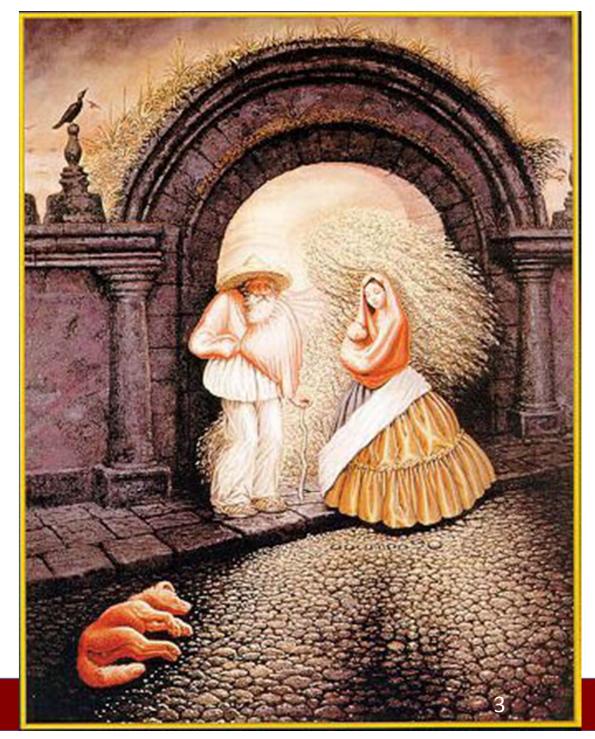


Fei-Fei Li Lecture 5 - 1 6-Oct-11

What we will learn today

- Segmentation and grouping
 - Gestalt principles
- Segmentation as clustering
 - K-means
 - Feature space
- Probabilistic clustering (Problem Set 1 (Q3))
 - Mixture of Gaussians, EM

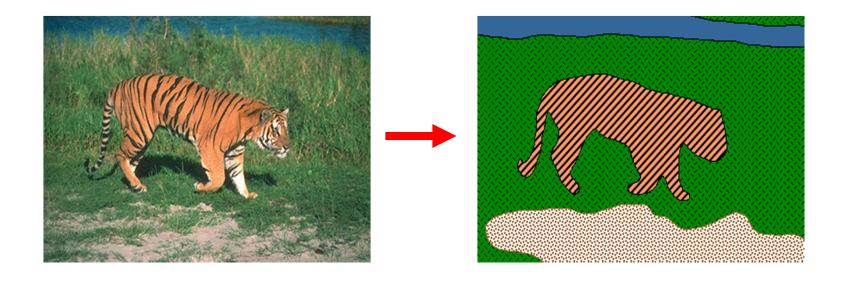
Fei-Fei Li Lecture 5 - 2 6-Oct-11



Fei-Fei Li

Image Segmentation

Goal: identify groups of pixels that go together



Slide credit: Steve Seitz, Kristen Grauman

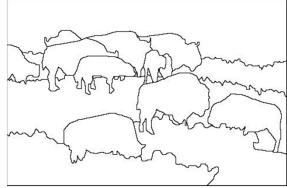
Fei-Fei Li Lecture 5 - 4 6-Oct-11

The Goals of Segmentation

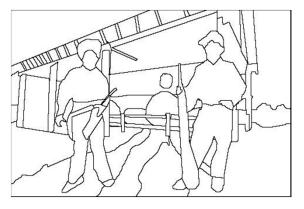
Separate image into coherent "objects"

Image Human segmentation









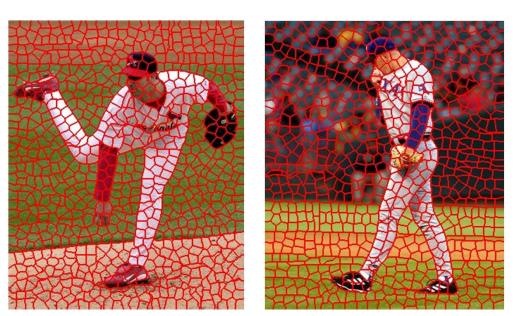
Slide credit: Svetlana Lazebnik

Slide credit: Svetlana Lazebnik

The Goals of Segmentation

- Separate image into coherent "objects"
- Group together similar-looking pixels for efficiency of further processing

"superpixels"



X. Ren and J. Malik. Learning a classification model for segmentation. ICCV 2003.

Fei-Fei Li Lecture 5 - 6 6-Oct-11

Segmentation

- Compact representation for image data in terms of a set of components
- Components share "common" visual properties
- Properties can be defined at different level of abstractions

Fei-Fei Li Lecture 5 - 7 6-Oct-11

General ideas

This lecture (#5)

- Tokens
 - whatever we need to group (pixels, points, surface elements, etc., etc.)
- Bottom up segmentation
 - tokens belong together because they are locally coherent
- Top down segmentation
 - tokens belong together because they lie on the same visual entity (object, scene...)
- > These two are not mutually exclusive

Fei-Fei Li Lecture 5 - 8 6-Oct-11

What is Segmentation?

Clustering image elements that "belong together"

Partitioning

Divide into regions/sequences with coherent internal properties

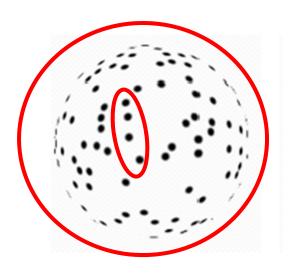
- Grouping

Identify sets of coherent tokens in image

Slide credit: Christopher Rasmussen

Fei-Fei Li Lecture 5 - 9 6-Oct-11

What is Segmentation?



Why do these tokens belong together?

Fei-Fei Li Lecture 5 - 10 6-Oct-11

Basic ideas of grouping in human vision

- Gestalt properties
- Figure-ground discrimination

Fei-Fei Li Lecture 5 - 11 6-Oct-11

Examples of Grouping in Vision



Determining image regions

Shot 1 Shot 2 Shot 3 Shot 4 Shot 5 Shot 6 Shot 7 Shot 8

Shot 9	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15		
Shot 9	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15		
Shot 9	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15		
Shot 9	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15		
Shot 9	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15		
Shot 9	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15		
Shot 9	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15		
Shot 9	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15		
Shot 9	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15		
Shot 9	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15		
Shot 9	Shot 10	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15	Shot 15
Shot 9	Shot 10	Shot 10	Shot 11	Shot 12	Shot 13	Shot 14	Shot 15	Shot 15

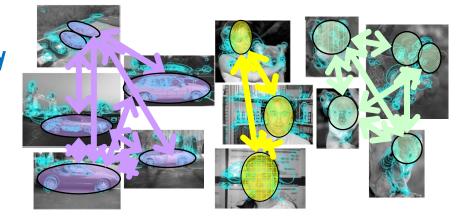
Grouping video frames into shots



Figure-ground

What things should be grouped?

What cues indicate groups?



Object-level grouping

Slide credit: Kristen Grauman

Fei-Fei Li Lecture 5 - 12 6-Oct-11

Similarity





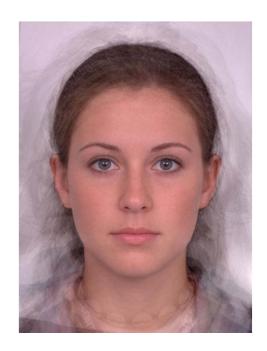






Fei-Fei Li Lecture 5 - 13 6-Oct-11

Symmetry









Slide credit: Kristen Grauman

Common Fate





Image credit: Arthus-Bertrand (via F. Durand)

Slide credit: Kristen Grauman

Fei-Fei Li Lecture 5 - 15 6-Oct-11

Proximity

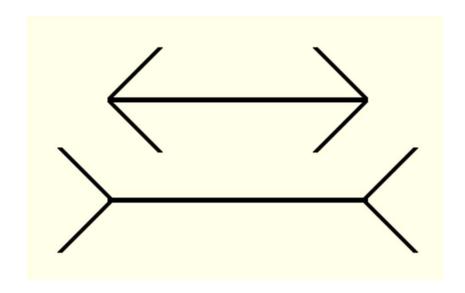




Slide credit: Kristen Grauman

Fei-Fei Li Lecture 5 - 16 6-Oct-11

Muller-Lyer Illusion



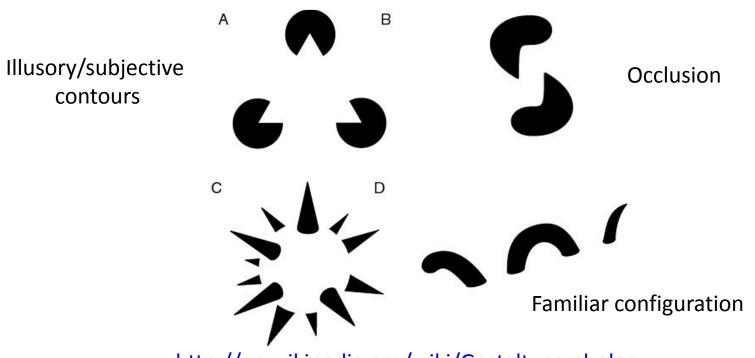
 Gestalt principle: grouping is key to visual perception.

Fei-Fei Li Lecture 5 - 17 6-Oct-11

Slide credit: Svetlana Lazebnik

The Gestalt School

- Grouping is key to visual perception
- Elements in a collection can have properties that result from relationships
 - "The whole is greater than the sum of its parts"



http://en.wikipedia.org/wiki/Gestalt_psychology

Fei-Fei Li Lecture 5 - 18 6-Oct-11

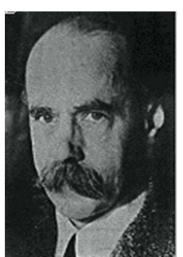
Gestalt Theory

- Gestalt: whole or group
 - Whole is greater than sum of its parts
 - Relationships among parts can yield new properties/features
- Psychologists identified series of factors that predispose set of elements to be grouped (by human visual system)

"I stand at the window and see a house, trees, sky.
Theoretically I might say there were 327 brightnesses
and nuances of colour. Do I have "327"? No. I have sky, house,
and trees."

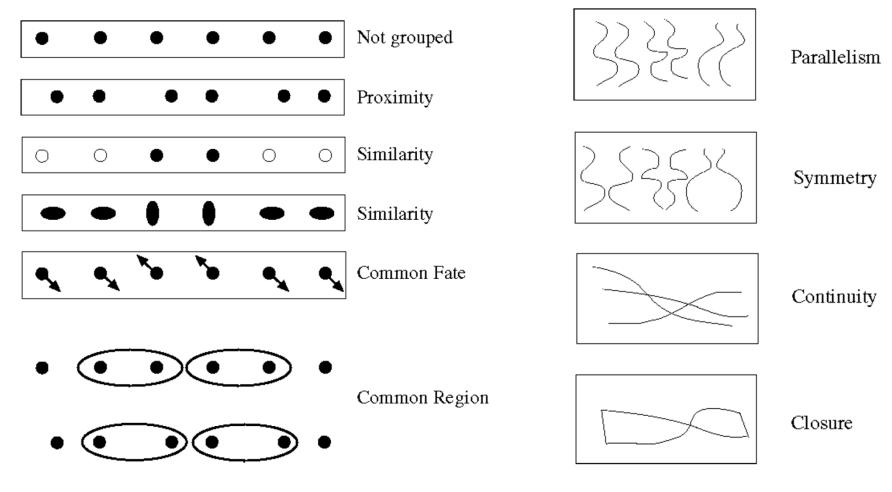
Max Wertheimer (1880-1943)

Untersuchungen zur Lehre von der Gestalt, Psychologische Forschung, Vol. 4, pp. 301-350, 1923 http://psy.ed.asu.edu/~classics/Wertheimer/Forms/forms.htm



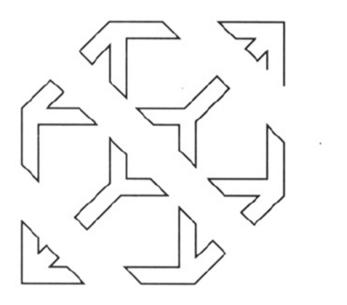
Fei-Fei Li Lecture 5 - 19 6-Oct-11

Gestalt Factors

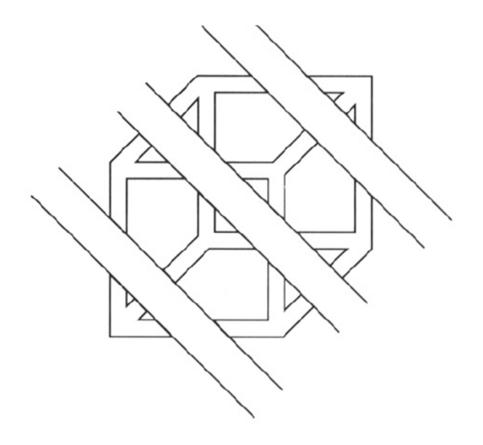


• These factors make intuitive sense, but are very difficult to translate into algorithms.

Image source: Forsyth & Ponce



Fei-Fei Li Lecture 5 - 21 6-Oct-11



Continuity, explanation by occlusion

Fei-Fei Li Lecture 5 - 22 6-Oct-11



Image source: Forsyth & Ponce

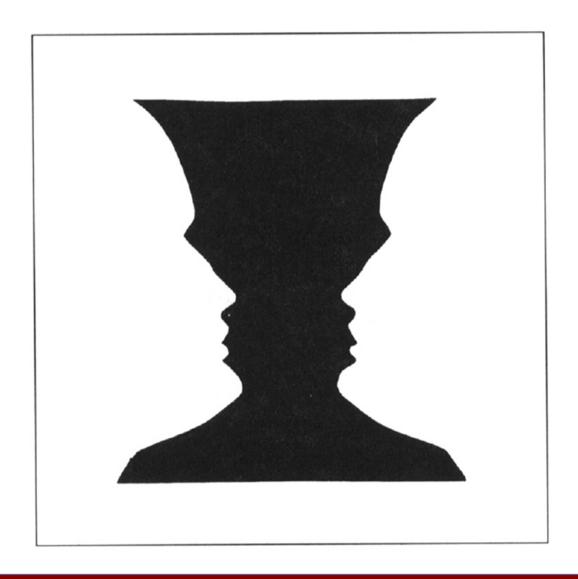
Fei-Fei Li Lecture 5 - 23 6-Oct-11



Image source: Forsyth & Ponce

Fei-Fei Li Lecture 5 - 24 6-Oct-11

Figure-Ground Discrimination



Fei-Fei Li Lecture 5 - 25 6-Oct-11

The Ultimate Gestalt?



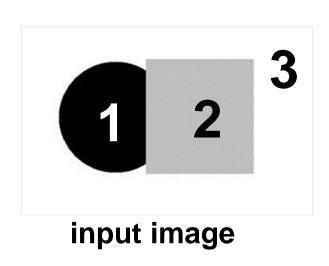
Fei-Fei Li Lecture 5 - 26 6-Oct-11

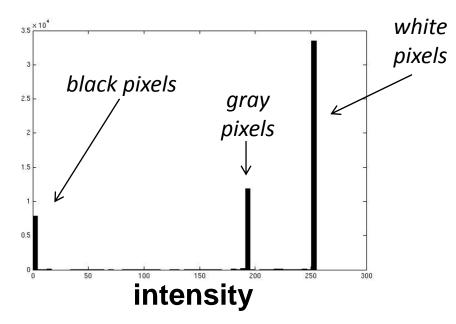
What we will learn today

- Segmentation and grouping
 - Gestalt principles
- Segmentation as clustering
 - K-means
 - Feature space
- Probabilistic clustering
 - Mixture of Gaussians, EM
- Model-free clustering
 - Mean-shift

Fei-Fei Li Lecture 5 - 27 6-Oct-11

Image Segmentation: Toy Example

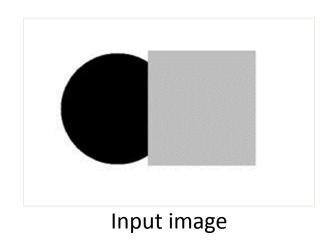


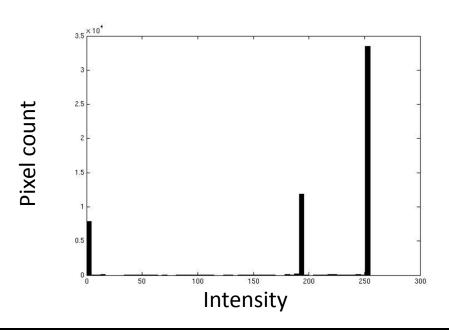


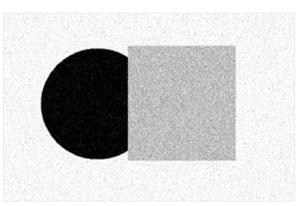
- These intensities define the three groups.
- We could label every pixel in the image according to which of these primary intensities it is.
 - i.e., segment the image based on the intensity feature.
- What if the image isn't quite so simple?

Slide credit: Kristen Grauman

Fei-Fei Li Lecture 5 - 28 6-Oct-11

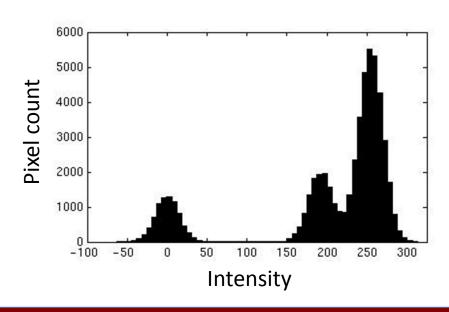




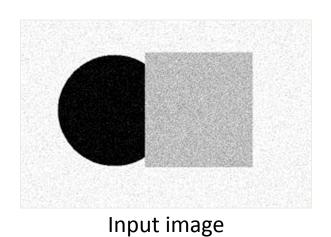


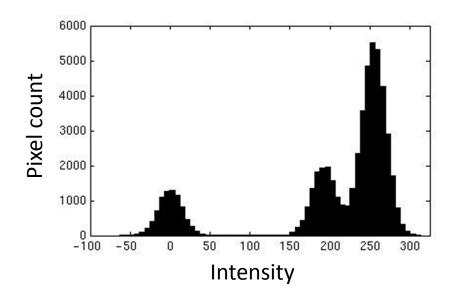
Input image

Slide credit: Kristen Grauman



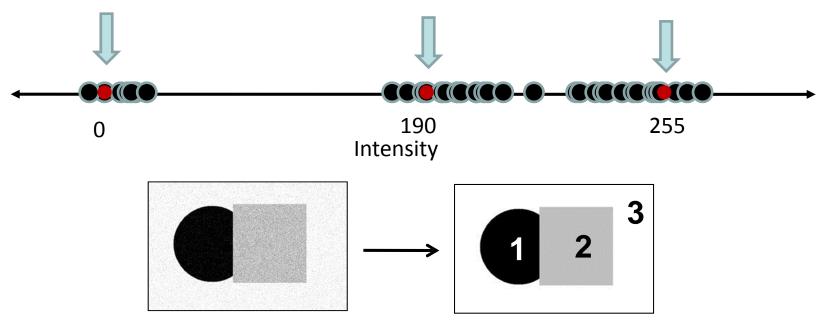
Fei-Fei Li Lecture 5 - 29 6-Oct-11





- Now how to determine the three main intensities that define our groups?
- We need to cluster.

Slide credit: Kristen Grauman



- Goal: choose three "centers" as the representative intensities, and label every pixel according to which of these centers it is nearest to.
- Best cluster centers are those that minimize Sum of Square Distance (SSD) between all points and their nearest cluster center c_i :

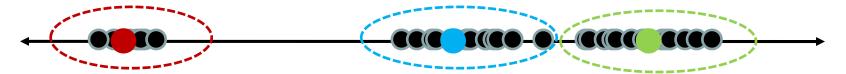
$$SSD = \sum_{clusters \ i} \sum_{p \in cluster \ i} ||p - c_i||^2$$

Fei-Fei Li Lecture 5 - 31 6-Oct-11

Slide credit: Kristen Grauman

Clustering

- With this objective, it is a "chicken and egg" problem:
 - If we knew the cluster centers, we could allocate points to groups by assigning each to its closest center.



 If we knew the group memberships, we could get the centers by computing the mean per group.



Fei-Fei Li Lecture 5 - 32 6-Oct-11

Slide credit: Steve Seitz

K-Means Clustering

- Basic idea: randomly initialize the k cluster centers, and iterate between the two steps we just saw.
 - 1. Randomly initialize the cluster centers, c_1 , ..., c_K
 - 2. Given cluster centers, determine points in each cluster
 - For each point p, find the closest c_i. Put p into cluster i
 - 3. Given points in each cluster, solve for ci
 - Set c_i to be the mean of points in cluster i
 - 4. If c_i have changed, repeat Step 2



- Will always converge to some solution
- Can be a "local minimum"
 - Does not always find the global minimum of objective function:

$$SSD = \sum_{clusters \ i} \sum_{p \in cluster \ i} ||p - c_i||^2$$

Segmentation as Clustering



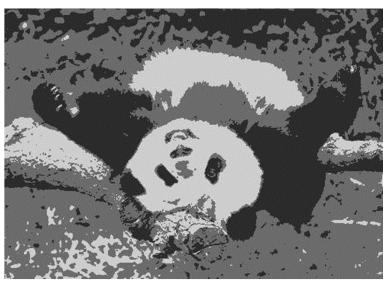
K=2



```
img_as_col = double(im(:));
cluster_membs = kmeans(img_as_col, K);

labelim = zeros(size(im));
for i=1:k
   inds = find(cluster_membs==i);
   meanval = mean(img_as_column(inds));
   labelim(inds) = meanval;
end
```

Slide credit: Kristen Grauman



Fei-Fei Li Lecture 5 - 34 6-Oct-11

K-Means Clustering

• Java demo:

http://home.dei.polimi.it/matteucc/Clustering/tutorial html/AppletKM.html

Fei-Fei Li Lecture 5 - 35 6-Oct-11

K-Means++

- Can we prevent arbitrarily bad local minima?
- 1. Randomly choose first center.
- 2. Pick new center with prob. proportional to $||p-c_i||^2$
 - (Contribution of p to total error)
- 3. Repeat until *k* centers.
- Expected error = O(log k) * optimal

Arthur & Vassilvitskii 2007

Slide credit: Steve Seitz

Fei-Fei Li Lecture 5 - 36 6-Oct-11

Feature Space

- Depending on what we choose as the feature space, we can group pixels in different ways.
- Grouping pixels based on intensity similarity





Feature space: intensity value (1D)

Slide credit: Kristen Grauman

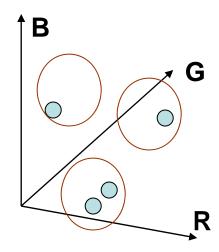
Fei-Fei Li Lecture 5 - 37 6-Oct-11

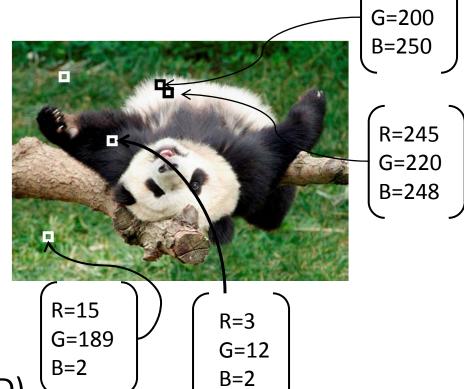
Feature Space

Depending on what we choose as the feature space, we can

group pixels in different ways.

 Grouping pixels based on color similarity





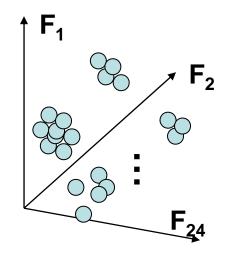
R=255

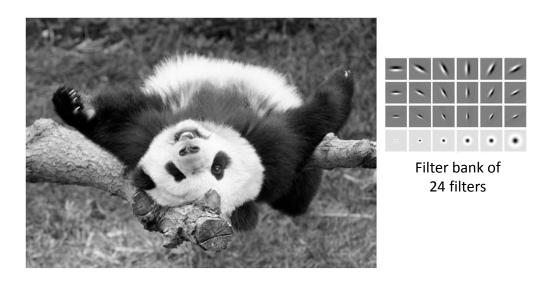
Feature space: color value (3D)

Slide credit: Kristen Grauman

Feature Space

- Depending on what we choose as the feature space, we can group pixels in different ways.
- Grouping pixels based on texture similarity





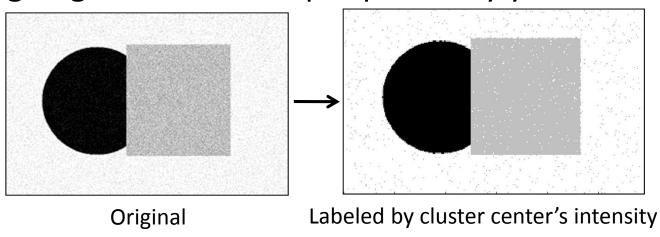
• Feature space: filter bank responses (e.g., 24D)

Slide credit: Kristen Grauman

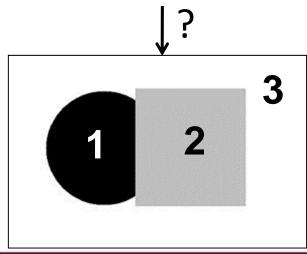
Fei-Fei Li Lecture 5 - 39 6-Oct-11

Smoothing Out Cluster Assignments

Assigning a cluster label per pixel may yield outliers:



 How can we ensure they are spatially smooth?

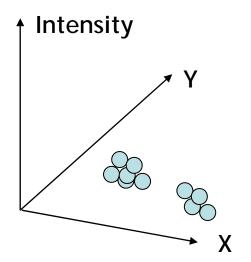


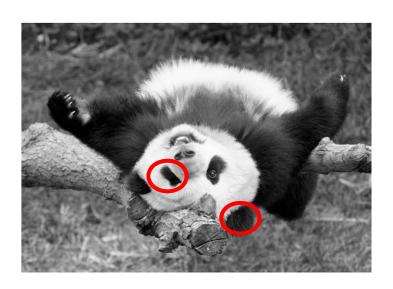
Slide credit: Kristen Grauman

Fei-Fei Li Lecture 5 - 40 6-Oct-11

Segmentation as Clustering

- Depending on what we choose as the feature space, we can group pixels in different ways.
- Grouping pixels based on intensity+position similarity



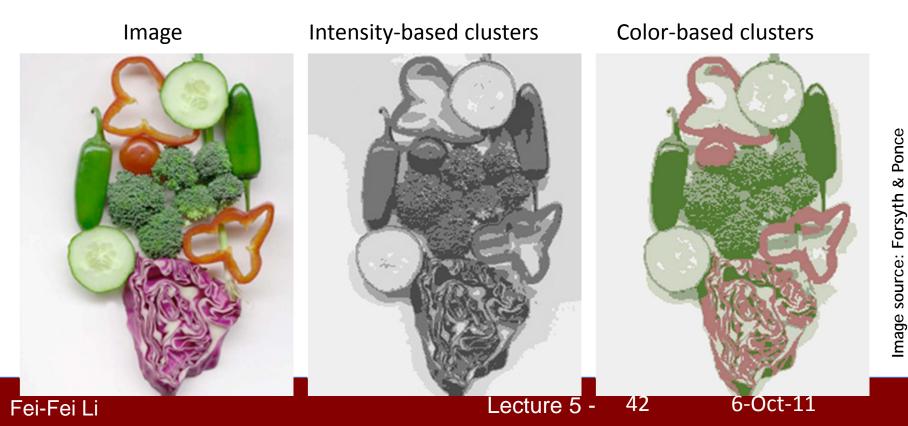


 \Rightarrow Way to encode both *similarity* and *proximity*.

Slide credit: Kristen Grauman

Fei-Fei Li Lecture 5 - 41 6-Oct-11

- K-means clustering based on intensity or color is essentially vector quantization of the image attributes
 - Clusters don't have to be spatially coherent



- K-means clustering based on intensity or color is essentially vector quantization of the image attributes
 - Clusters don't have to be spatially coherent
- Clustering based on (r,g,b,x,y) values enforces more spatial coherence



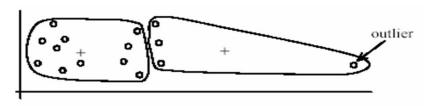
Image source: Forsyth & Ponce

43

Summary K-Means

Pros

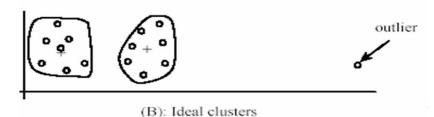
- Simple, fast to compute
- Converges to local minimum of within-cluster squared error



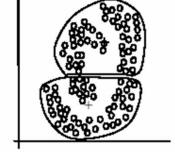
(A): Undesirable clusters

Cons/issues

- Setting k?
- Sensitive to initial centers
- Sensitive to outliers
- Detects spherical clusters only
- Assuming means can be computed



2000 Sept. S



(A): Two natural clusters

(B): k-means clusters

Slide credit: Kristen Grauman

What we will learn today

- Segmentation and grouping
 - Gestalt principles
- Segmentation as clustering
 - K-means
 - Feature space
- Probabilistic clustering (Problem Set 1 (Q3))
 - Mixture of Gaussians, EM

Fei-Fei Li Lecture 5 - 45 6-Oct-11

Probabilistic Clustering

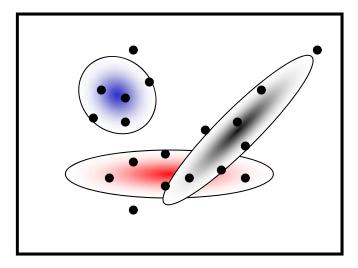
- Basic questions
 - What's the probability that a point x is in cluster m?
 - What's the shape of each cluster?
- K-means doesn't answer these questions.
- Basic idea
 - Instead of treating the data as a bunch of points, assume that they are all generated by sampling a continuous function.
 - This function is called a generative model.
 - Defined by a vector of parameters θ

Slide credit: Steve Seitz

Fei-Fei Li Lecture 5 - 46 6-Oct-11

Slide credit: Steve Seitz

Mixture of Gaussians



- One generative model is a mixture of Gaussians (MoG)
 - K Gaussian blobs with means μ_b covariance matrices V_b , dimension d

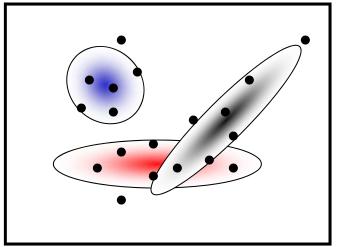
• Blob *b* defined by:
$$P(x|\mu_b, V_b) = \frac{1}{\sqrt{(2\pi)^d |V_b|}} e^{-\frac{1}{2}(x-\mu_b)^T V_b^{-1}(x-\mu_b)}$$

- Blob b is selected with probability α_b
- The likelihood of observing x is a weighted mixture of Gaussians

$$P(x|\theta) = \sum_{b=1}^{K} \alpha_b P(x|\theta_b)$$
, $\theta = [\mu_1, \dots, \mu_n, V_1, \dots, V_n]$

Slide credit: Steve Seitz

Expectation Maximization (EM)



- Goal
 - Find blob parameters θ that maximize the likelihood function:

$$P(data|\theta) = \prod_{x} P(x|\theta)$$

- Approach:
 - 1. E-step: given current guess of blobs, compute ownership of each point
 - 2. M-step: given ownership probabilities, update blobs to maximize likelihood function
 - 3. Repeat until convergence

EM Details



- E-step
 - Compute probability that point x is in blob b, given current guess of θ

$$P(b|x, \mu_b, V_b) = \frac{\alpha_b P(x|\mu_b, V_b)}{\sum_{i=1}^K \alpha_i P(x|\mu_i, V_i)}$$

- M-step
 - Compute probability that blob b is selected

$$\alpha_b^{new} = \frac{1}{N} \sum_{i=1}^{N} P(b|x_i, \mu_b, V_b) \qquad (N \text{ data points})$$

Mean of blob b

$$\mu_b^{new} = \frac{\sum_{i=1}^{N} x_i P(b|x_i, \mu_b, V_b)}{\sum_{i=1}^{N} P(b|x_i, \mu_b, V_b)}$$

Covariance of blob b

$$V_b^{new} = \frac{\sum_{i=1}^{N} (x_i - \mu_b^{new})(x_i - \mu_b^{new})^T P(b|x_i, \mu_b, V_b)}{\sum_{i=1}^{N} P(b|x_i, \mu_b, V_b)}$$

Slide credit: Steve Seitz

Slide credit: Steve Seitz

Applications of EM

- Turns out this is useful for all sorts of problems
 - Any clustering problem
 - Any model estimation problem
 - Missing data problems
 - Finding outliers
 - Segmentation problems
 - Segmentation based on color
 - Segmentation based on motion
 - Foreground/background separation
 - **–** ...
- EM demo
 - http://lcn.epfl.ch/tutorial/english/gaussian/html/index.html

Fei-Fei Li Lecture 5 - 50 6-Oct-11

Segmentation with EM

Original image



EM segmentation results

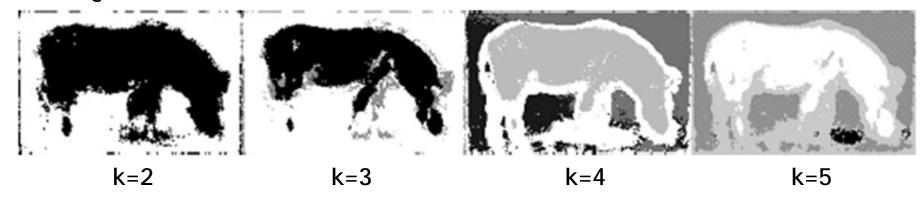


Image source: Serge Belongie

Fei-Fei Li Lecture 5 - 51 6-Oct-11

Summary: Mixtures of Gaussians, EM

Pros

- Probabilistic interpretation
- Soft assignments between data points and clusters
- Generative model, can predict novel data points
- Relatively compact storage

Cons

- Local minima
- Initialization
 - Often a good idea to start with some k-means iterations.
- Need to know number of components
 - Solutions: model selection (AIC, BIC), Dirichlet process mixture
- Need to choose generative model
- Numerical problems are often a nuisance

Fei-Fei Li Lecture 5 - 52 6-Oct-11

What we have learned today

- Segmentation and grouping
 - Gestalt principles
- Segmentation as clustering
 - K-means
 - Feature space
- Probabilistic clustering (Problem Set 1 (Q3))
 - Mixture of Gaussians, EM

Fei-Fei Li Lecture 5 - 53 6-Oct-11