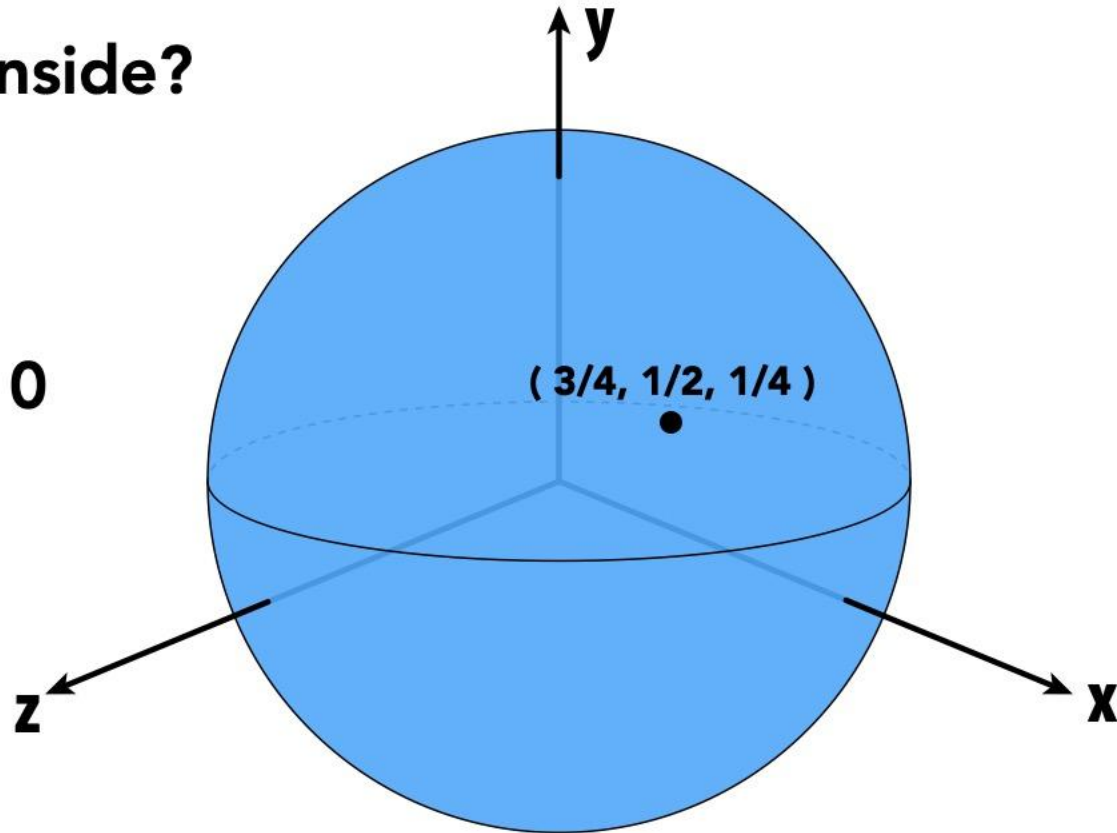
$$f(x, y, z) = x^2 + y^2 + z^2 - 1$$

Is $(3/4, 1/2, 1/4)$ inside?

Just plug it in:

$$f(x, y, z) = -1/8 < 0$$

Yes, inside.



Implicit representations make some tasks easy

Algebraic Surfaces (Implicit)

Surface is zero set of a polynomial in x, y, z



$$x^2 + y^2 + z^2 = 1$$

Algebraic Surfaces (Implicit)

Surface is zero set of a polynomial in x, y, z



$$x^2 + y^2 + z^2 = 1$$



$$(R - \sqrt{x^2 + y^2})^2 + z^2 = r^2$$



$$\left(x^2 + \frac{9y^2}{4} + z^2 - 1\right)^3 = x^2 z^3 + \frac{9y^2 z^3}{80}$$

Algebraic Surfaces (Implicit)

Surface is zero set of a polynomial in x, y, z



$$x^2 + y^2 + z^2 = 1$$



$$(R - \sqrt{x^2 + y^2})^2 + z^2 = r^2$$



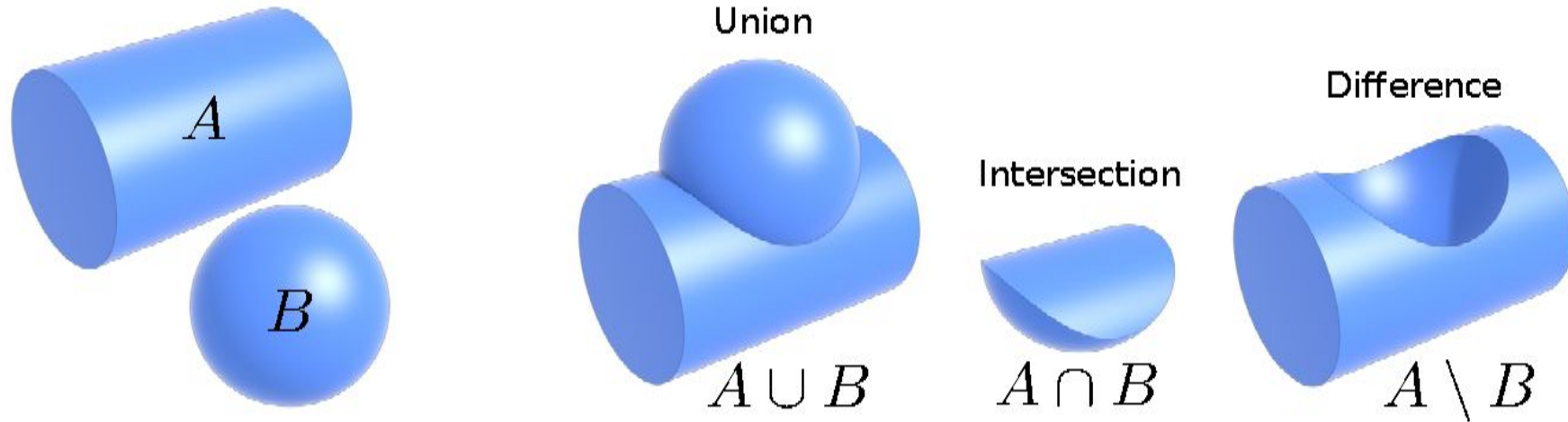
$$(x^2 + \frac{9y^2}{4} + z^2 - 1)^3 = x^2 z^3 + \frac{9y^2 z^3}{80}$$



More complex shapes?

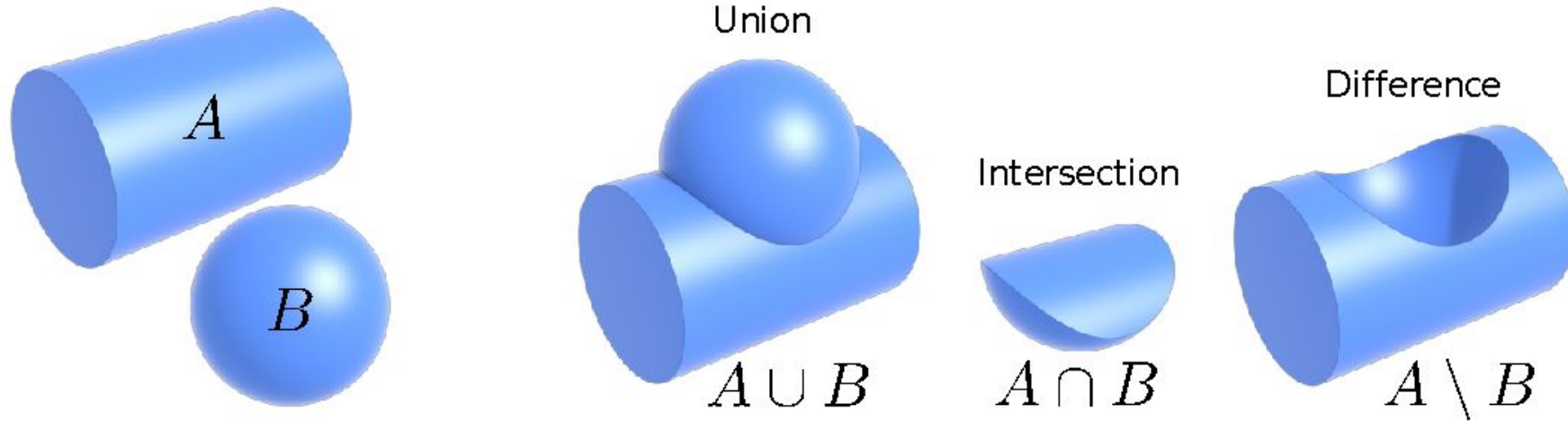
Constructive Solid Geometry (Implicit)

Combine implicit geometry via Boolean operations

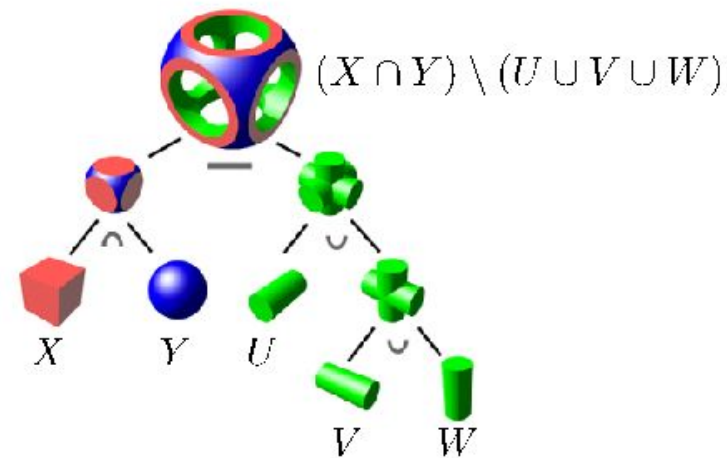


Constructive Solid Geometry (Implicit)

Combine implicit geometry via Boolean operations



Boolean expressions:

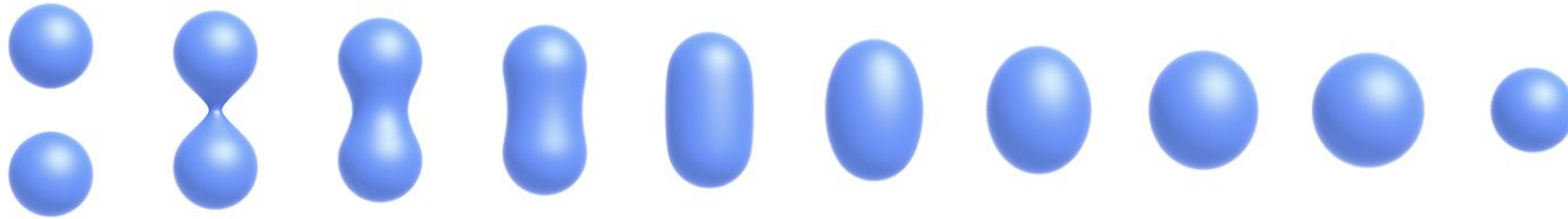


Distance Functions (Implicit)

Instead of Booleans, gradually blend surfaces together using

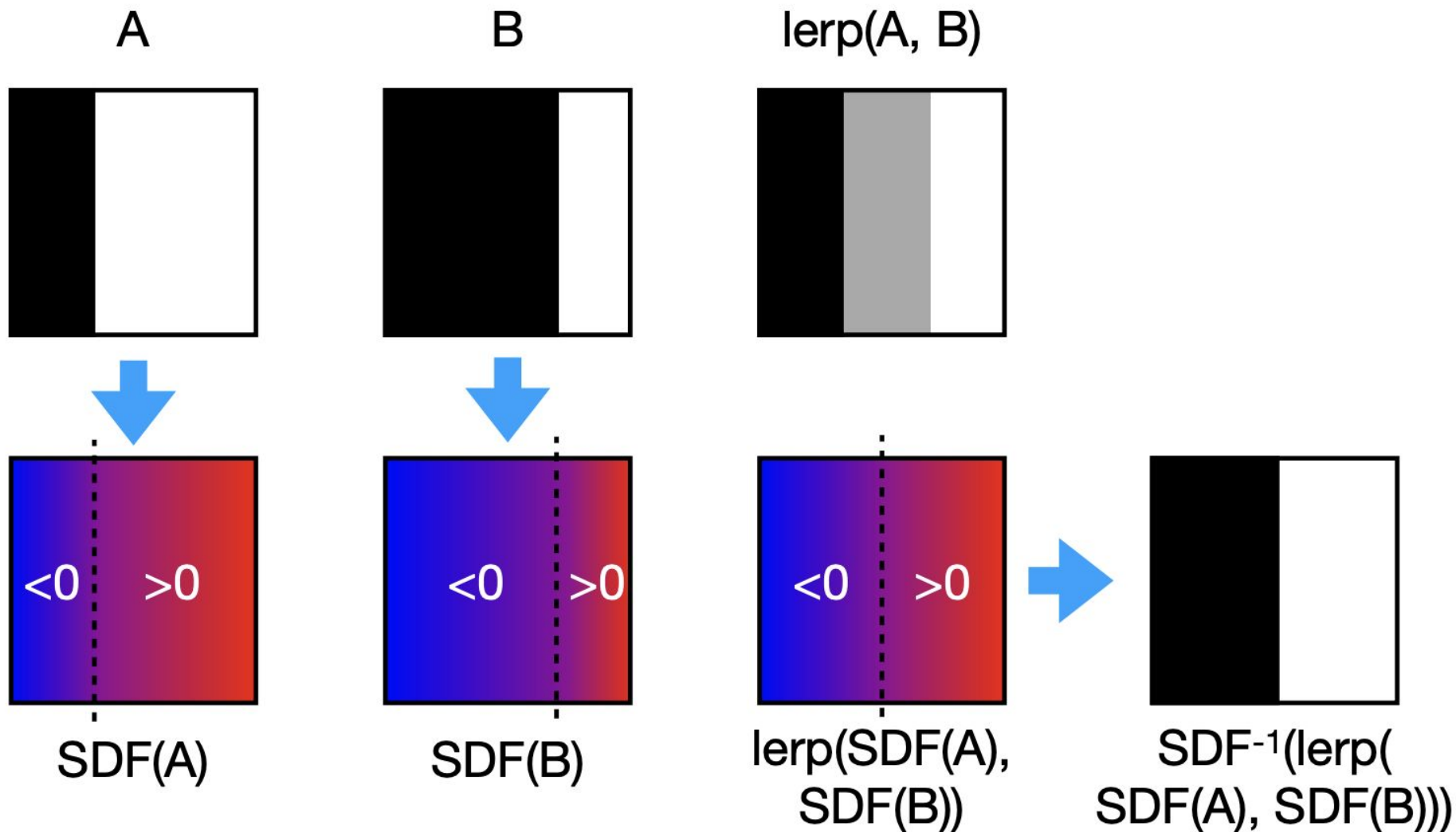
Distance functions:

giving minimum distance (could be **signed** distance)
from anywhere to object



Distance Functions (Implicit)

An Example: Blending (linear interp.) a moving boundary



Scene of Pure Distance Functions (Not Easy!)



See <http://iquilezles.org/www/material/nvscene2008/nvscene2008.htm>

Shape Representations

Explicit

Implicit

Non-parametric

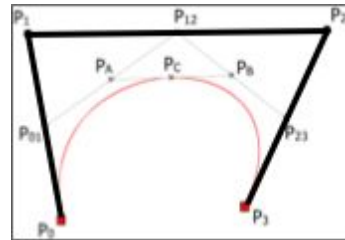


Points

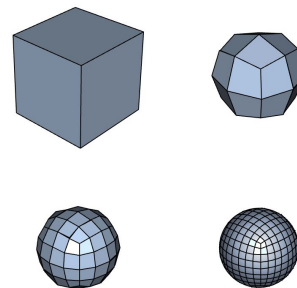


Meshes

Parametric



Splines

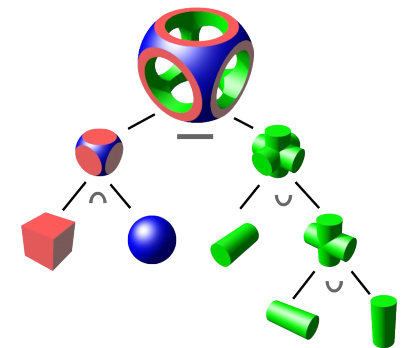


Subdivision Surfaces



$$x^2 + y^2 + z^2 = 1$$

Algebraic Surfaces



Constructive Solid Geometry

Level Set Methods (Implicit)

Implicit surfaces have some nice features (e.g., merging/splitting)

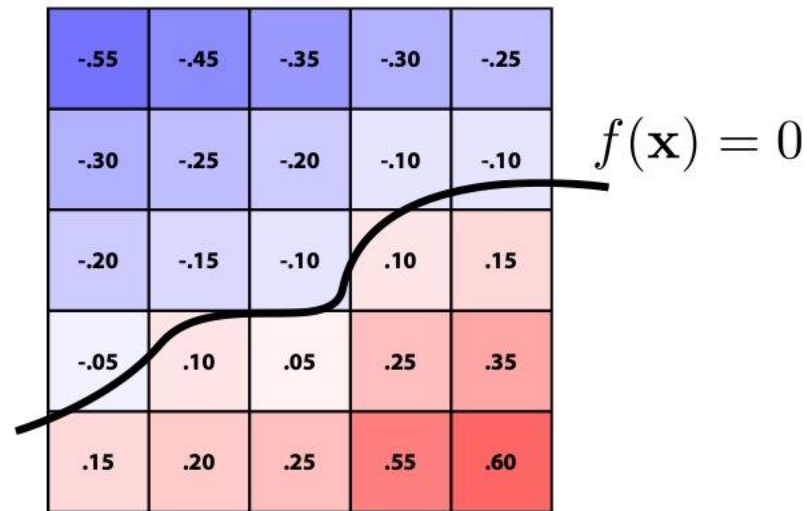
But, hard to describe complex shapes in closed form

Level Set Methods (Implicit)

Implicit surfaces have some nice features (e.g., merging/splitting)

But, hard to describe complex shapes in closed form

Alternative: store a grid of values approximating function

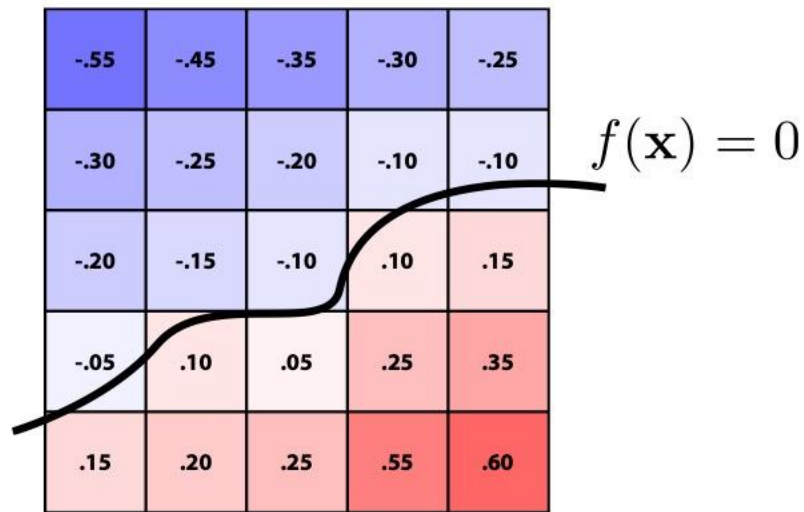


Level Set Methods (Implicit)

Implicit surfaces have some nice features (e.g., merging/splitting)

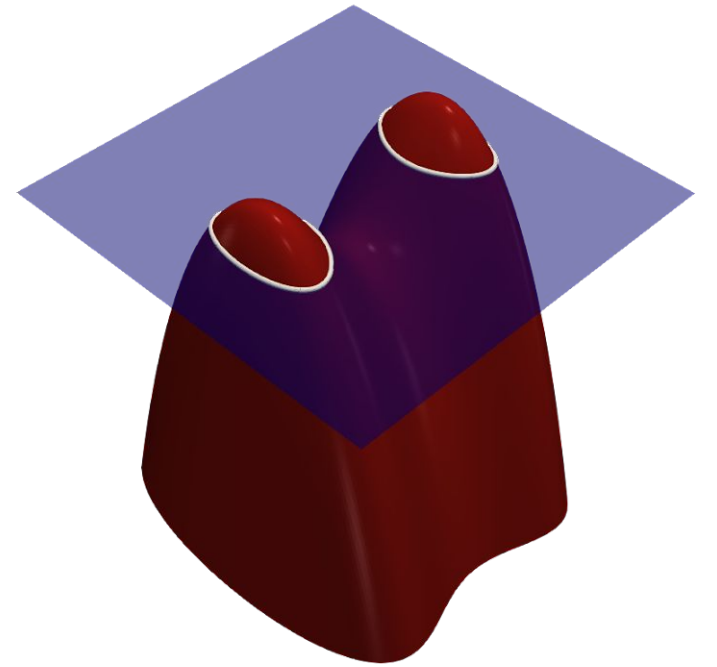
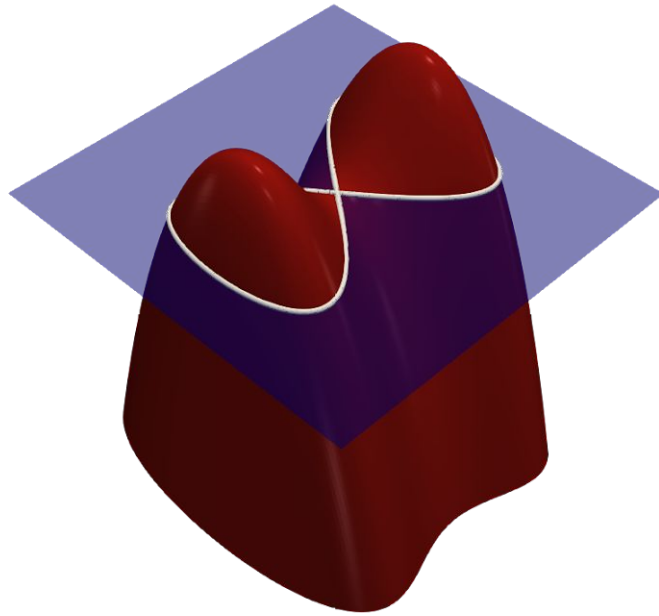
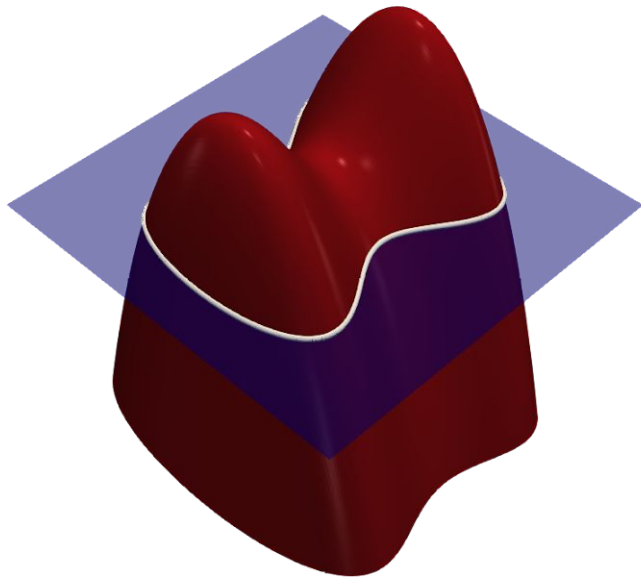
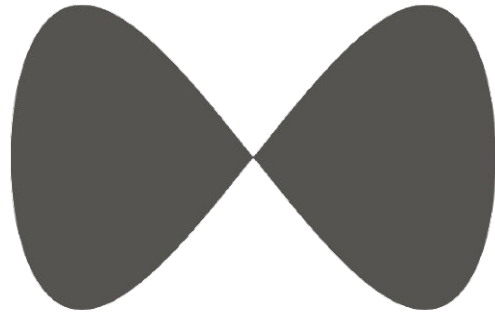
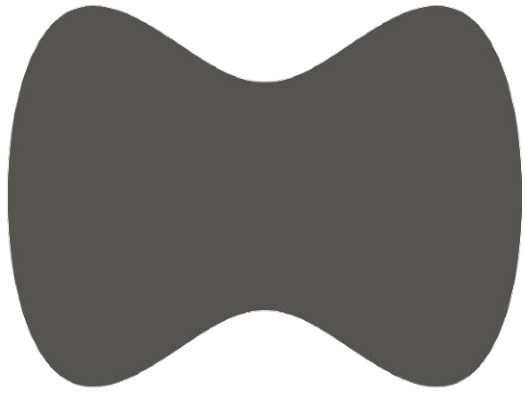
But, hard to describe complex shapes in closed form

Alternative: store a grid of values approximating function



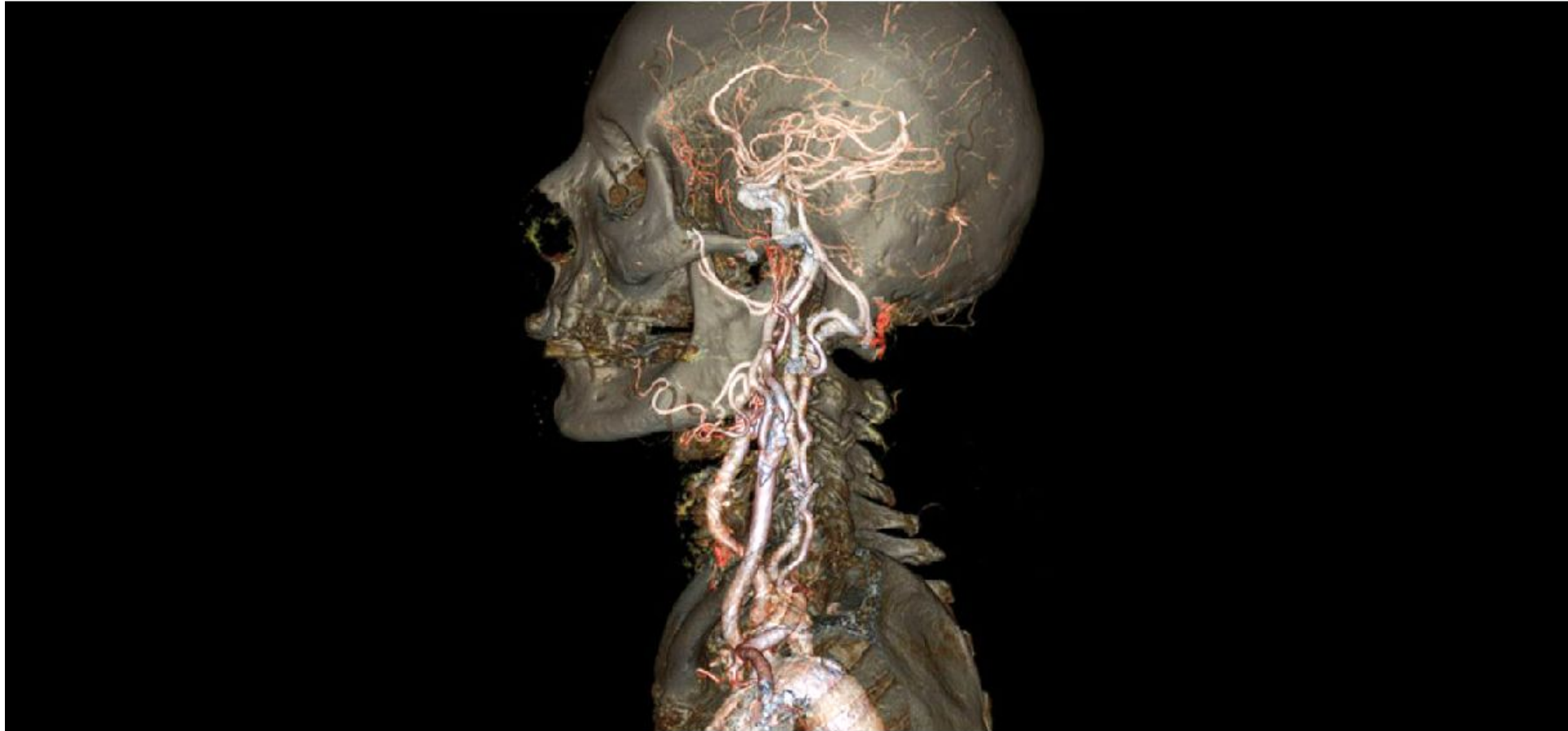
Surface is found where interpolated values equal zero

Provides much more explicit control over shape (like a texture)



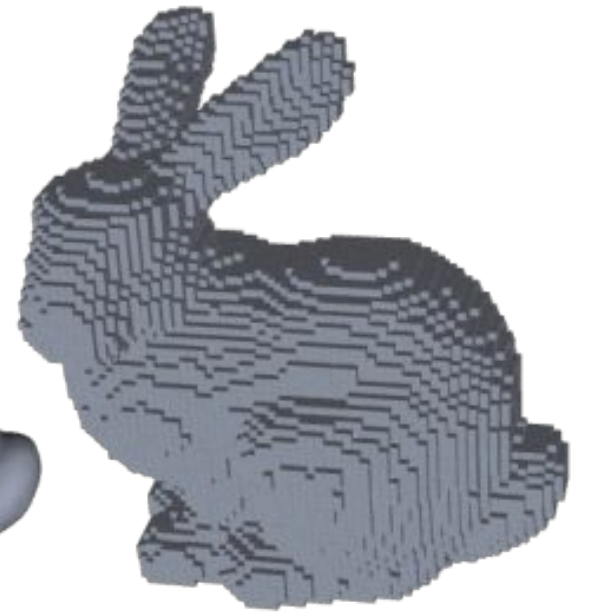
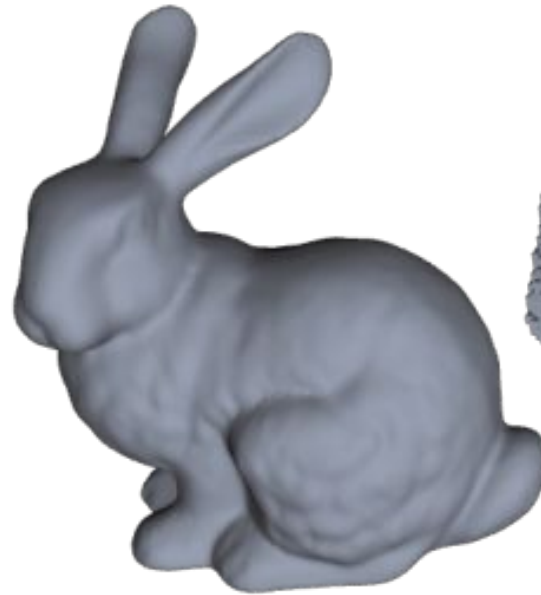
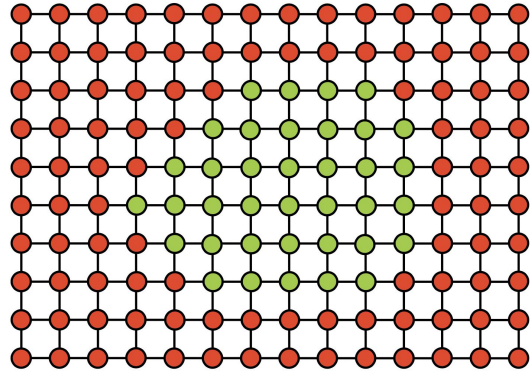
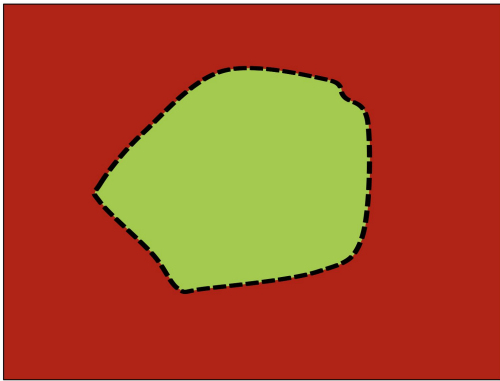
Level Sets from Medical Data (CT, MRI, etc.)

Level sets encode, e.g., constant tissue density



Related Representation: Voxels

- Binary thresholding the volumetric grid



Shape Representations

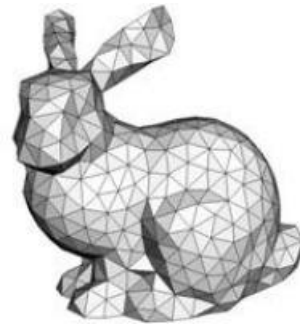
Explicit

Implicit (Eulerian)

Non-parametric



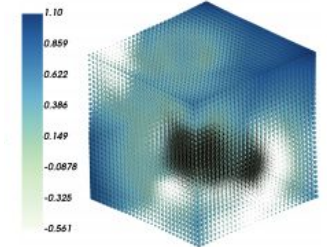
Points



Meshes

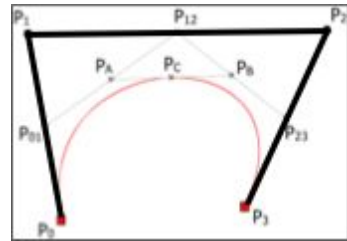


Voxels

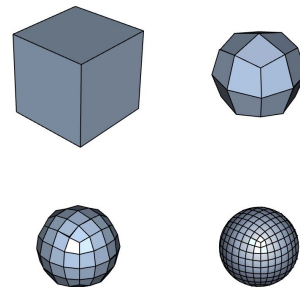


Level Sets

Parametric



Splines

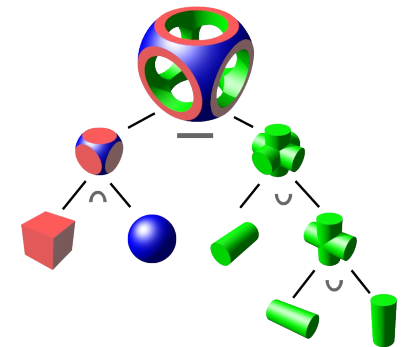


Subdivision Surfaces



$$x^2 + y^2 + z^2 = 1$$

Algebraic Surfaces



Constructive Solid Geometry

AI + Shapes

- In 3D ...

Princeton Shape Benchmark

- 1814 Models
- 182 Categories



Datasets Prior to 2014

Benchmarks	Types	# models	# classes	Avg # models per class
SHREC14LSGTB	Generic	8,987	171	53
PSB	Generic	907+907 (train+test)	90+92 (train+test)	10+10 (train+test)
SHREC12GTB	Generic	1200	60	20
TSB	Generic	10,000	352	28
CCCC	Generic	473	55	9
WMB	Watertight (articulated)	400	20	20
MSB	Articulated	457	19	24
BAB	Architecture	2257	183+180 (function+form)	12+13 (function+form)
ESB	CAD	867	45	19

Table 1. Source datasets from SHREC 2014: *Princeton Shape Benchmark (PSB)* [27], *SHREC 2012 generic Shape Benchmark (SHREC12GTB)* [16], *Toyohashi Shape Benchmark (TSB)* [29], *Konstanz 3D Model Benchmark (CCCC)* [32], *Watertight Model Benchmark (WMB)* [31], *McGill 3D Shape Benchmark (MSB)* [37], *Bonn Architecture Benchmark (BAB)* [33], *Purdue Engineering Shape Benchmark (ESB)* [9].

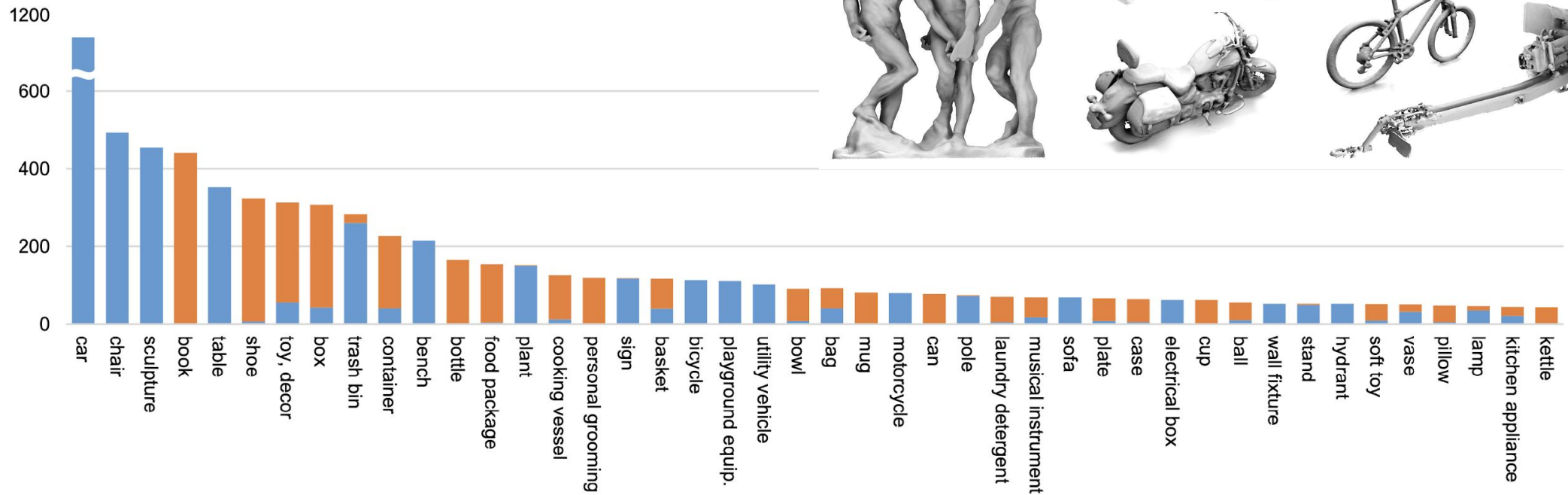
Datasets for 3D Objects

- Large-scale Synthetic Objects: ShapeNet, 3M models
- ModelNet: absorbed by ShapeNet
- ShapeNetCore: 51.3K models in 55 categories



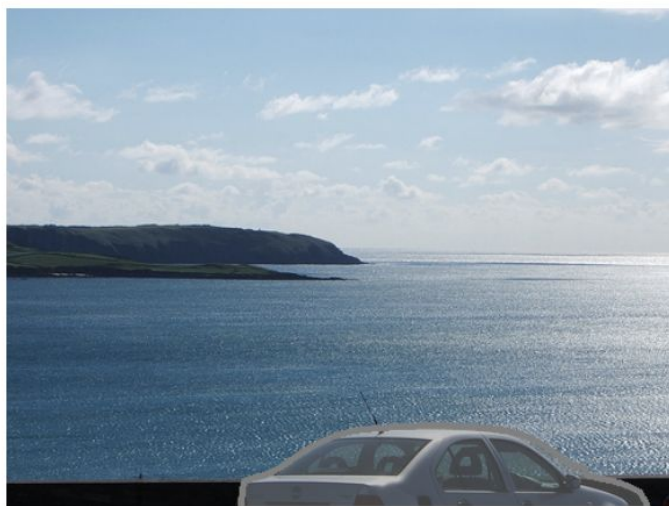
Object Scan

- 10,933 RGBD scans
- 441 models



Pascal 3D+

- Retrieve a nearest-neighbor 3D model for objects in real images
- 8,505 PASCAL images (13,898 instances) + 22,394 ImageNet images
- 12 rigid categories, 3,000+ instances per category on average



Pix3D

- 10,069 images
- 395 shapes (IKEA furniture + 3D scan)



Link to WordNet Taxonomy Alignment+Symmetry Part Hierarchy Part Correspondences

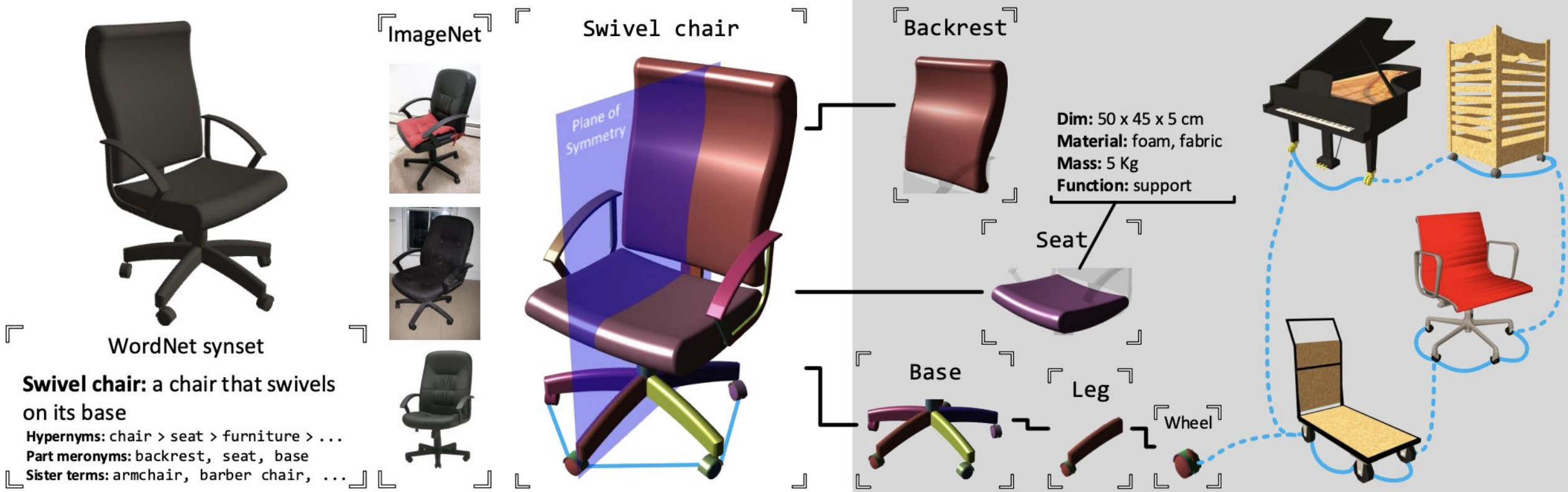
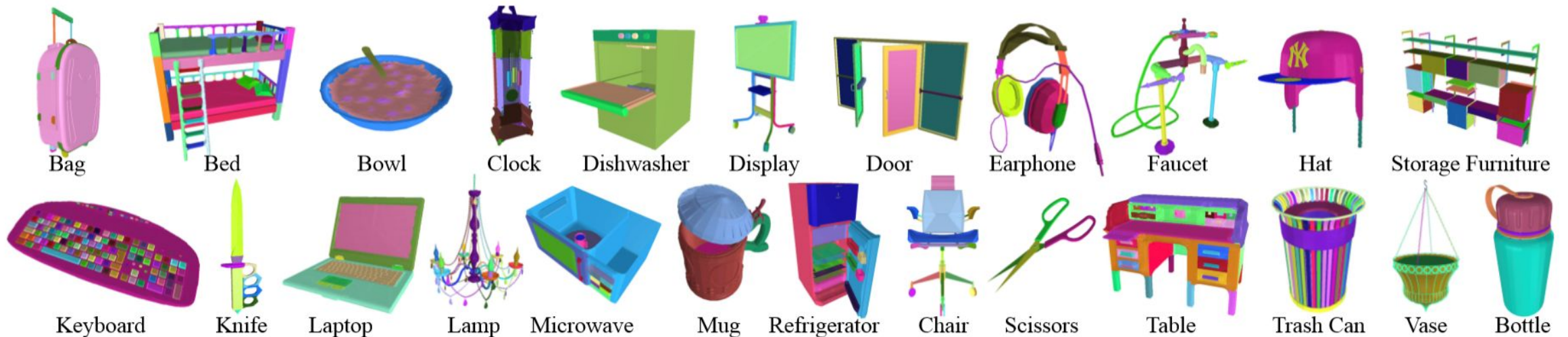


Figure from the ShapeNet paper, Chang et al. arXiv 2015

Datasets for 3D Object Parts

Fine-grained Parts: PartNet

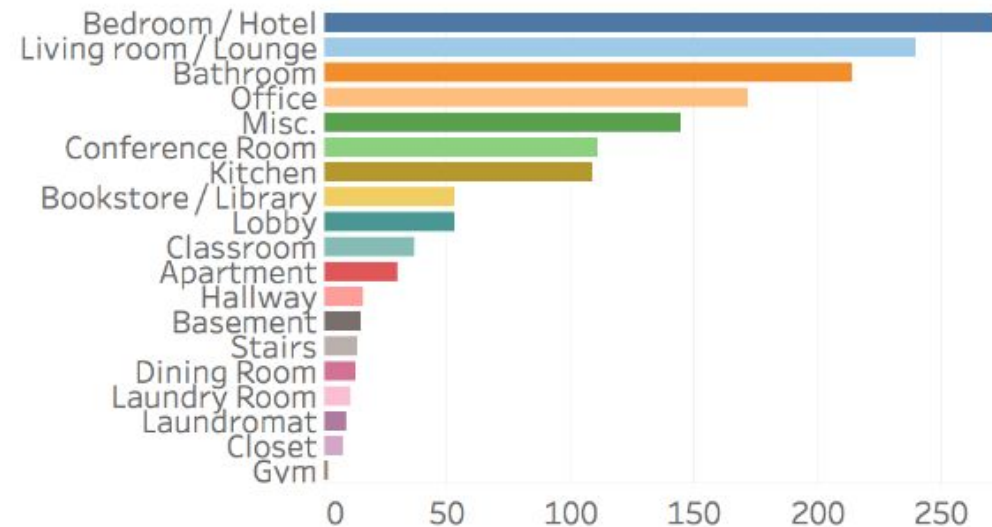
- Fine-grained (+mobility)
- Instance-level
- Hierarchical



Datasets for Indoor 3D Scenes

Large-scale Scanned Real Scenes: ScanNet

- 2.5M Views in 1,500 RGBD scans
- 3D camera poses
- Surface reconstructions
- Instance-level semantic segmentations



Physical Interaction with Articulated Objects

**300+ door
annotations**

**support
articulated
objects**

(cabinets, doors, fridge,
oven, window etc.)



AI + Geometry

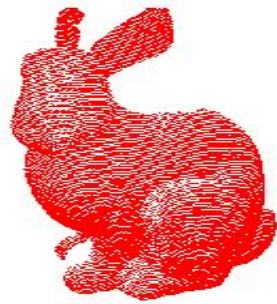
- $P(S)$ or $P(S|c)$ --- Generative models
 - Learning (conditional) shape priors
 - Shape generation, completion, & geometry data processing
- $P(c|S)$ --- Discriminative models
 - Learning shape descriptors
 - Shape classification, segmentation, view estimation, etc.
- Joint modeling of 3D and 2D data
 - Large-scale 2D datasets & very good pretrained models
 - Differentiable projection/back-projection & differentiable/neural rendering

Which Shape Representation?

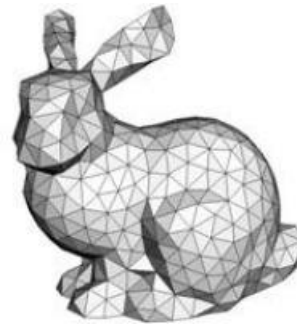
Explicit

Implicit (Eulerian)

Non-parametric



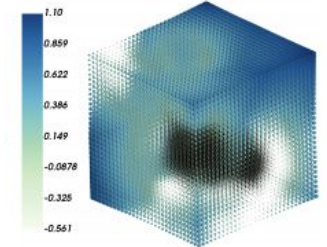
Points



Meshes

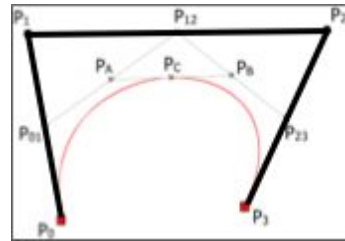


Voxels

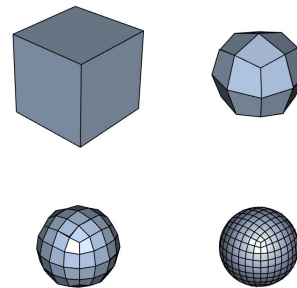


Level Sets

Parametric



Splines

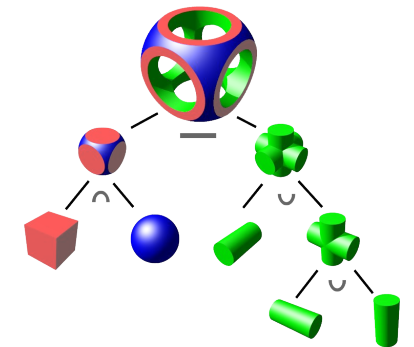


Subdivision Surfaces



$$x^2 + y^2 + z^2 = 1$$

Algebraic Surfaces

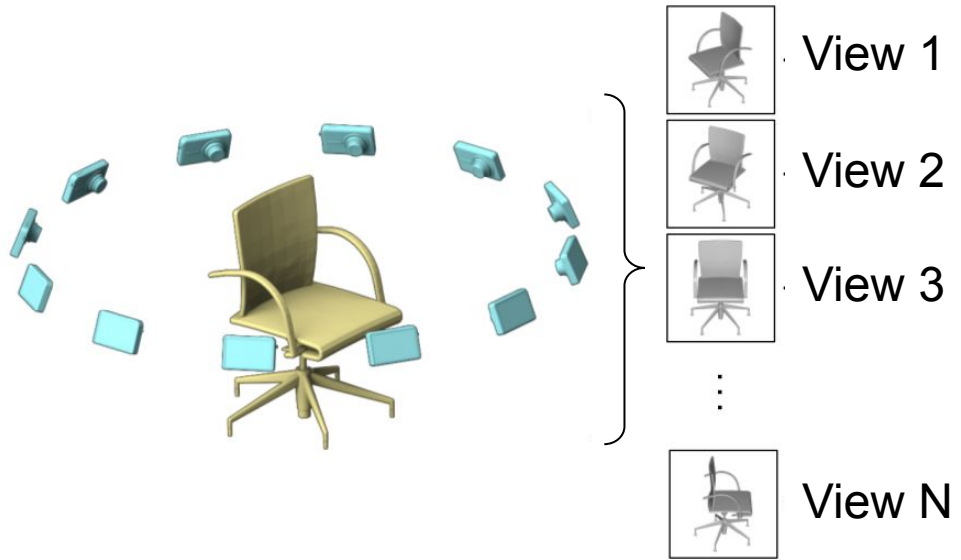


Constructive Solid Geometry

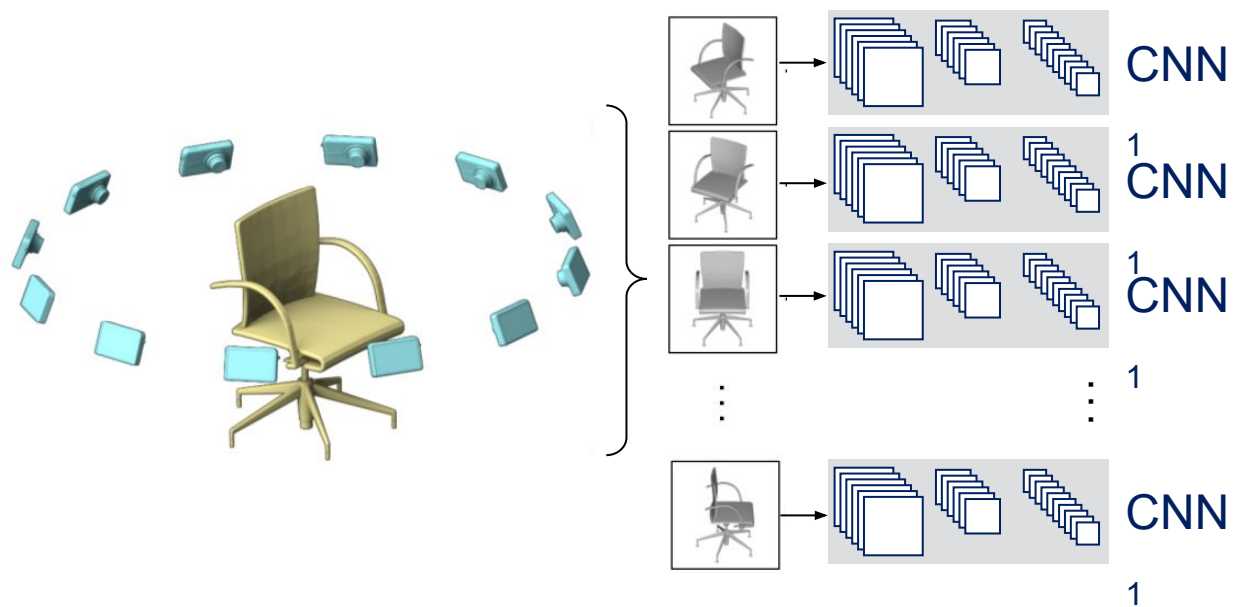
Multi-View CNN



Multi-View CNN

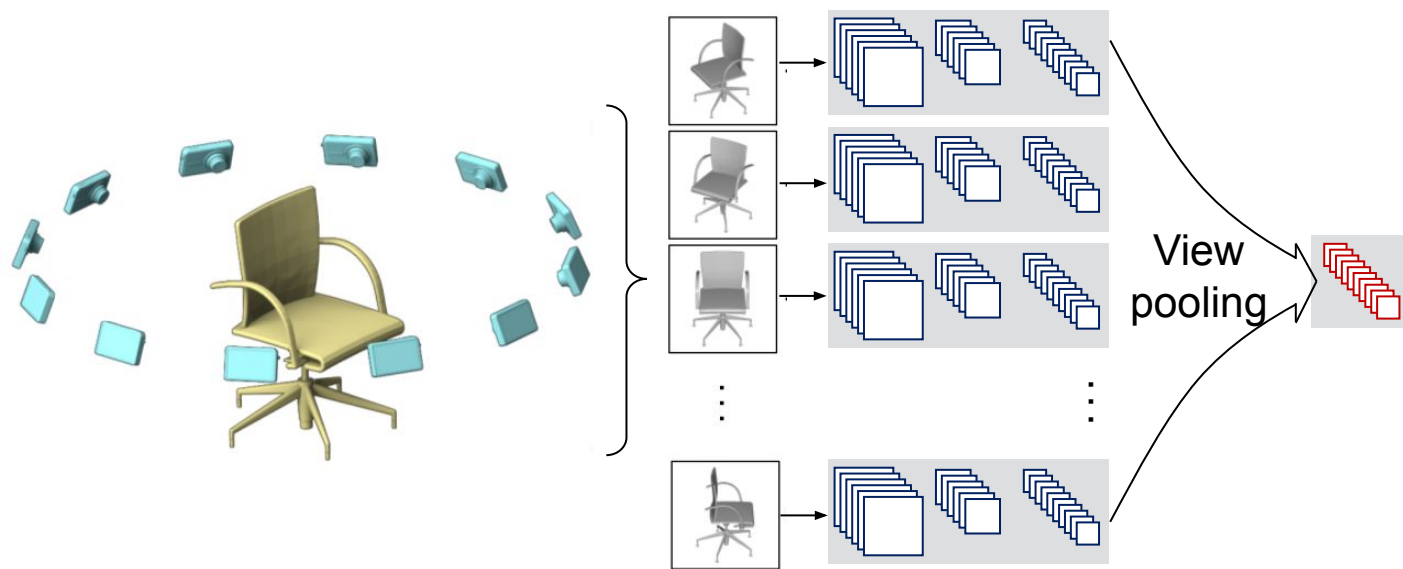


Multi-View CNN



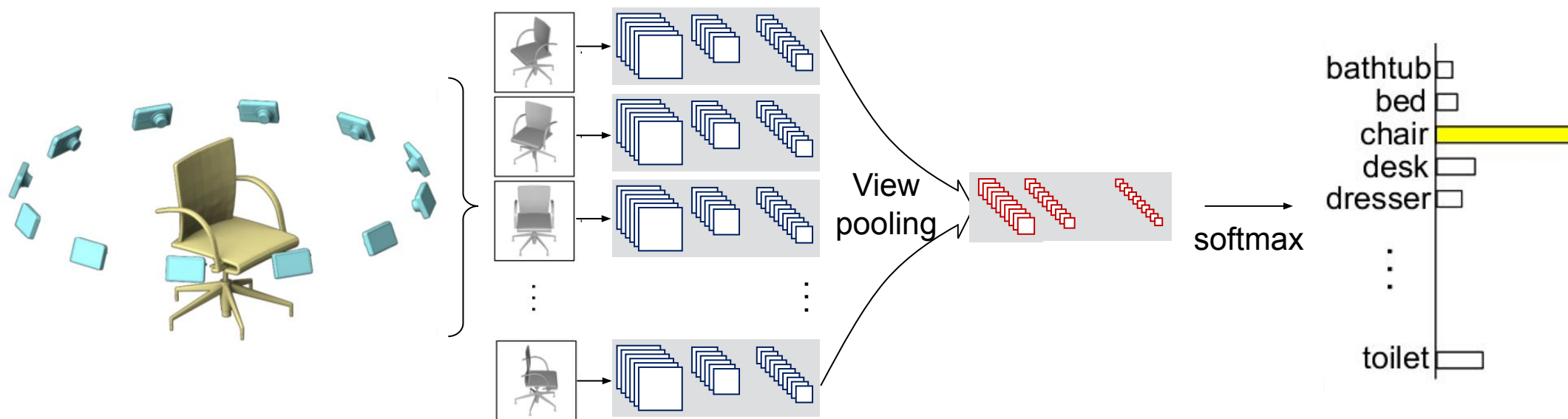
CNN_1 : a ConvNet extracting image features

Multi-View CNN



View pooling: element-wise
max-pooling across all views

Multi-View CNN



CNN₂: a second ConvNet
producing shape descriptors

Experiments – Classification & Retrieval

Non-deep {

Method	Classification	Retrieval
	(Accuracy)	(mAP)
SPH	68.2%	33.3%
LFD	75.5%	40.9%
3D ShapeNets	77.3%	49.2%
FV, 12 views	84.8%	43.9%
CNN, 12 views	88.6%	62.8%
MVCNN, 12 views	89.9%	70.1%
MVCNN+metric, 12 views	89.5%	80.2%
MVCNN, 80 views	90.1%	70.4%
MVCNN+metric, 80 views	90.1%	79.5%

On ModelNet

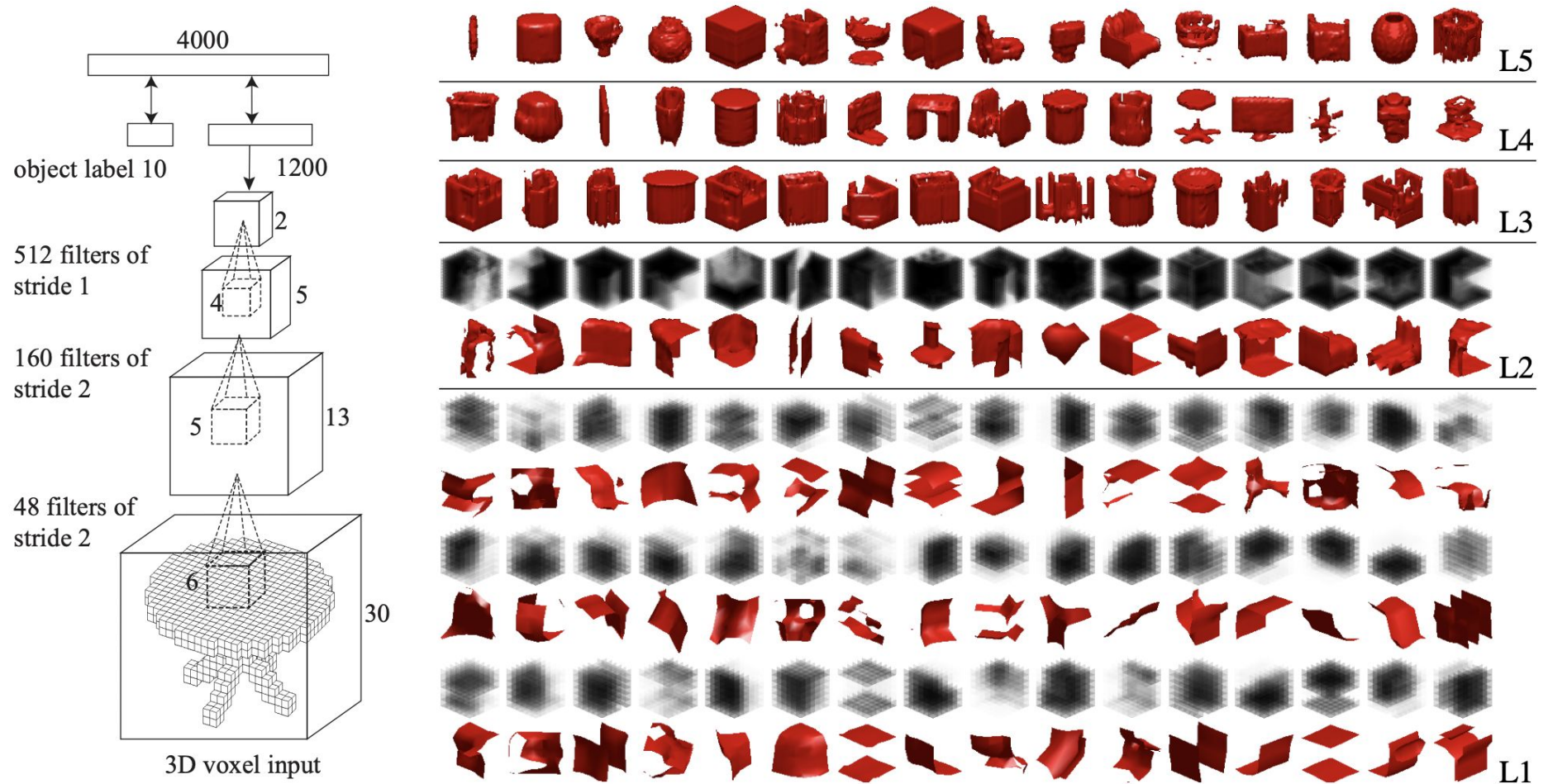
Multi-View Representations

- Indeed gives good performance
- Can leverage vast literature of image classification
- Can use pertained features

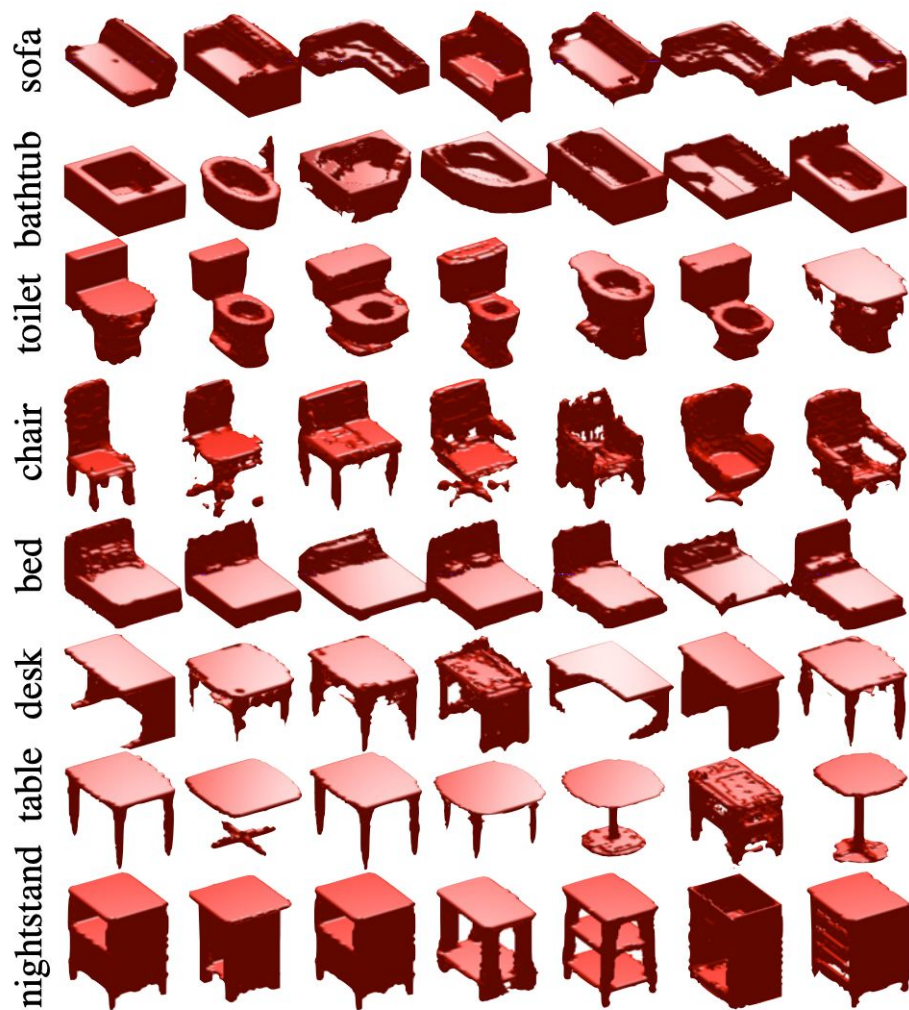
- Need projection
- What if the input is noisy and/or incomplete? e.g., point cloud

Pixels -> Voxels

- 3D Conv Deep Belief Networks (CDBN)



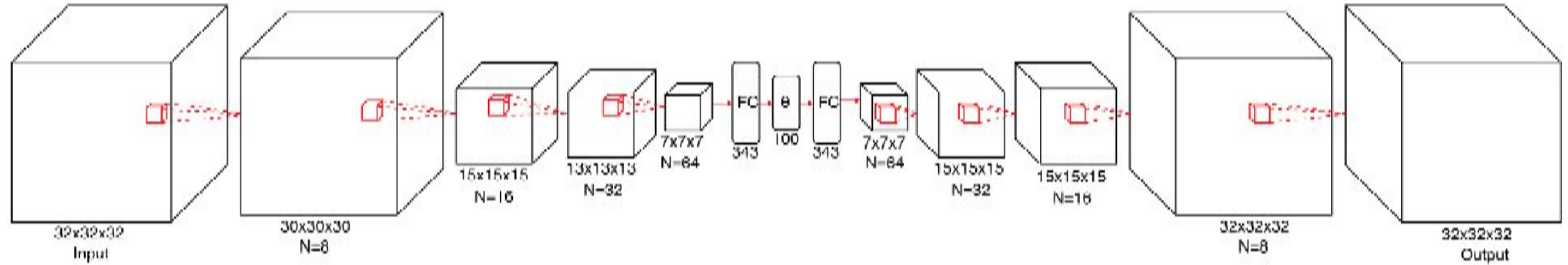
Generative Modeling



10 classes	SPH [18]	LFD [8]	Ours
classification	79.79 %	79.87 %	83.54%
retrieval AUC	45.97%	51.70%	69.28%
retrieval MAP	44.05%	49.82%	68.26%
40 classes	SPH [18]	LFD [8]	Ours
classification	68.23%	75.47%	77.32%
retrieval AUC	34.47%	42.04%	49.94%
retrieval MAP	33.26%	40.91%	49.23%

Table 1: Shape Classification and Retrieval Results.

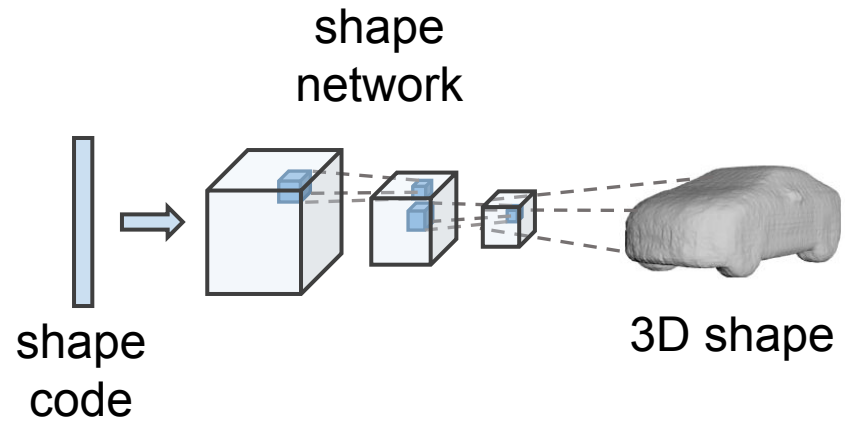
Volumetric Autoencoders



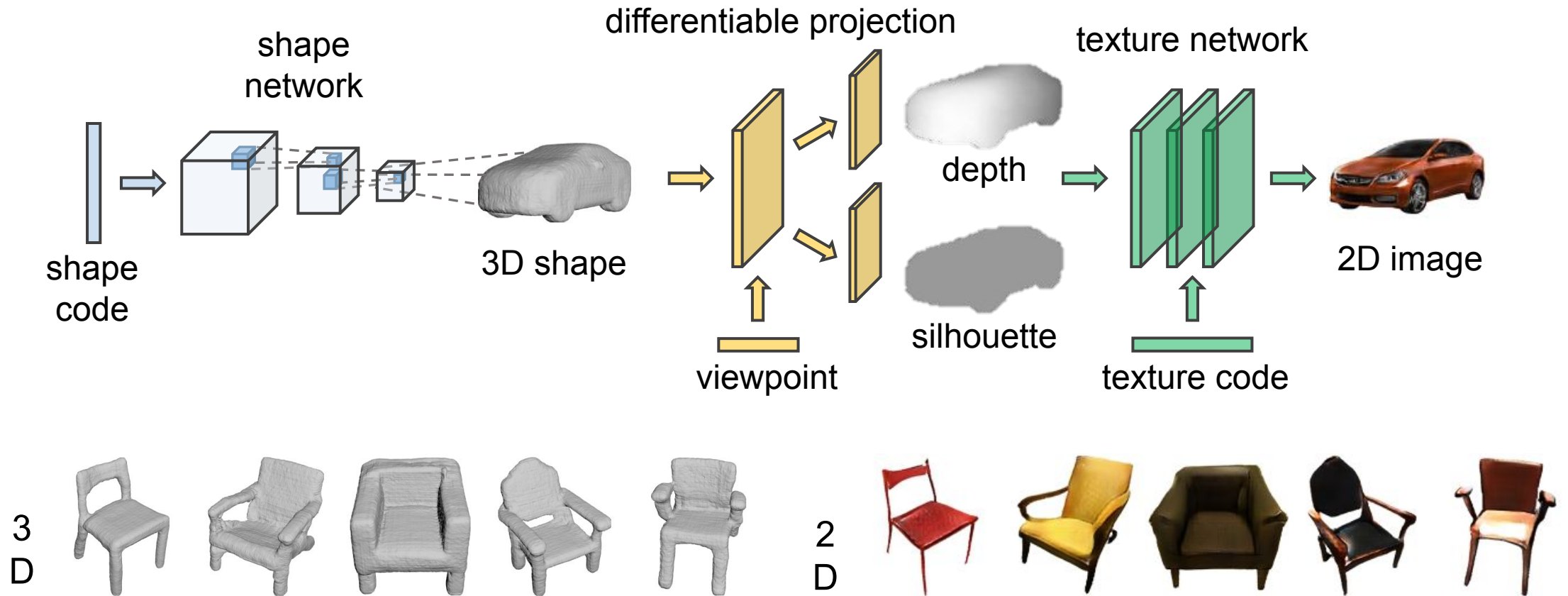
Binary Cross-Entropy Loss: $\mathcal{L} = -l \log(o) - (1 - l) \log(1 - o)$



3D-GANs



Visual Object Networks



Editing viewpoint, shape, and

texture

viewpoint



shape



texture



viewpoint



shape



texture



Interpolation in the latent

space

shape



texture



both



Transferring shape and

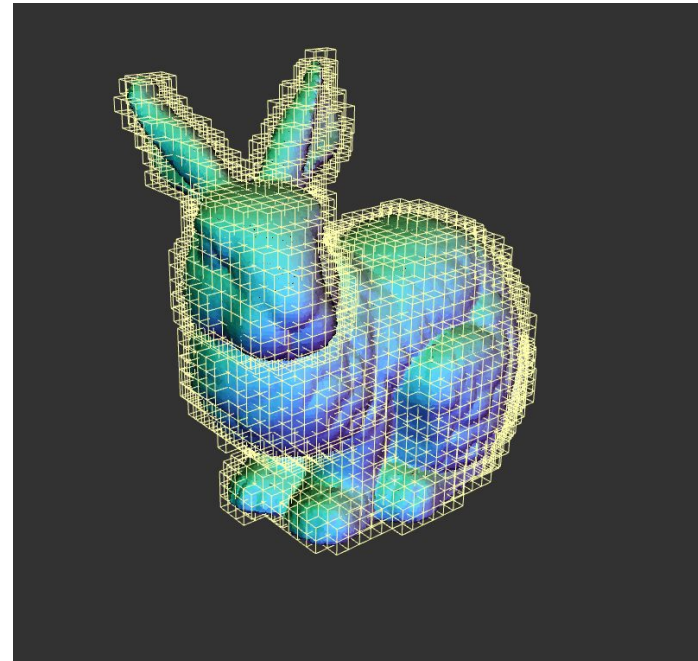
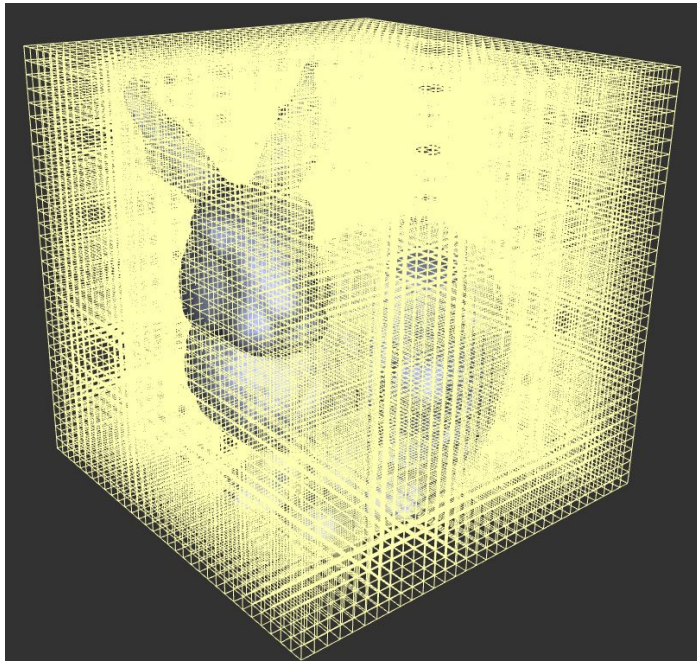
shape
image

texture

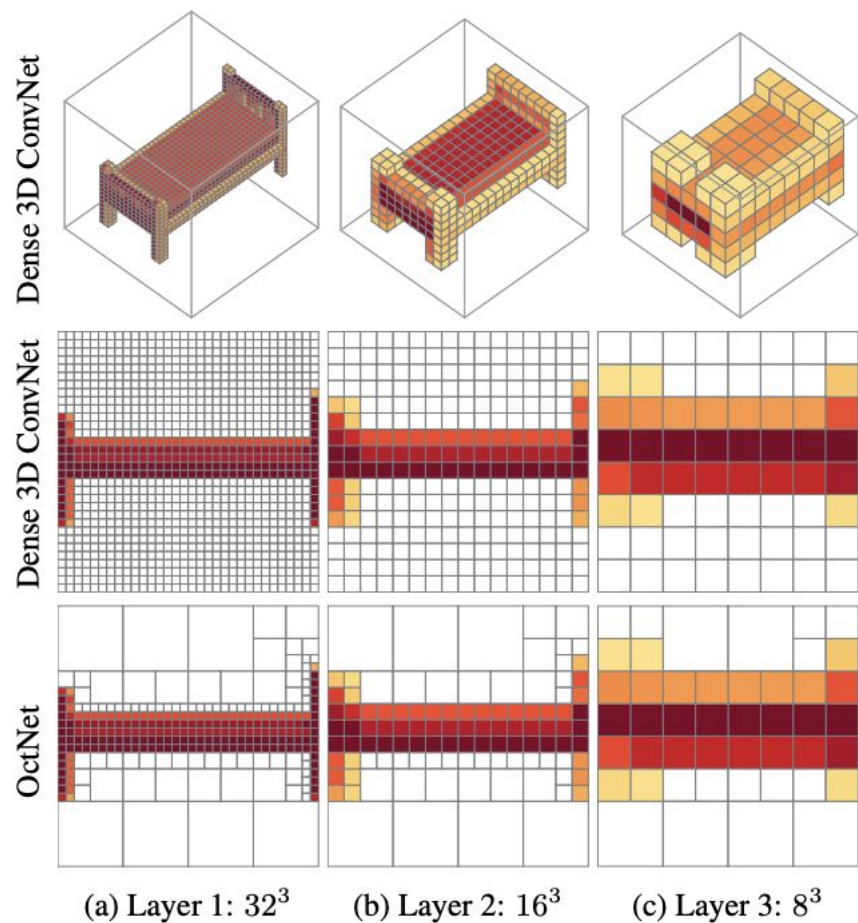


Octave Tree Representations

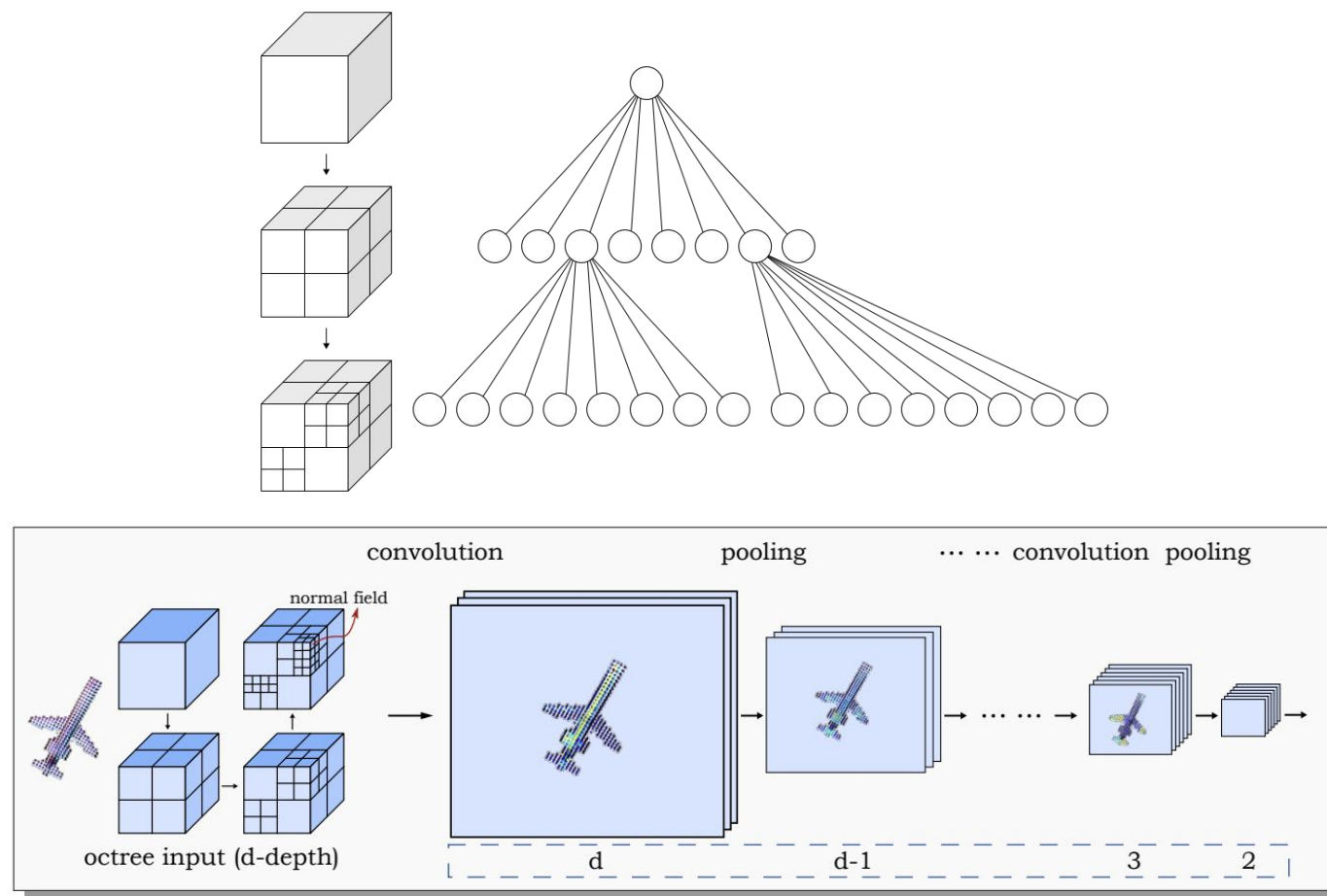
- Store the sparse surface signals
- Constrain the computation near the surface



Octree: Recursively Partition the Space

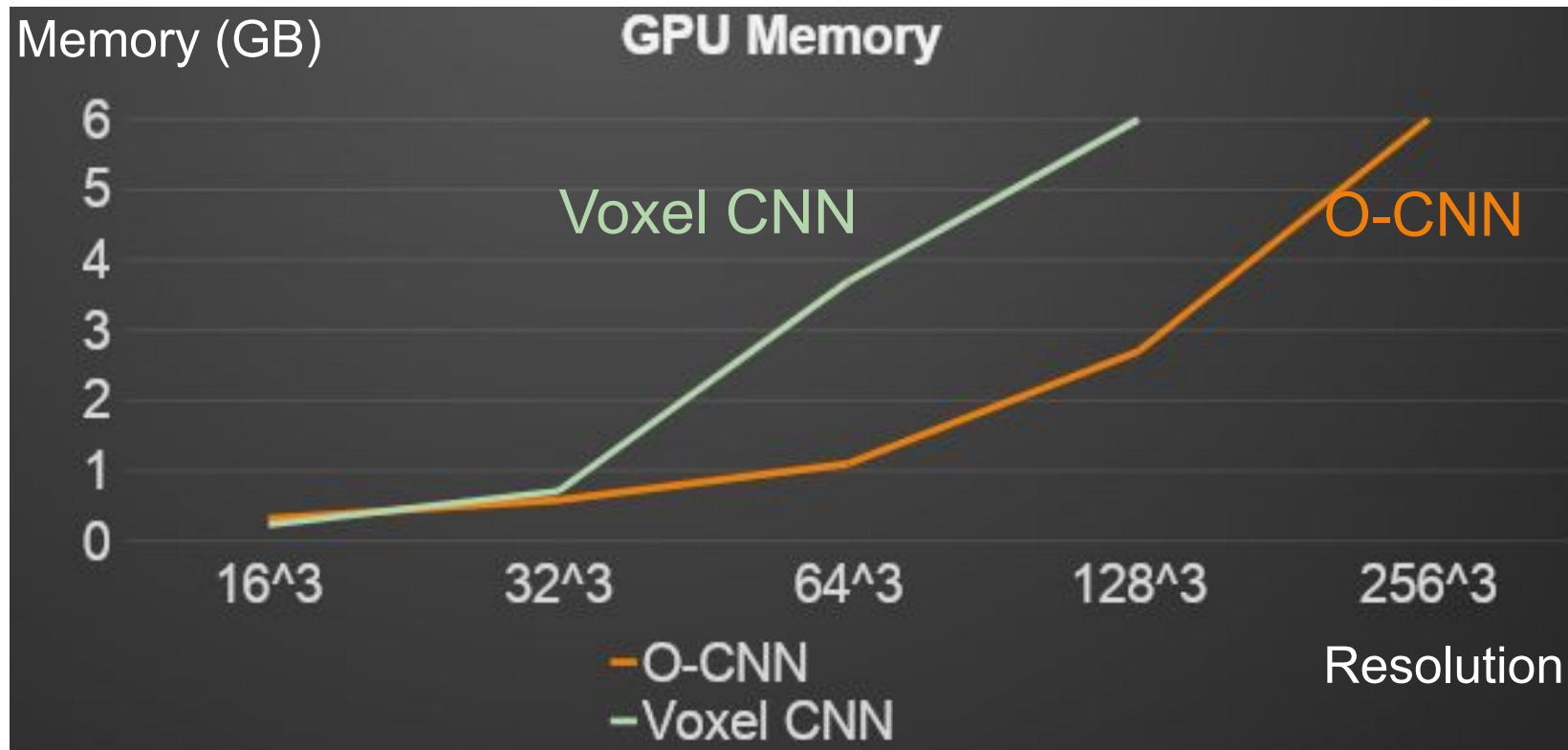


Riegler et al. OctNet. CVPR 2017

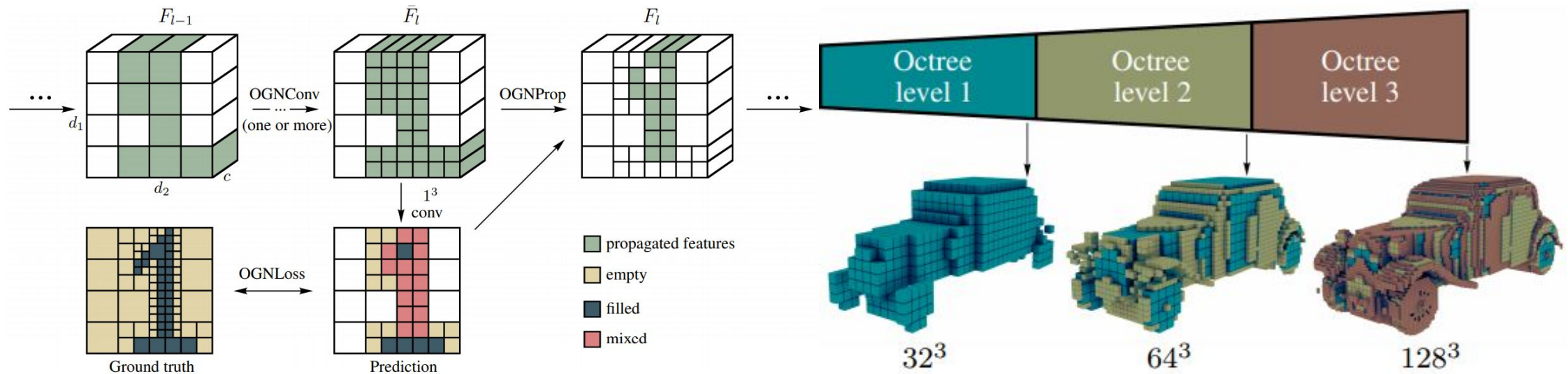


Wang et al. O-CNN. SIGGRAPH 2017

Memory Efficiency



Octree Generating Networks

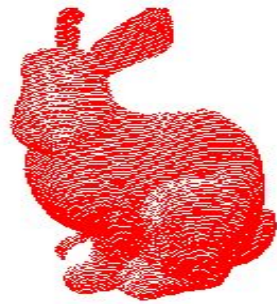


Eulerian -> Lagrangian

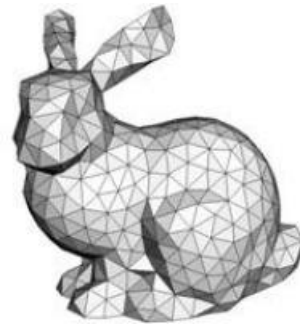
Explicit

Implicit (Eulerian)

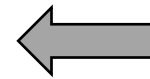
Non-parametric



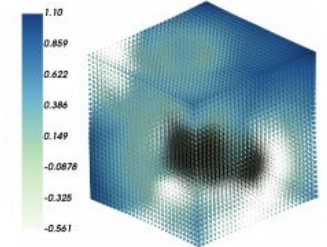
Points



Meshes

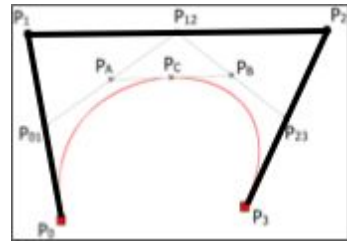


Voxels

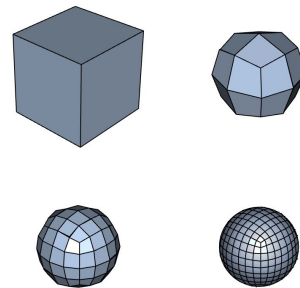


Level Sets

Parametric



Splines

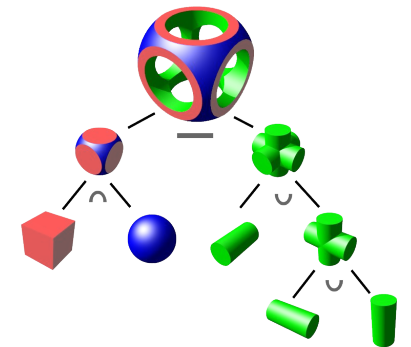


Subdivision Surfaces



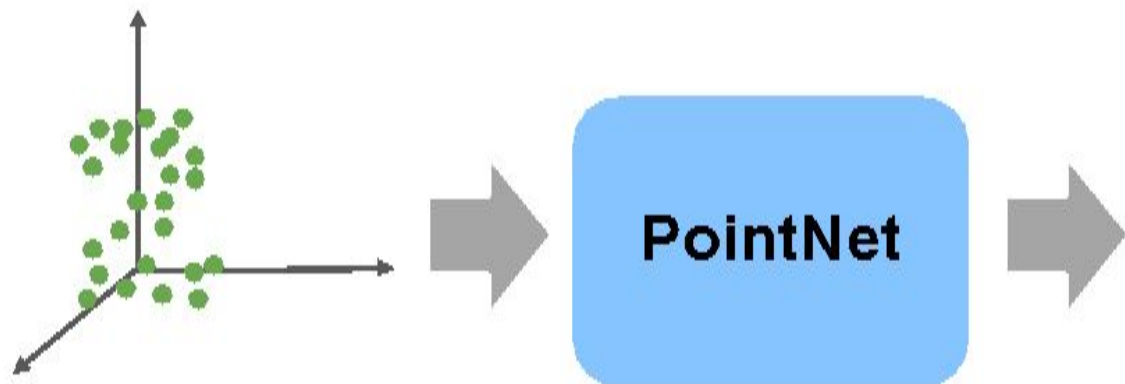
$$x^2 + y^2 + z^2 = 1$$

Algebraic Surfaces



Constructive Solid Geometry

PointNet: First Learning Tool for Point Clouds



Object Classification

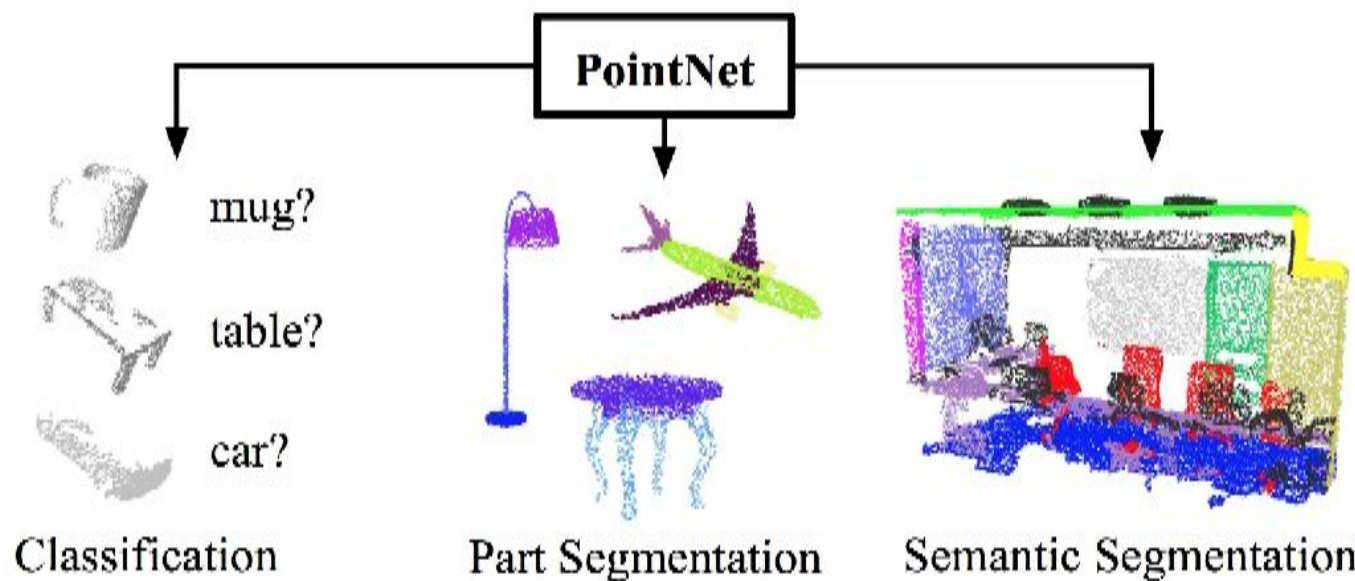
Object Part Segmentation

Semantic Scene Parsing

...

End-to-end learning for irregular point data

Unified framework for various tasks



Slide credit: He Wang

Charles R. Qi, Hao Su, Kaichun Mo, Leonidas J. Guibas.
PointNet: Deep Learning on Point Sets for 3D
Classification and Segmentation. (CVPR'17)

Invariances

The model has to respect key desiderata for point clouds:

Point Permutation Invariance

Point cloud is a set of **unordered** points

Sampling Invariance

Output a function of the underlying geometry and **not the sampling**

Permutation Invariance: Symmetric Functions

$$f(x_1, x_2, \dots, x_n) \equiv f(x_{\pi_1}, x_{\pi_2}, \dots, x_{\pi_n}), \quad x_i \in \mathbb{R}^D$$

Examples:

$$f(x_1, x_2, \dots, x_n) = \max\{x_1, x_2, \dots, x_n\}$$

$$f(x_1, x_2, \dots, x_n) = x_1 + x_2 + \dots + x_n$$

...

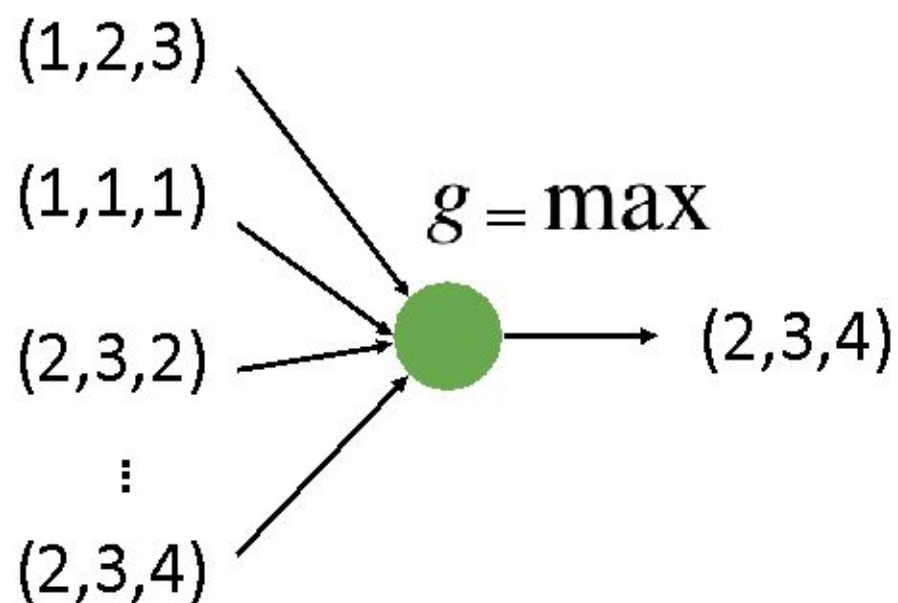
How can we construct a universal family of symmetric functions by neural networks?

Construct Symmetric Functions by Neural Networks

Simplest form: directly aggregate all points with a symmetric operator

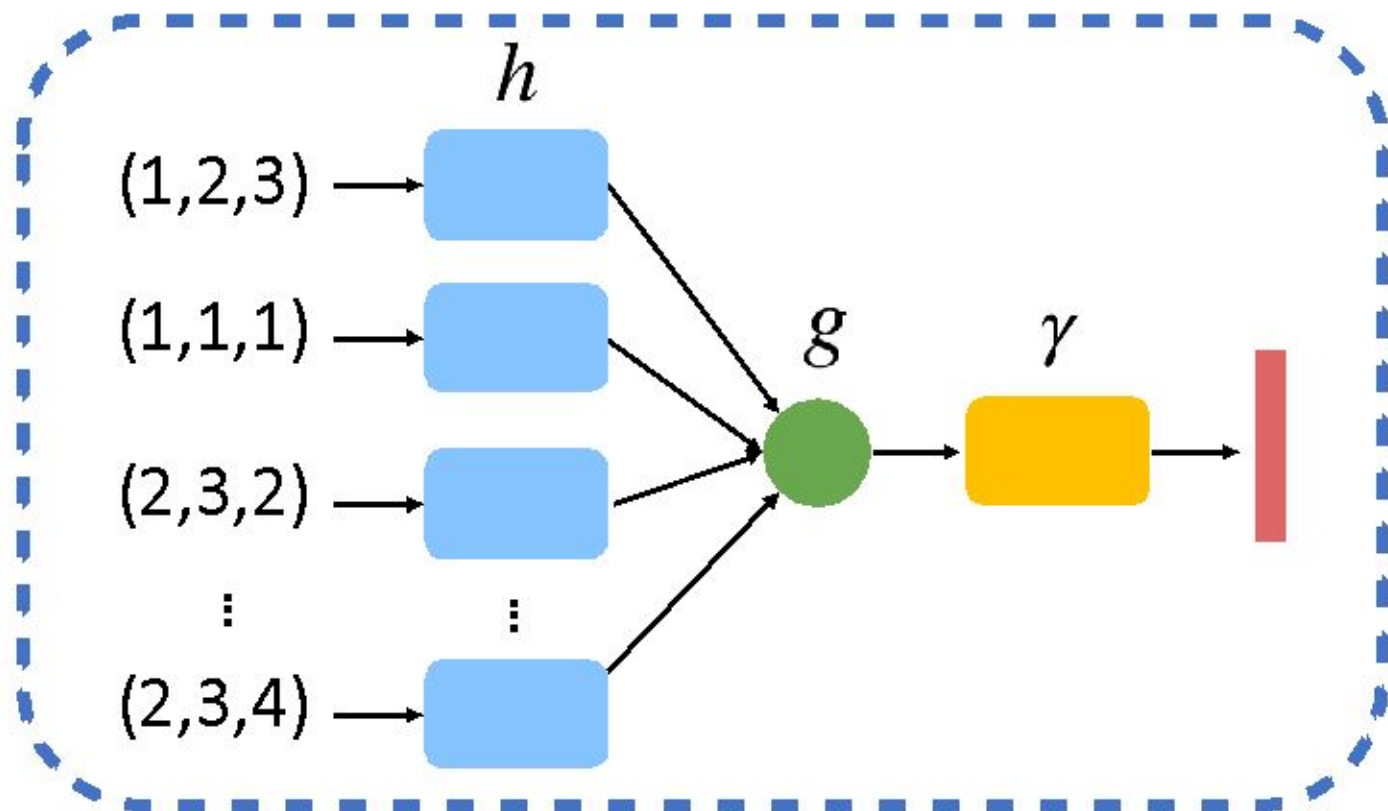
g

Just discovers simple extreme/aggregate properties of the geometry.



Construct Symmetric Functions by Neural Networks

$f(x_1, x_2, \dots, x_n) = \gamma \circ g(h(x_1), \dots, h(x_n))$ is symmetric if g is symmetric

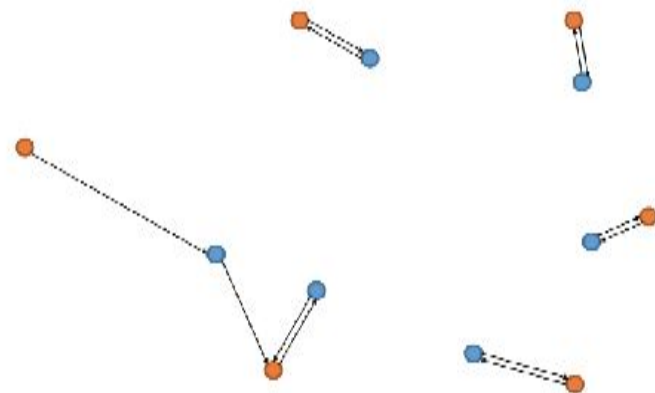


PointNet (vanilla)

Distance Metrics for Point Cloud

Chamfer distance We define the Chamfer distance between $S_1, S_2 \subseteq \mathbb{R}^3$ as:

$$d_{CD}(S_1, S_2) = \sum_{x \in S_1} \min_{y \in S_2} \|x - y\|_2 + \sum_{y \in S_2} \min_{x \in S_1} \|x - y\|_2$$



Distance Metrics for Point Cloud

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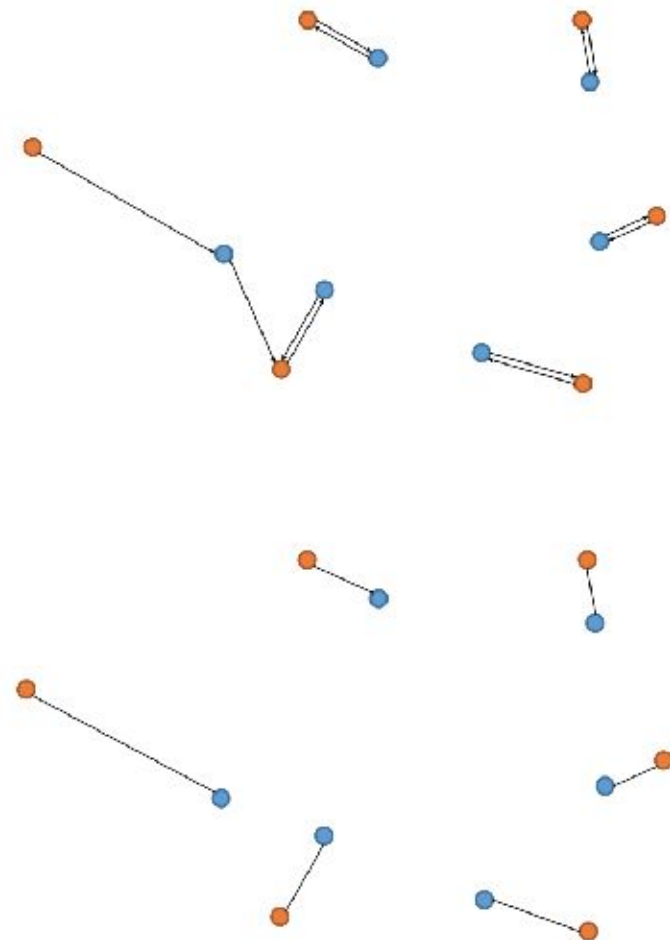
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Earth Mover's distance Consider $S_1, S_2 \subseteq \mathbb{R}^3$ of equal size $s = |S_1| = |S_2|$. The EMD between A and B is defined as:

$$d_{EMD}(S_1, S_2) = \min_{\phi: S_1 \rightarrow S_2} \sum_{x \in S_1} \|x - \phi(x)\|_2$$

where $\phi : S_1 \rightarrow S_2$ is a bijection.

A Point Set Generation Network for 3D Object
Reconstruction from a Single Image, CVPR 2016



Slide credit: He Wang

Distance Metrics for Point Cloud

Chamfer distance We define the Chamfer distance between $S_1, S_2 \subseteq \mathbb{R}^3$ as:

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where $\phi : S_1 \rightarrow S_2$ is a bijection.

Sum of closest distances

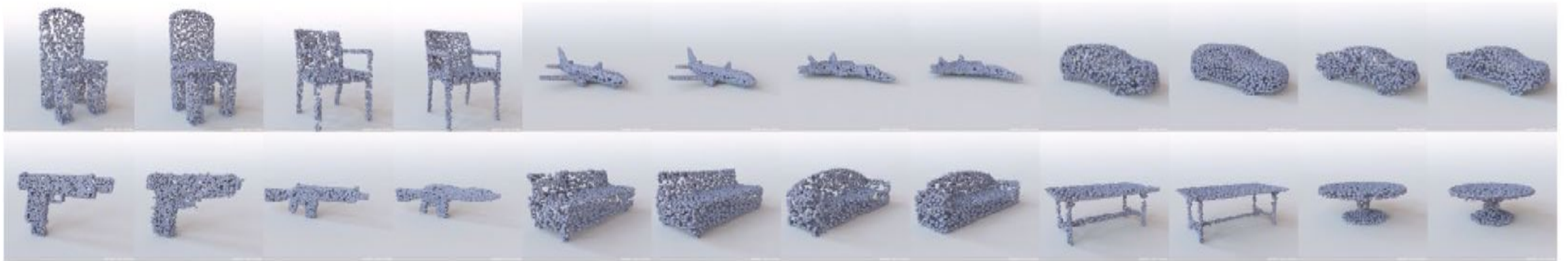
Insensitive to sampling
(only relatively)

Sum of matched closest distances

Sensitive to sampling

Point Cloud AE

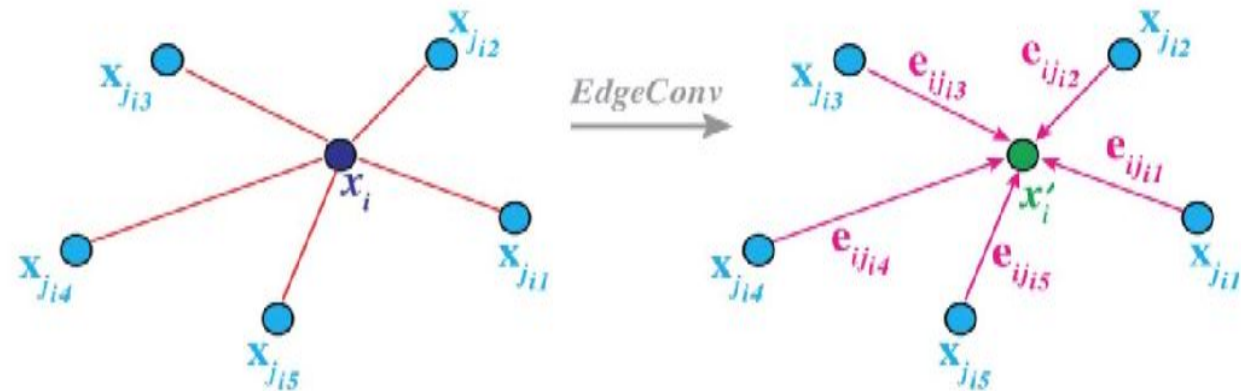
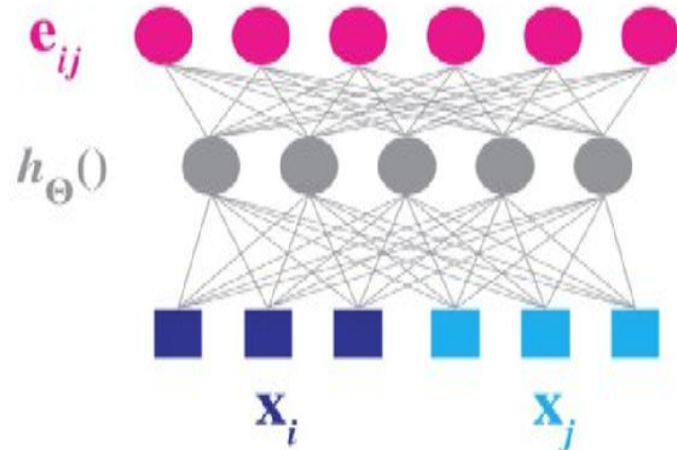
Encoder: PointNet
Decoder: MLP



ICML, 2018, Learning Representations and Generative Models for
3D Point Clouds, Panos Achlioptas, et. al.

Graph NNs on Point Clouds

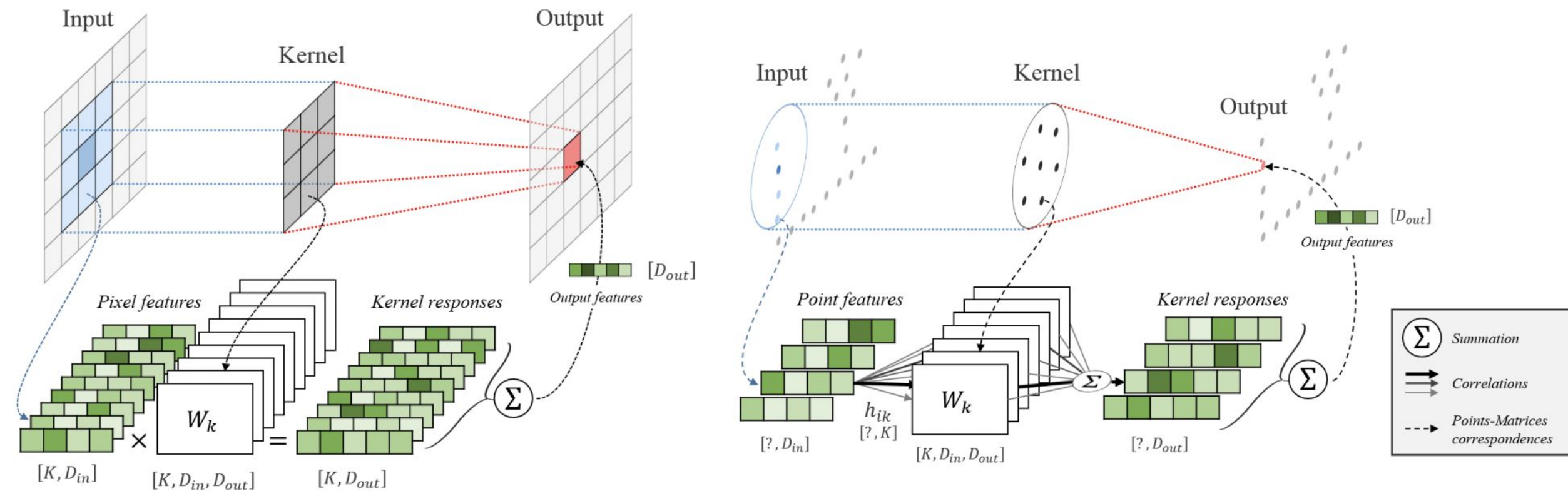
- Points \rightarrow Nodes
- Neighborhood \rightarrow Edges
- Graph NNs for point cloud processing



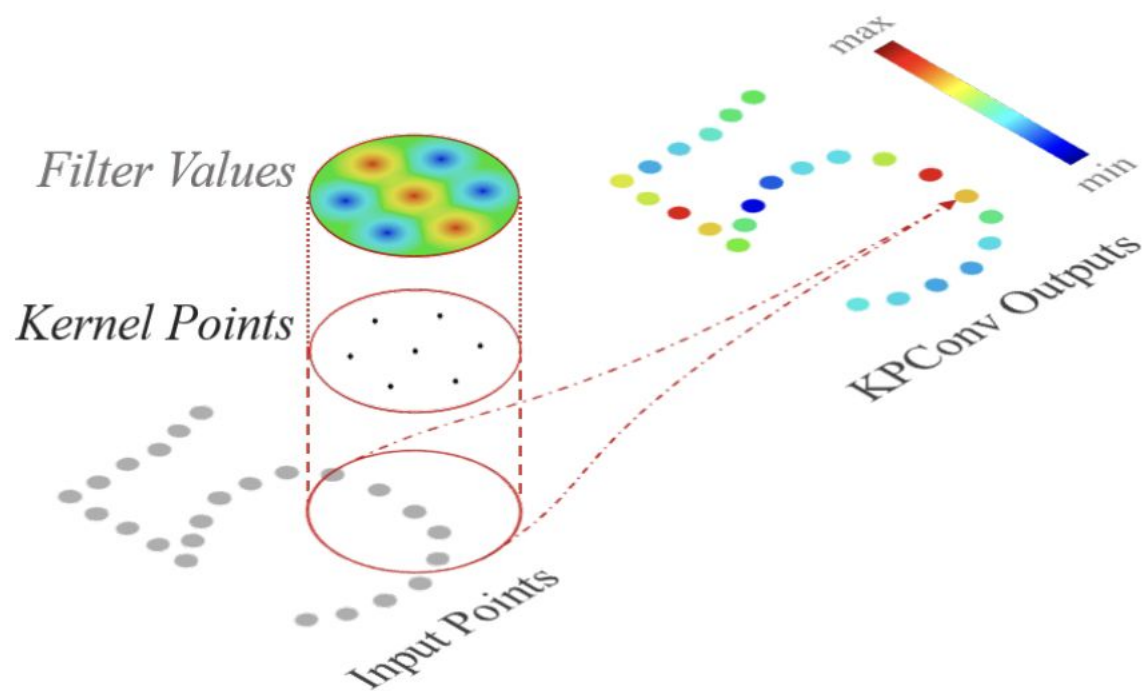
Message-Passing GNNs are not Geometry-Aware

- Points are **sampled** from surfaces.
- Ideally, features describe the geometry of underlying surface. They should be sample invariant.
- Message-passing GNNs do not address sample invariance.
- **Solution:** Estimate the continuous kernel and point density for continuous convolution (KPCConv)

Kernel Point Convolution (KPConv)

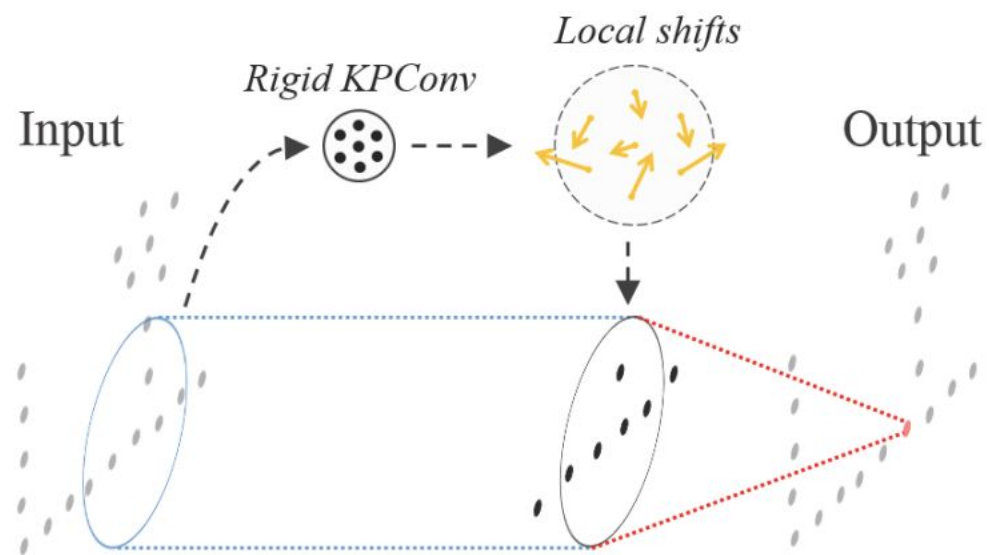


Deformable Kernel for Deformable Objects



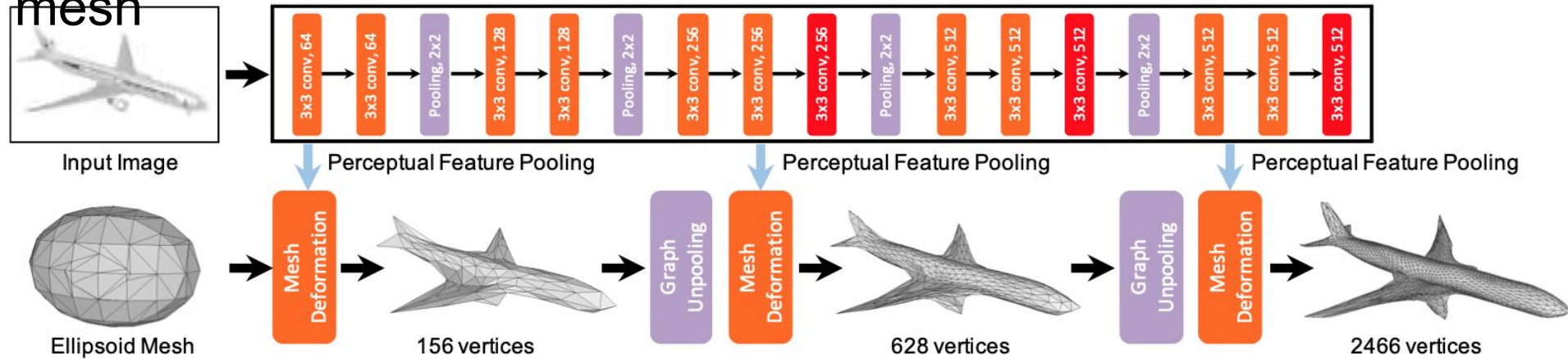
Deformable point-based kernel

- 3D version of 2D deformable convolution

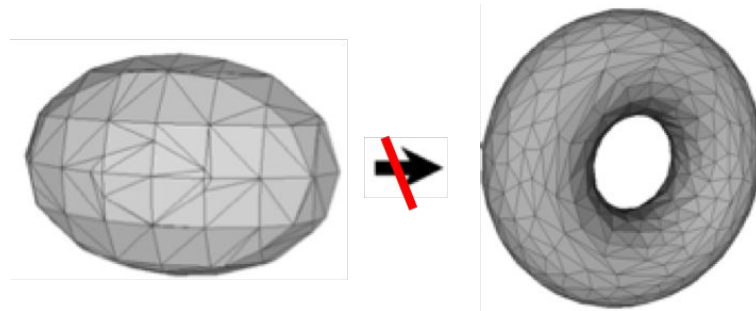


Pixel2Mesh

Learn to deform a template mesh



Cannot change the topology of the template mesh

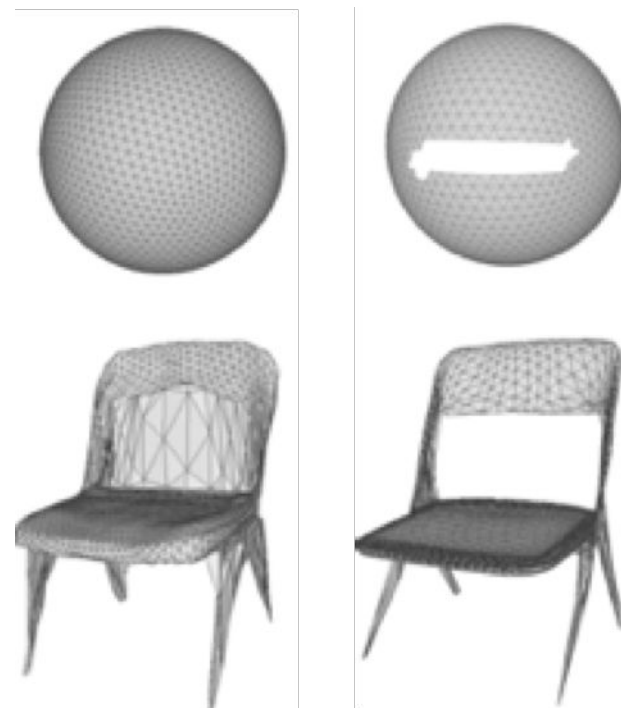


More on Mesh Deformation

Part-level deformation



Modify the topology of the template mesh



Non-Parametric -> Parametric

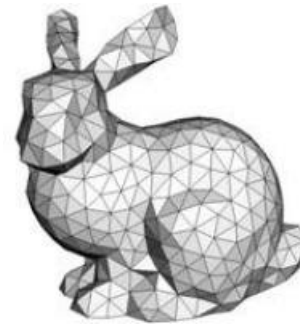
Explicit

Implicit (Eulerian)

Non-parametric



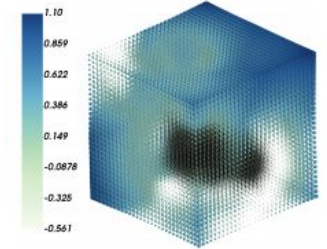
Points



Meshes

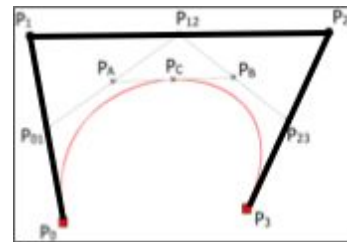


Voxels

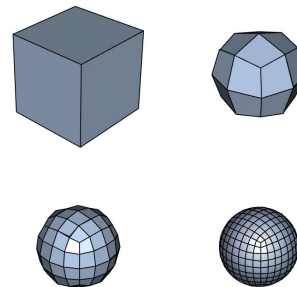


Level Sets

Parametric



Splines

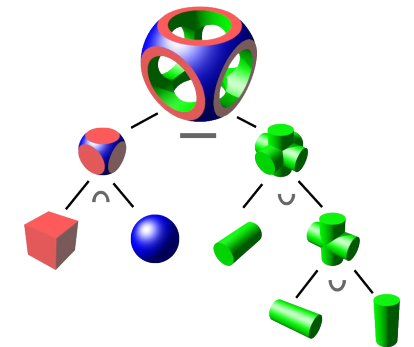


Subdivision Surfaces



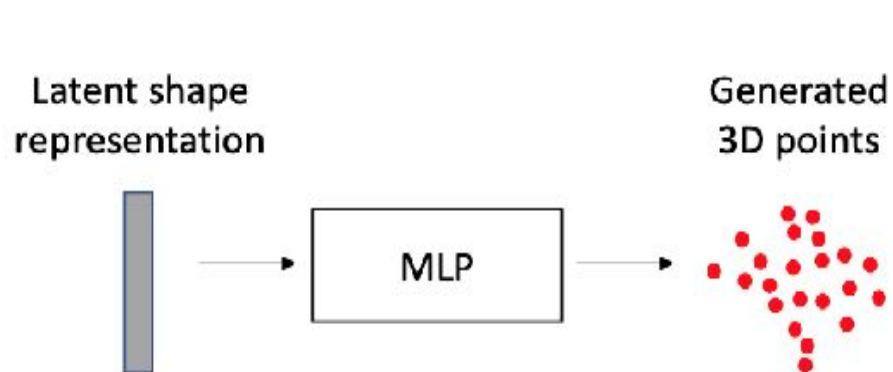
$$x^2 + y^2 + z^2 = 1$$

Algebraic Surfaces



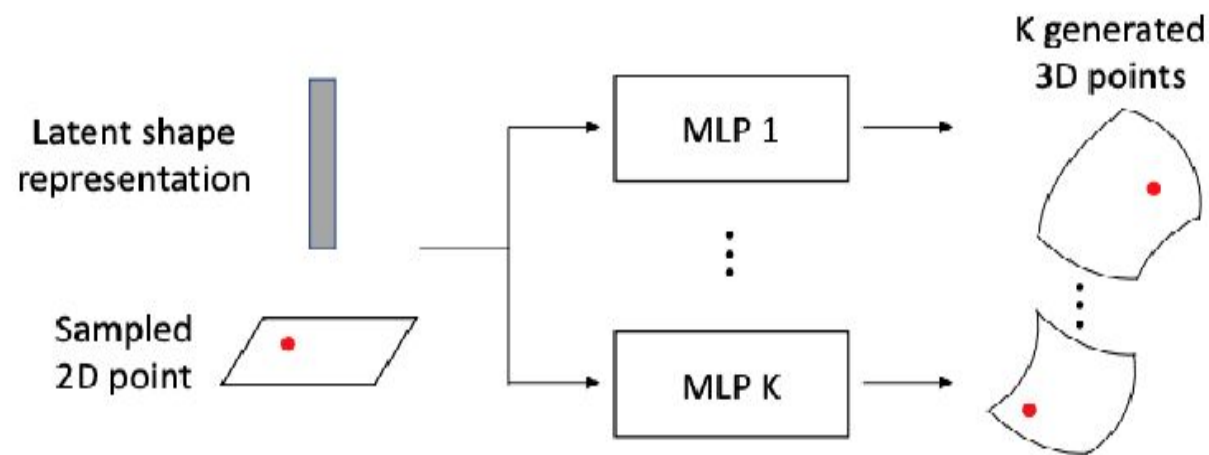
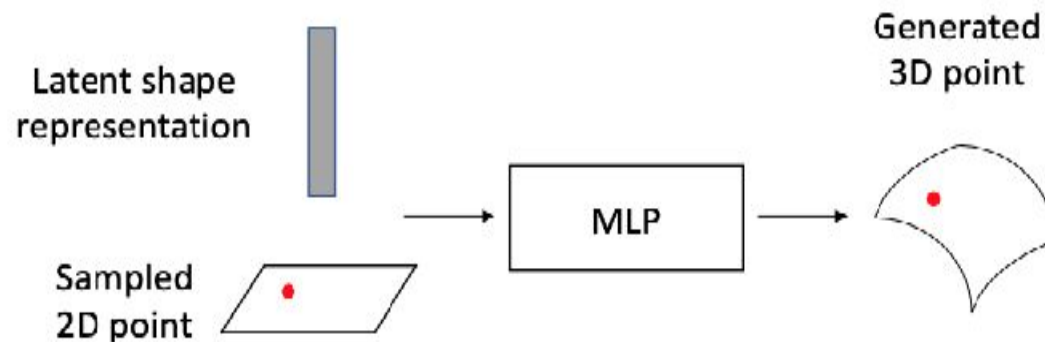
Constructive Solid Geometry

Parametric Decoder: AtlasNet



Given the output points form a smooth surface, enforce such a parametrization as input.

$\text{MLP}(z, u, v) \rightarrow \text{point}$

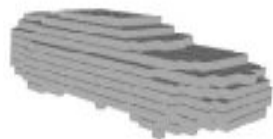
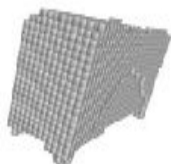
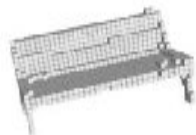


Results

Input image



Voxel



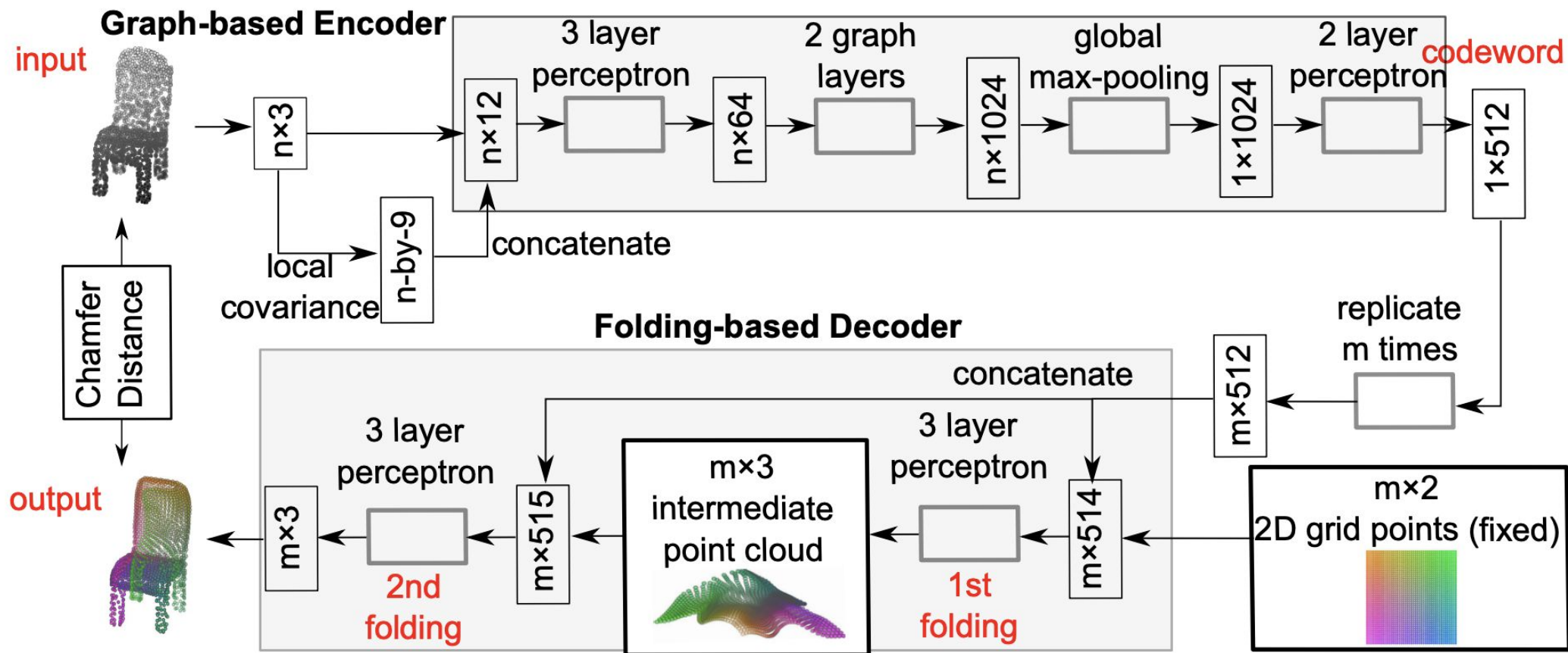
Point cloud



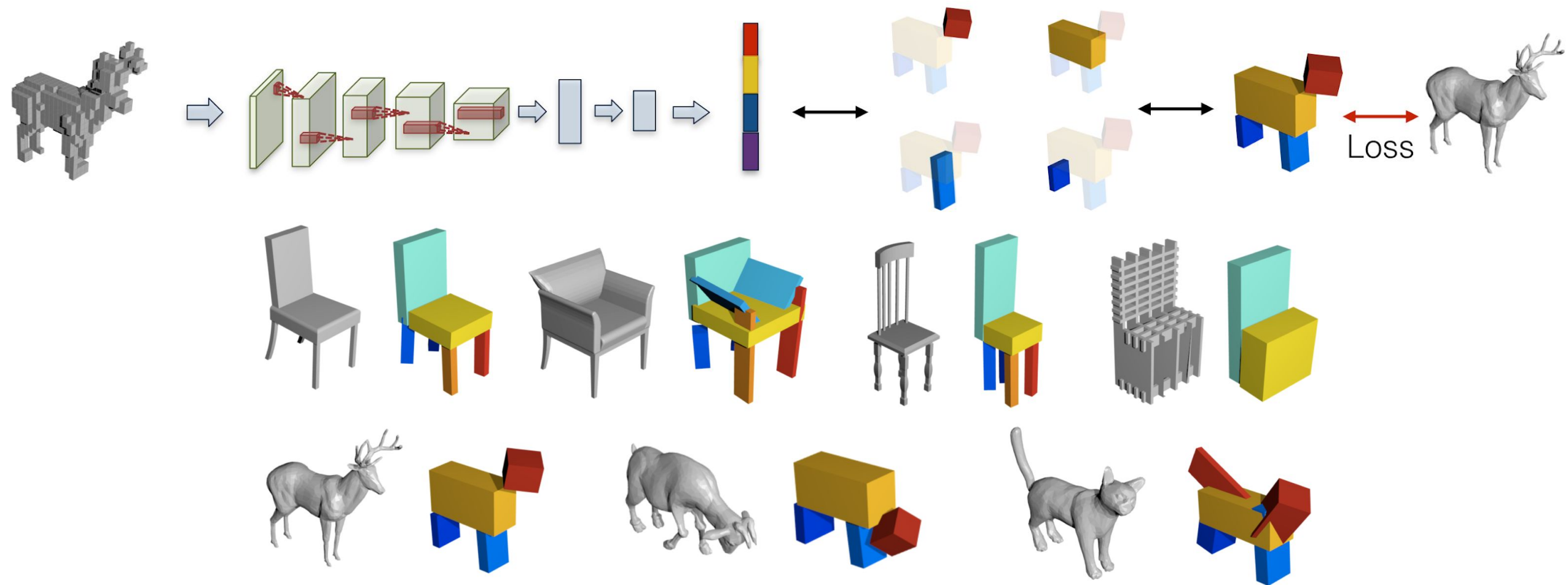
AtlasNet



FoldingNet

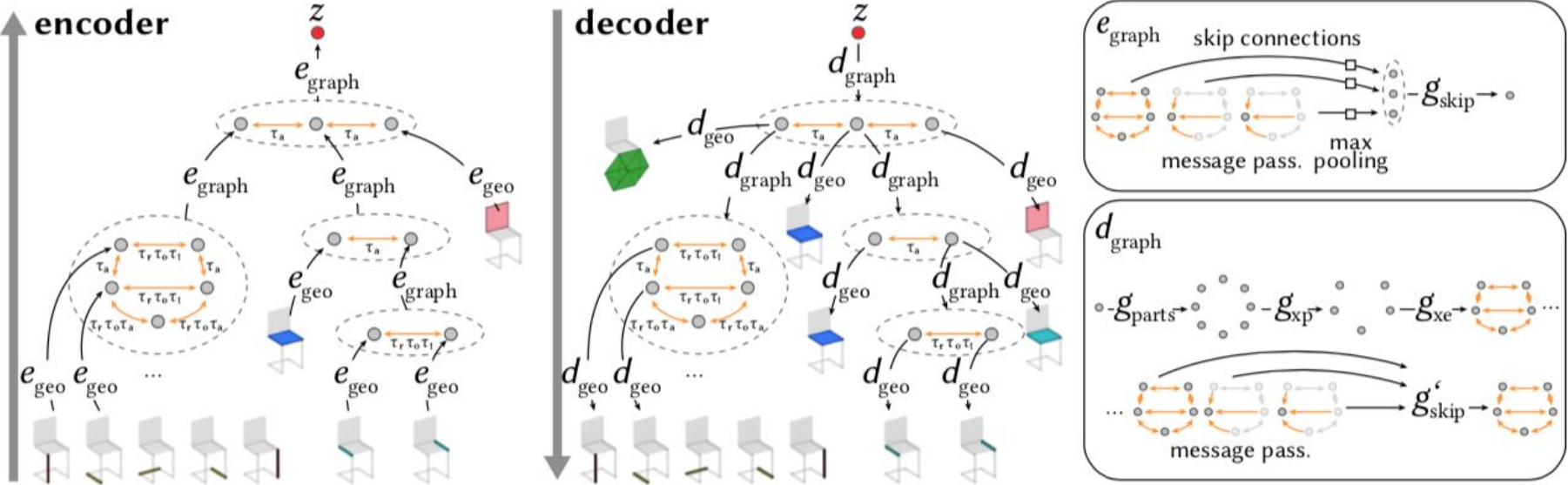


Assembling Volumetric Primitives

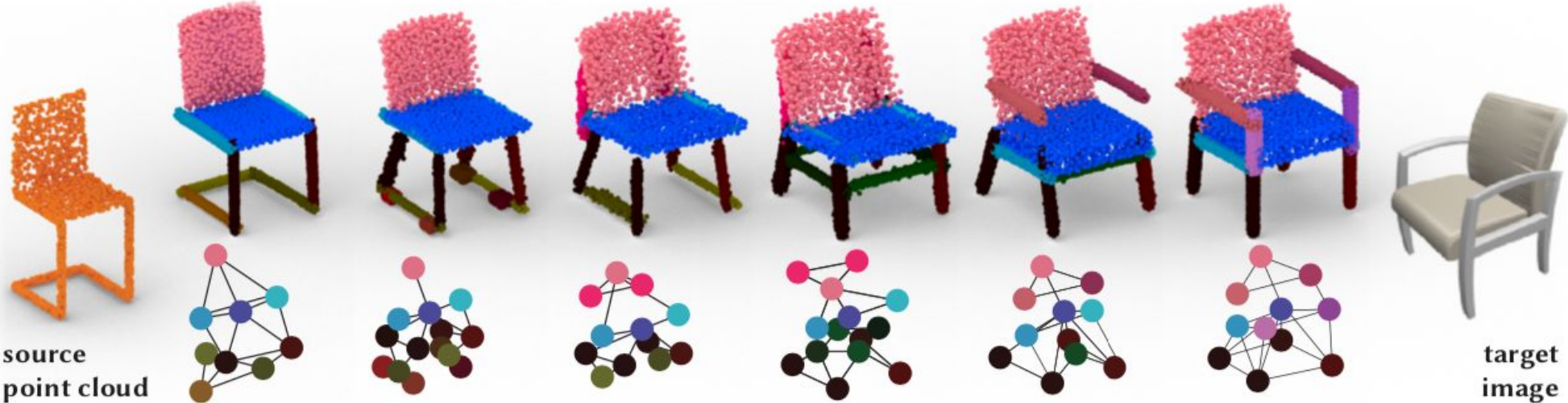


Incorporating Shape Structure

StructureNet



Graph convnets
encode/decode
variable-degree
nodes



Explicit -> Implicit

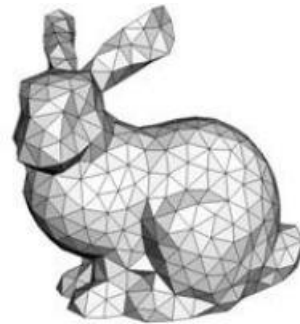
Explicit

Implicit (Eulerian)

Non-parametric



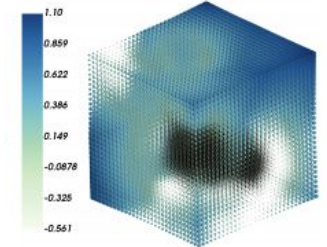
Points



Meshes

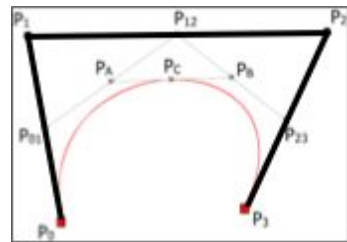


Voxels

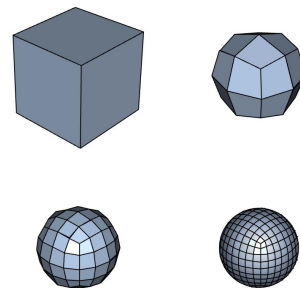


Level Sets

Parametric



Splines

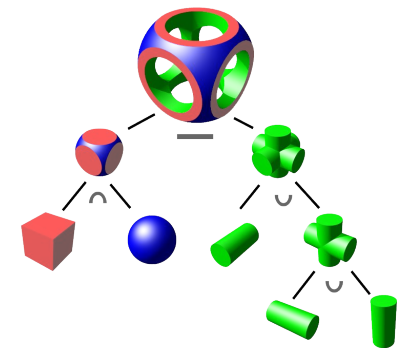


Subdivision Surfaces



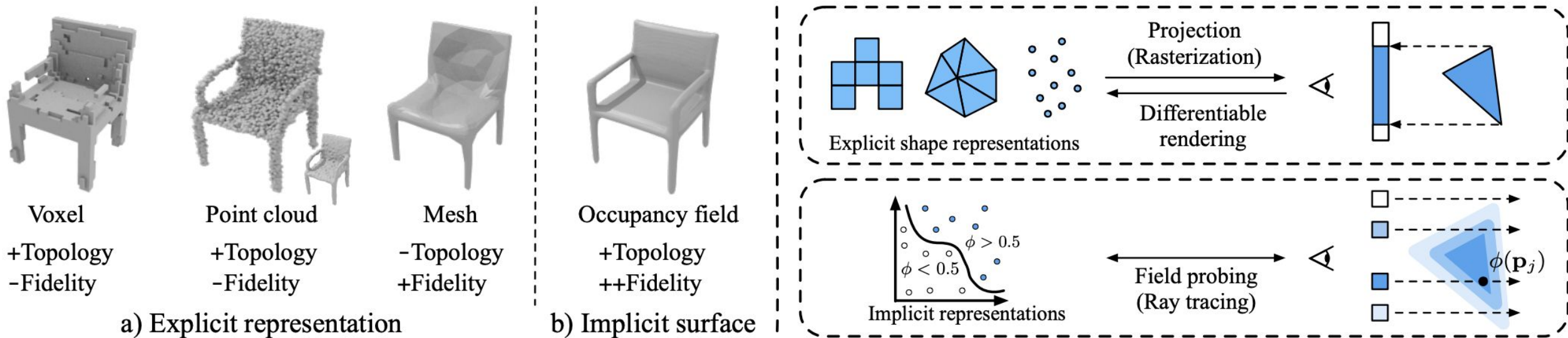
$$x^2 + y^2 + z^2 = 1$$

Algebraic Surfaces

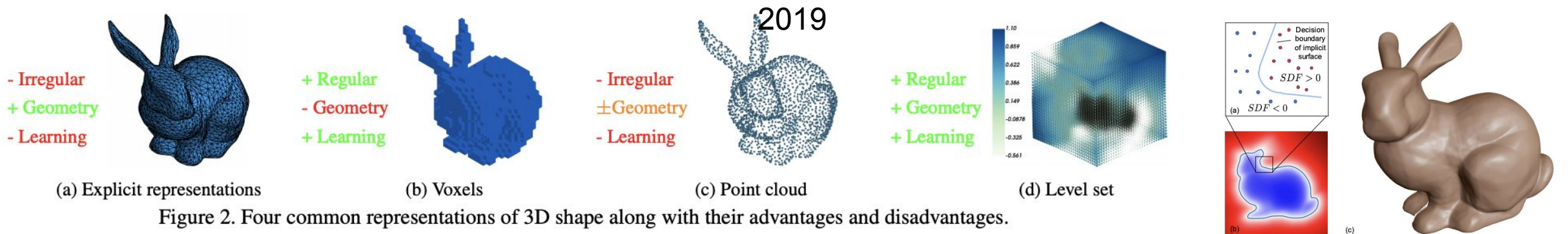


Constructive Solid Geometry

Deep Implicit Functions

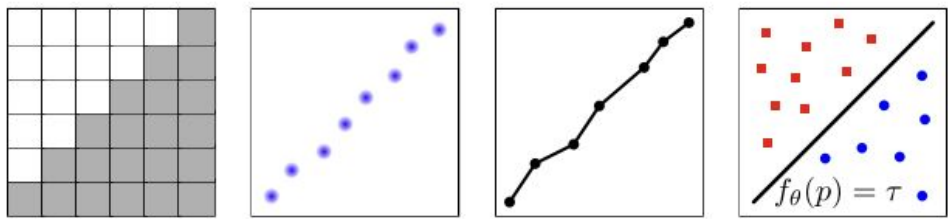


Liu et al. Learning to Infer Implicit Surfaces without 3D Supervision. NeurIPS

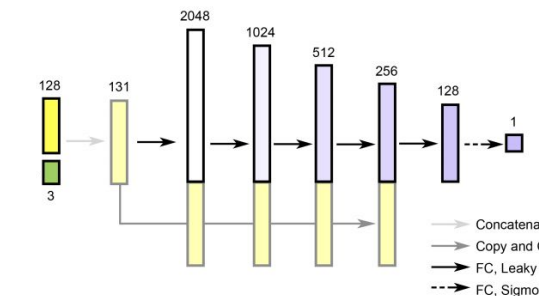


Deep Level Sets: Implicit Surface Representations for 3D Shape Inference. 2019

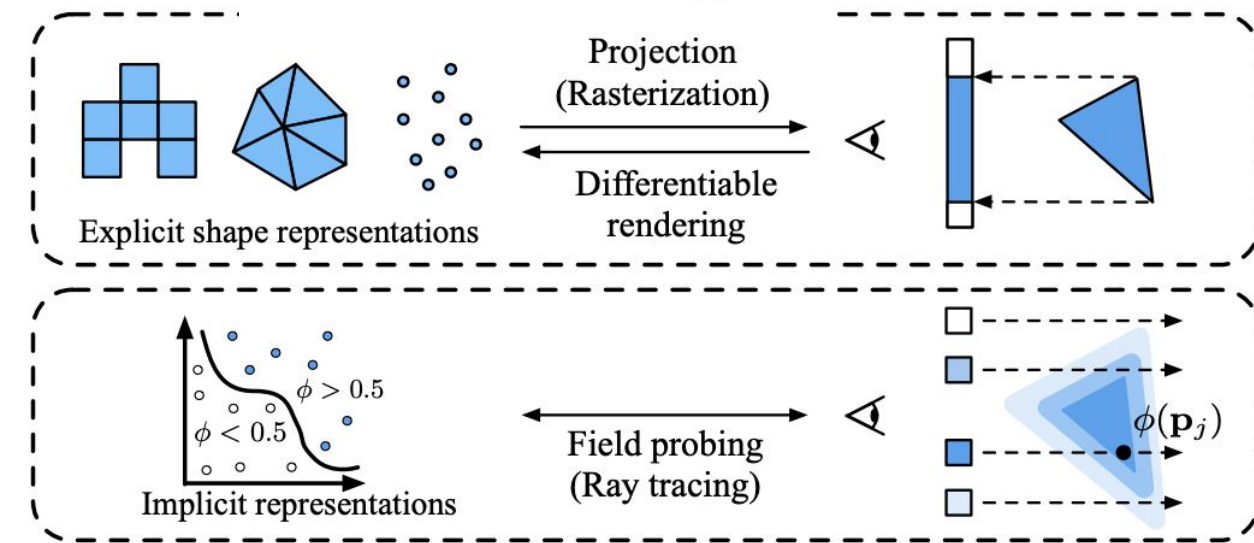
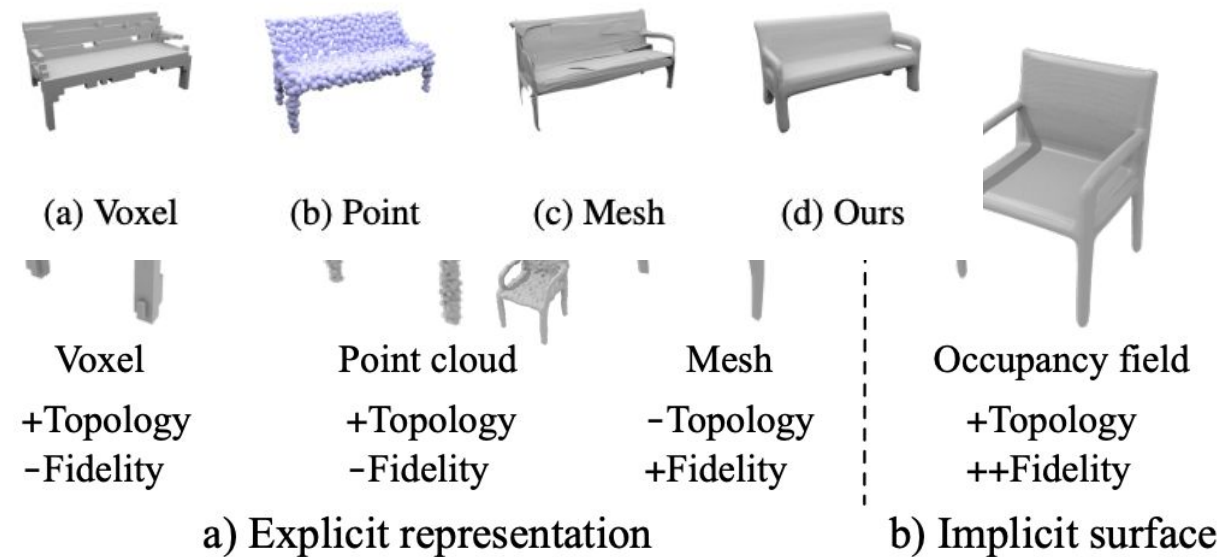
DeepSDF. CVPR 2019



Occupancy
Networks
CVPR 2019



Chen and Zhang.
Learning Implicit
Fields
CVPR 2019



Liu et al. Learning to Infer Implicit Surfaces without 3D Supervision. NeurIPS 2019

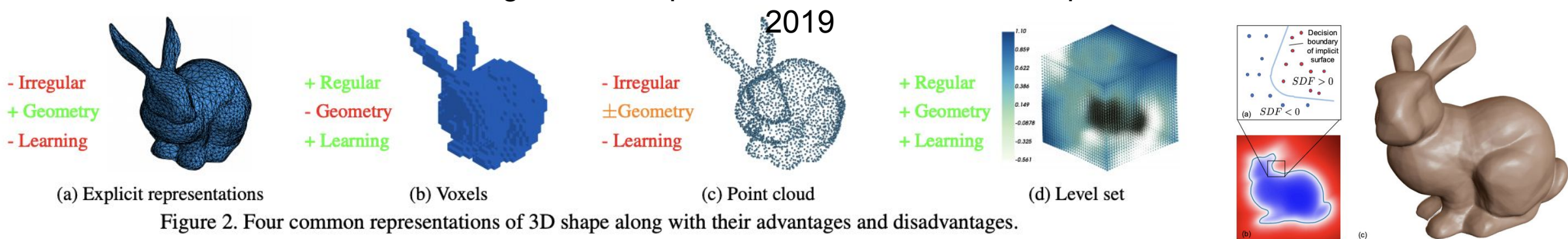


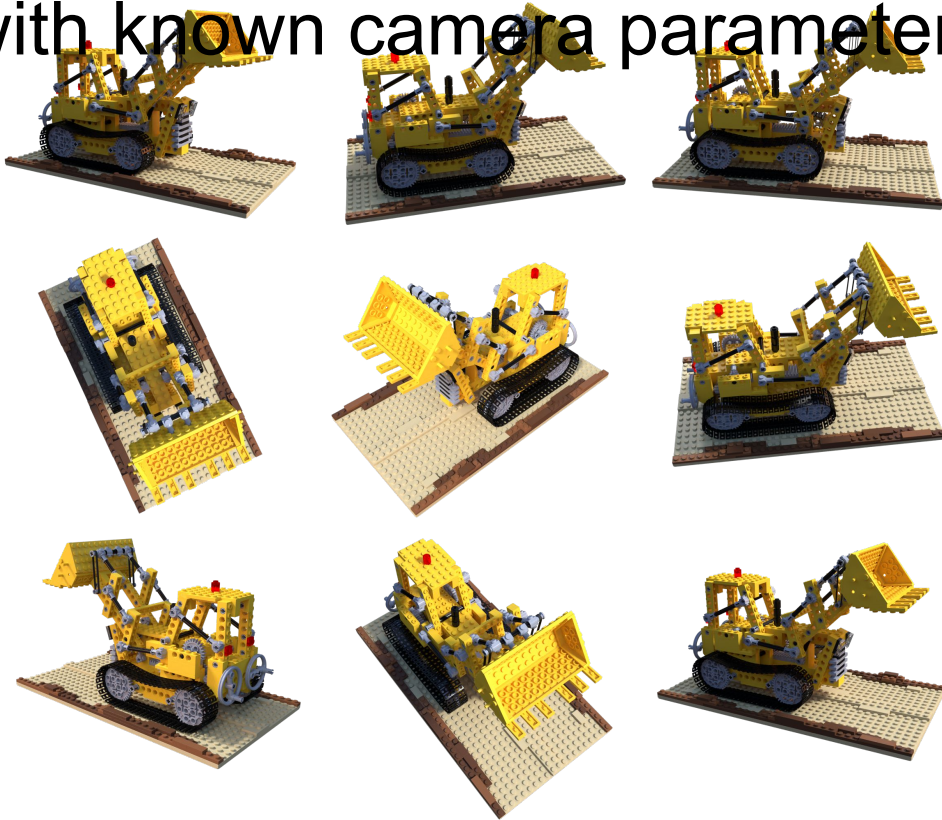
Figure 2. Four common representations of 3D shape along with their advantages and disadvantages.

Deep Level Sets: Implicit Surface Representations for 3D Shape Inference.
2019

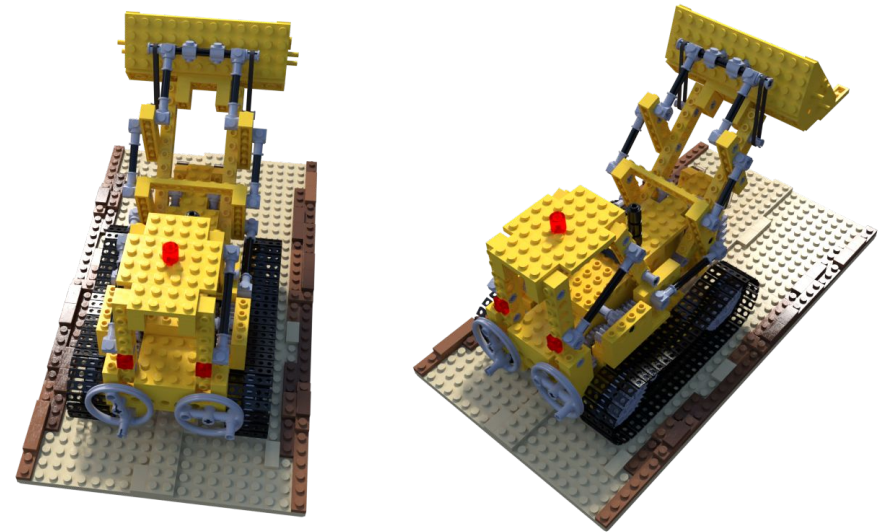
DeepSDF. CVPR
2019

Neural Radiance Fields (NeRF) for View Synthesis

Input: Many images of the same scene
(with known camera parameters)



Output: Images showing the scene from novel viewpoints



Shape Representations

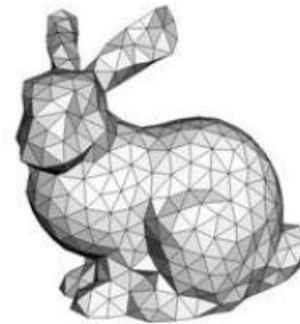
Explicit

Implicit (Eulerian)

Non-parametric



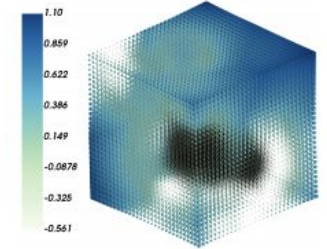
Points



Meshes

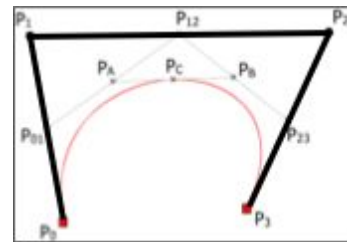


Voxels

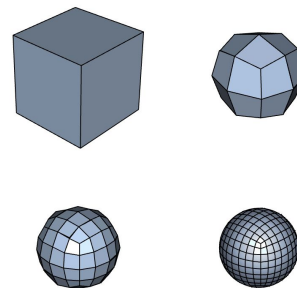


Level Sets

Parametric



Splines

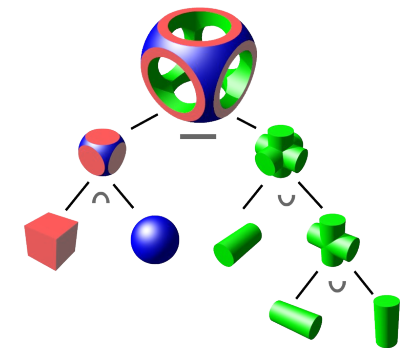


Subdivision Surfaces



$$x^2 + y^2 + z^2 = 1$$

Algebraic Surfaces



Constructive Solid Geometry

Next:

Human-Centered Artificial Intelligence