

# Lecture 7

## Multi-view geometry

- The SFM problem
- Affine SFM
- Perspective SFM
- Self-calibration



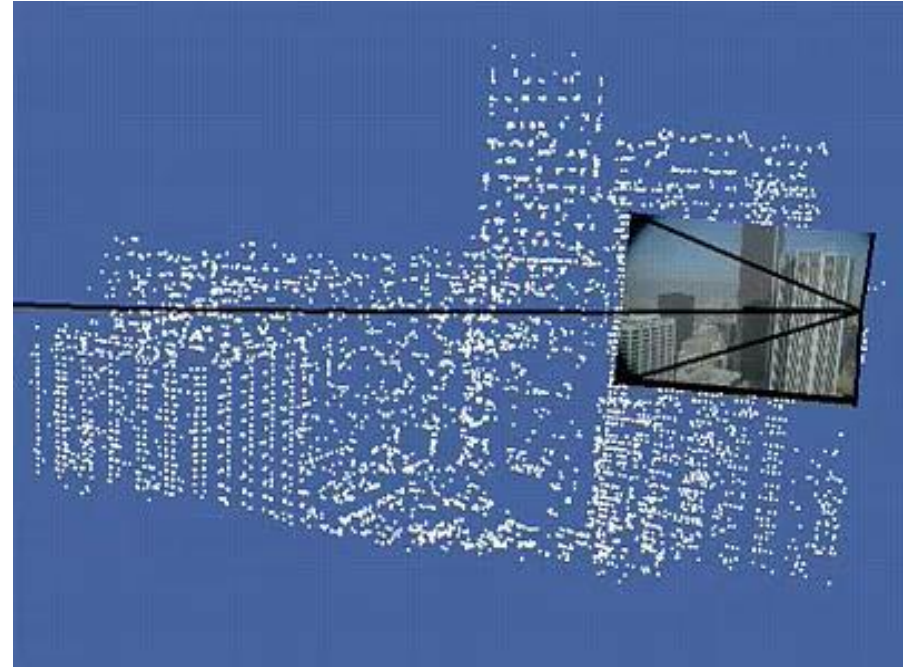
### Reading:

[HZ] Chapters: 10 “3D reconstruction of cameras and structure”,  
18 “N-view computational methods”,  
19 “Auto-calibration”

[FP] Chapter 13: “projective structure from motion”<sup>13</sup>

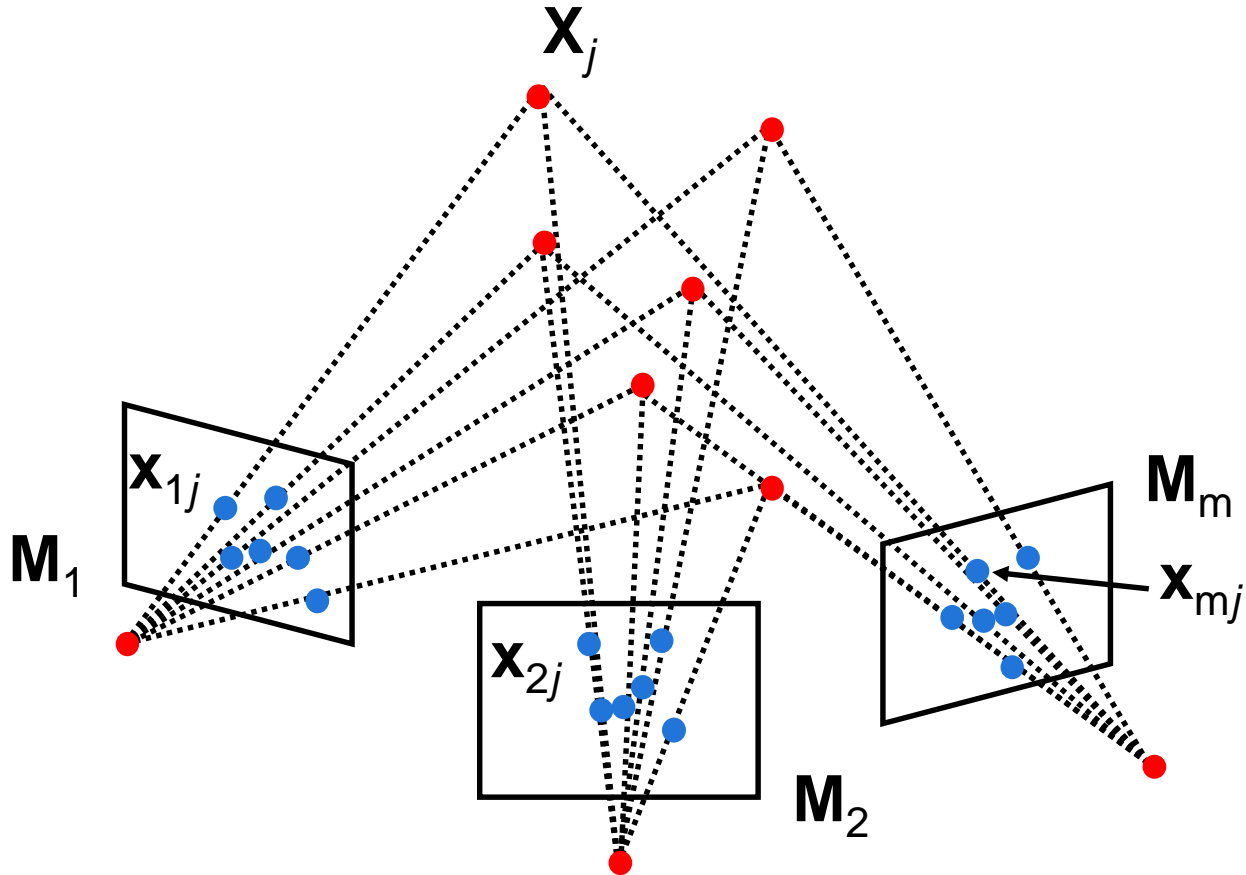
[Szelisky] Chapter 7 “Structure from motion”

# Structure from motion problem



Courtesy of Oxford **Visual Geometry Group**

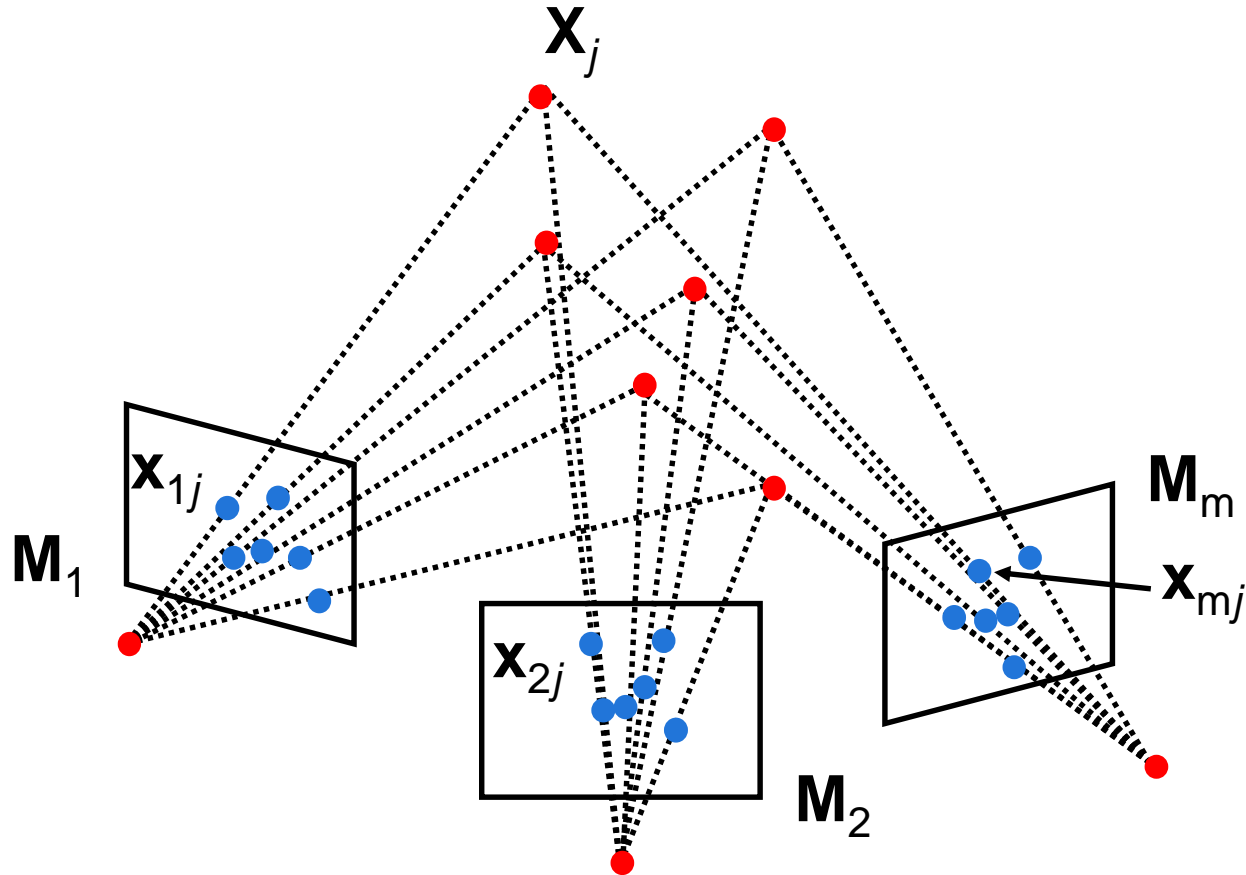
# Structure from motion problem



Given  $m$  images of  $n$  fixed 3D points

$$\bullet \mathbf{x}_{ij} = \mathbf{M}_i \mathbf{X}_j, \quad i = 1, \dots, m, \quad j = 1, \dots, n$$

# Structure from motion problem



From the  $m \times n$  correspondences  $x_{ij}$ , estimate:

•  $m$  projection matrices  $M_i$

•  $n$  3D points  $X_j$

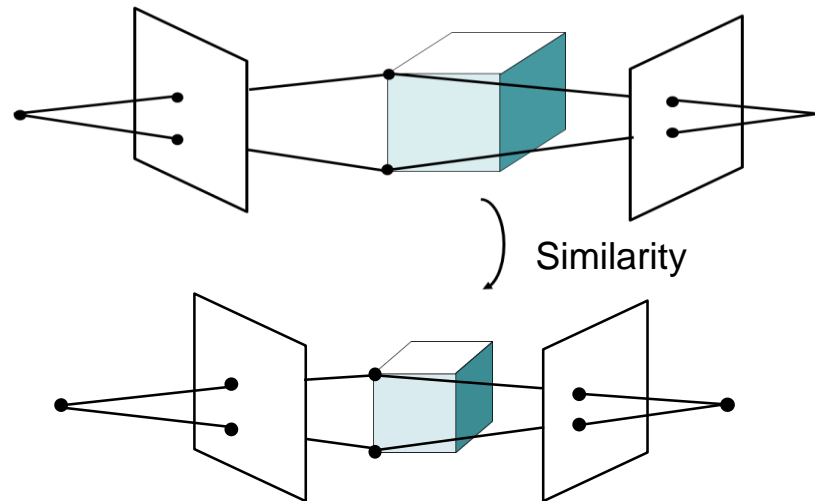
motion

structure



# Similarity Ambiguity

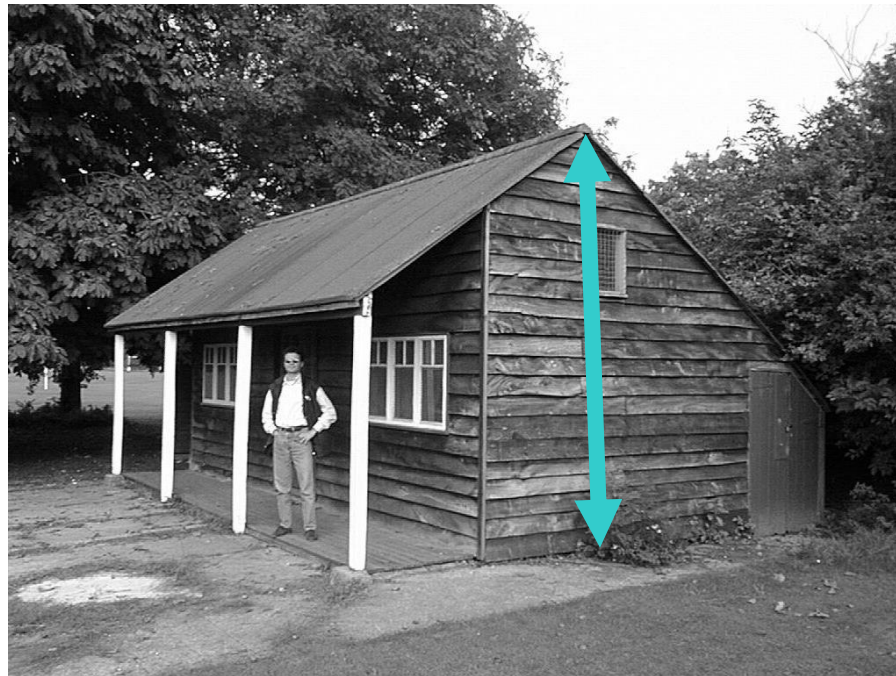
- The scene is determined by the images only up a **similarity transformation** (rotation, translation and scaling)
- This is called **metric reconstruction**



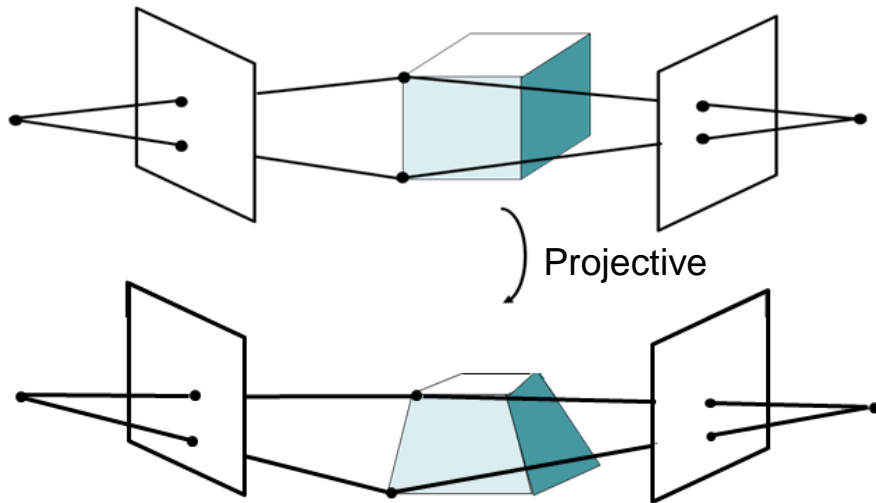
- The ambiguity exists even for (intrinsically) calibrated cameras
- For calibrated cameras, the similarity ambiguity is the **only** ambiguity

# Similarity Ambiguity

- It is impossible based on the images alone to estimate the absolute scale of the scene (i.e. house height)



# Structure from Motion Ambiguities



- In the general case (nothing is known) the ambiguity is expressed by an arbitrary **affine** or **projective transformation**

$$x_j = M_i X_j$$

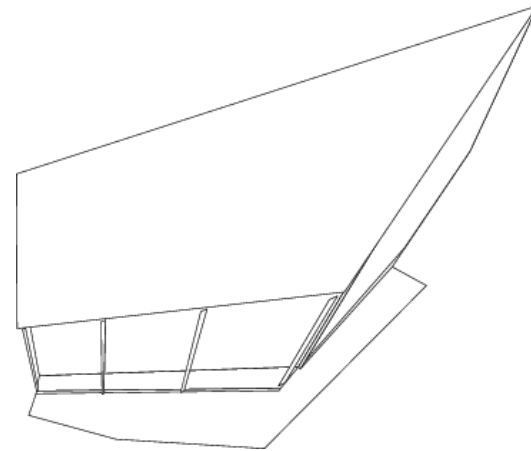
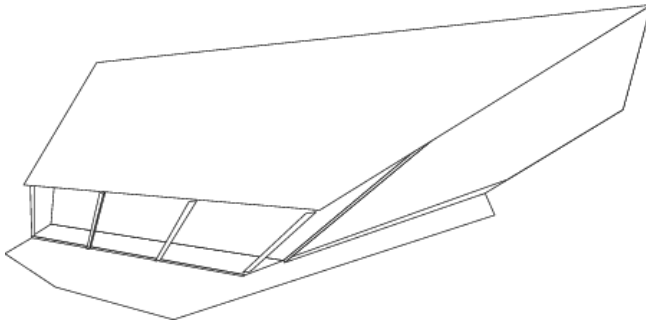
$$M_i = K_i [R_i \quad T_i]$$

$$H X_j$$

$$M_j H^{-1}$$

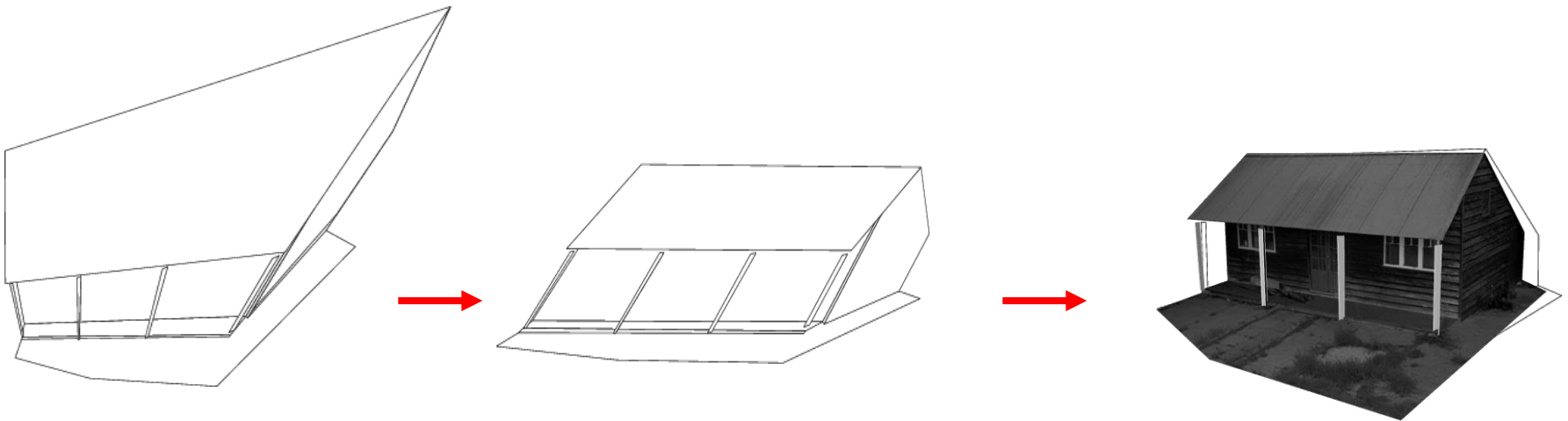
$$x_j = M_i X_j = (M_i H^{-1})(H X_j)$$

# Projective Ambiguity

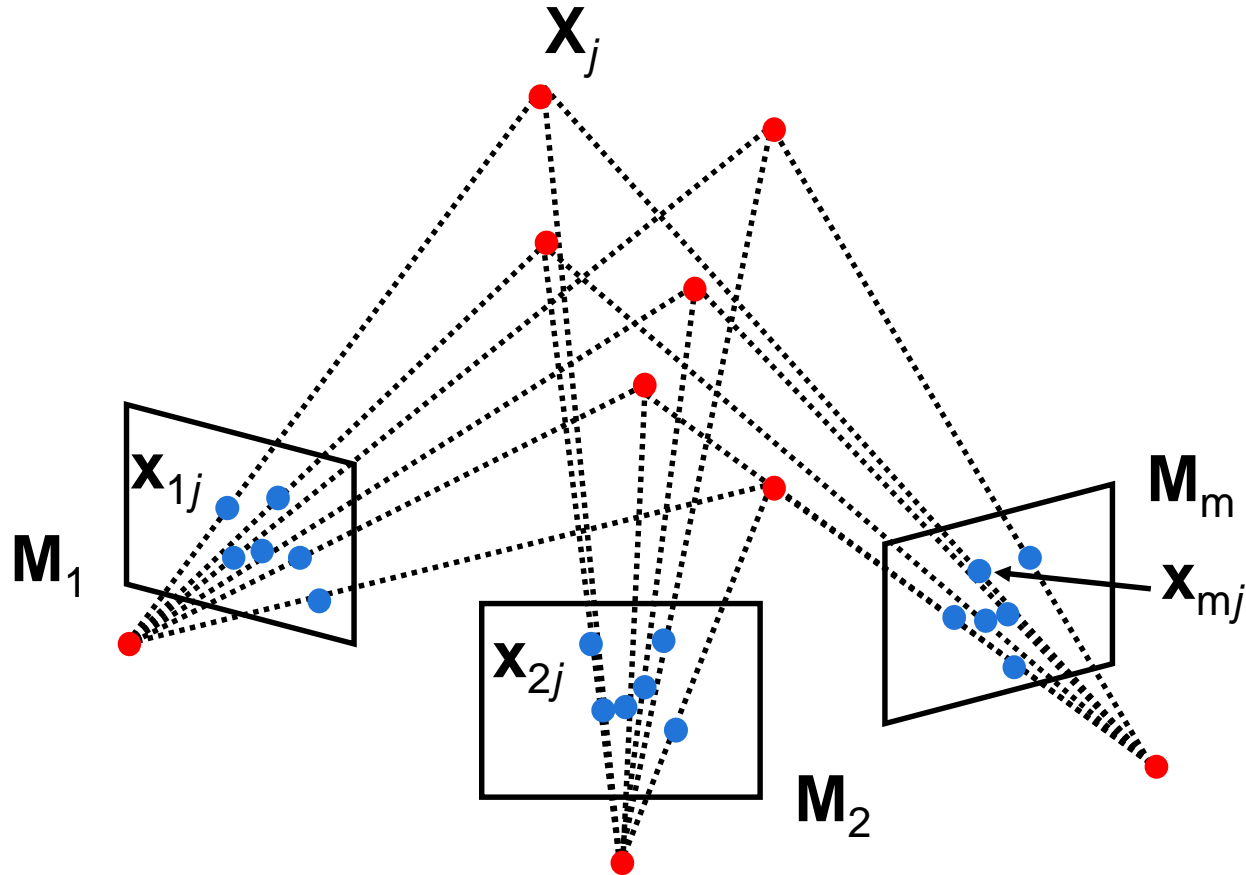


# Metric reconstruction (upgrade)

- The problem of recovering the metric reconstruction from the perspective one is called **self-calibration**
- Stratified reconstruction:
  - from perspective to affine
  - from affine to metric



# Structure from motion problem

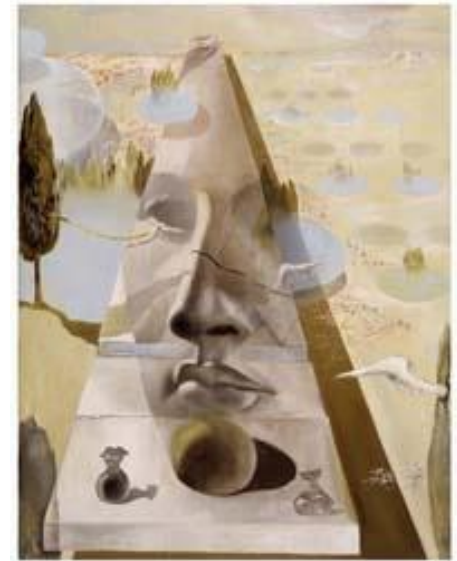


From the  $m \times n$  correspondences  $x_{ij}$ , estimate:

- $m$  projection matrices  $M_i$
- $n$  3D points  $X_j$
- Upgrade to metric reconstruction (self-calibration)

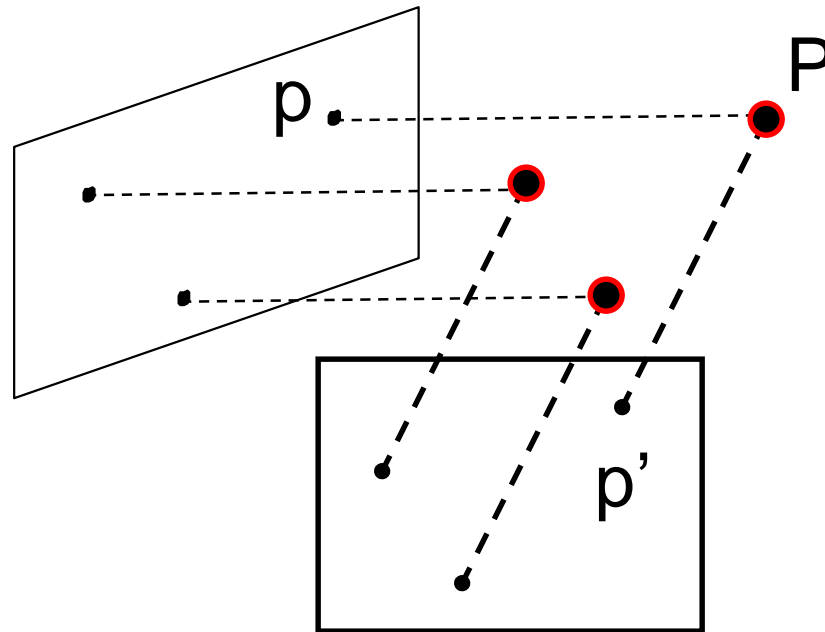
# Lecture 6

## Multi-view geometry



- The SFM problem
- Affine SFM
- Perspective SFM
- Self-calibration

# Affine cameras



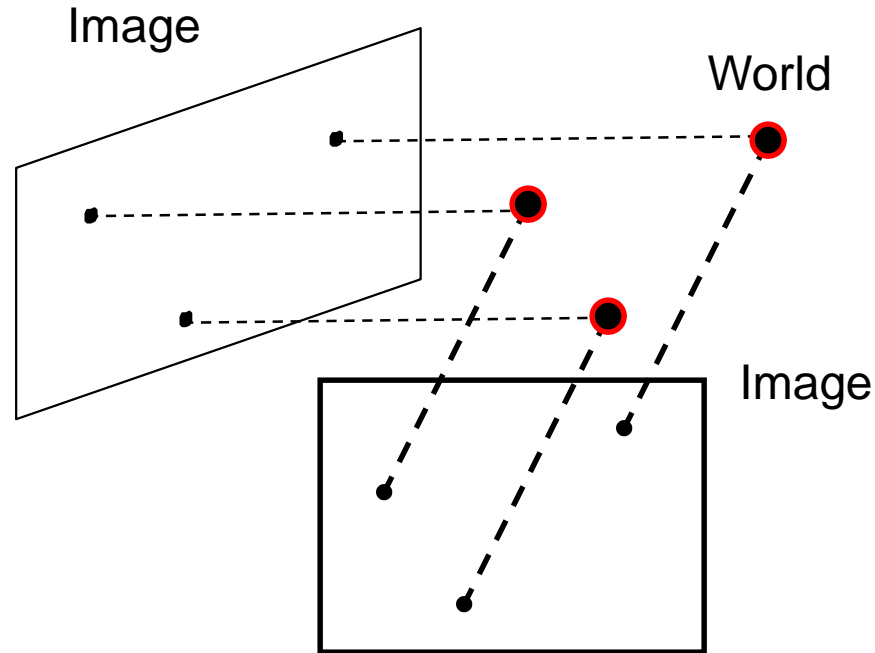
Camera matrix  $M$  for the affine case

$$\mathbf{p} = \begin{pmatrix} u \\ v \end{pmatrix} = \mathbf{A}\mathbf{P} + \mathbf{b} = M \begin{bmatrix} \mathbf{P} \\ 1 \end{bmatrix}; \quad M = \begin{bmatrix} \mathbf{A} & \mathbf{b} \end{bmatrix}$$



# Affine structure from motion

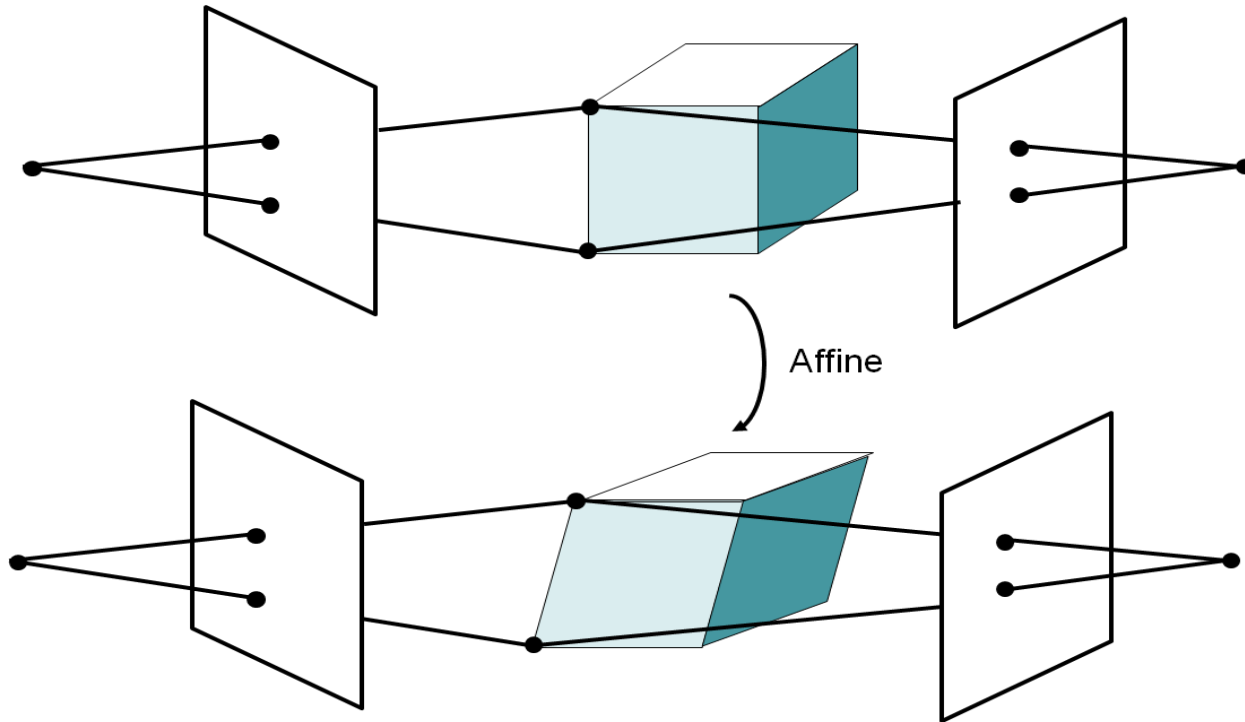
(simpler problem)



From the  $m \times n$  correspondences  $\mathbf{x}_{ij}$ , estimate:

- $m$  projection matrices  $\mathbf{M}_i$  (affine cameras)
- $n$  3D points  $\mathbf{X}_j$
- Upgrade to metric reconstruction

# Affine Ambiguity



$$\mathbf{p} = \mathbf{M} \mathbf{P} = \left( \mathbf{M} \mathbf{Q}_A^{-1} \right) \left( \mathbf{Q}_A \mathbf{P} \right)$$

# The Affine Structure-from-Motion Problem

Given  $m$  images of  $n$  fixed points  $P_j$  ( $=X_i$ ) we can write

$$\mathbf{p}_{ij} = \mathbf{M}_i \begin{bmatrix} \mathbf{P}_j \\ 1 \end{bmatrix} = \mathbf{A}_i \mathbf{P}_j + \mathbf{b}_i \quad \text{for } i = 1, \dots, m \text{ and } j = 1, \dots, n.$$

M of cameras                      N of points

Problem: estimate the  $m$   $2 \times 4$  matrices  $\mathbf{M}_i$  and the  $n$  positions  $\mathbf{P}_j$  from the  $m \times n$  correspondences  $\mathbf{p}_{ij}$ .

How many equations and how many unknowns?

$2m \times n$  equations in  $(8m + 3n - 8)$  unknowns

## Two approaches:

- Algebraic approach (affine epipolar geometry; estimate  $\mathbf{F}$ ; cameras; points)
- Factorization method

# A factorization method – Tomasi & Kanade algorithm

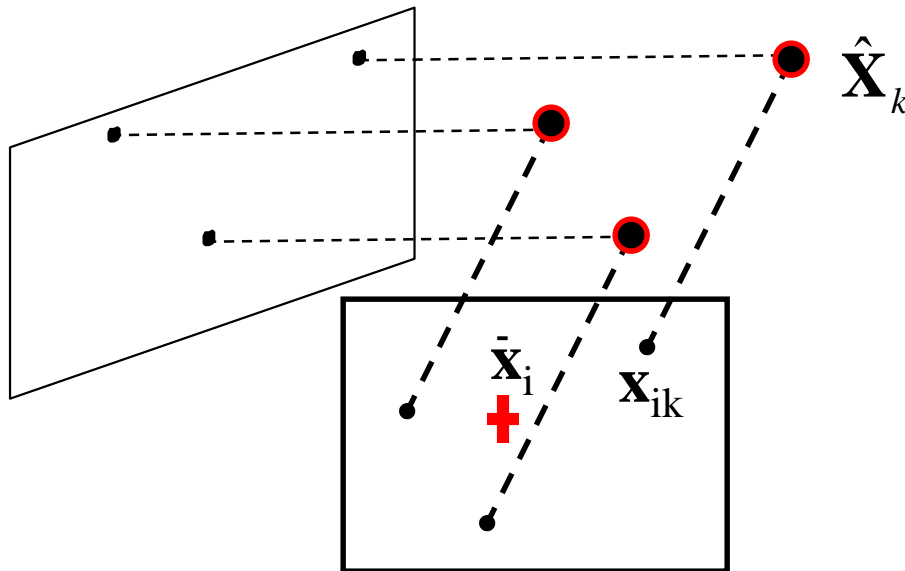
C. Tomasi and T. Kanade. [Shape and motion from image streams under orthography: A factorization method.](#) *IJCV*, 9(2):137-154, November 1992.

- Centering the data
- Factorization

# A factorization method - Centering the data

Centering: subtract the centroid of the image points

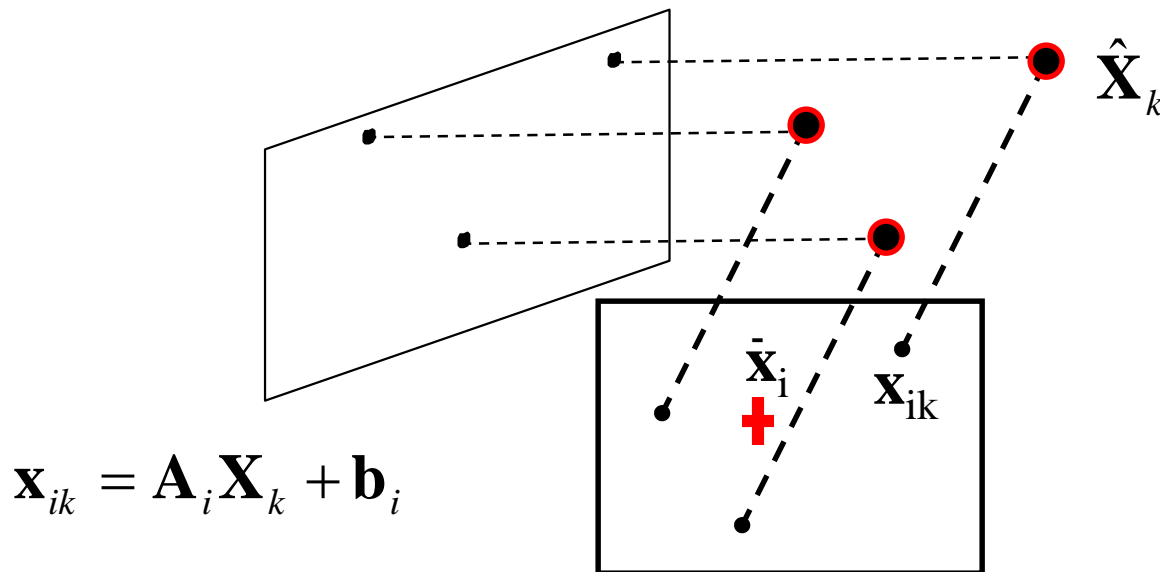
$$\hat{\mathbf{x}}_{ij} = \mathbf{x}_{ij} - \frac{1}{n} \sum_{k=1}^n \mathbf{x}_{ik} \quad \bar{\mathbf{x}}_i$$



# A factorization method - Centering the data

Centering: subtract the centroid of the image points

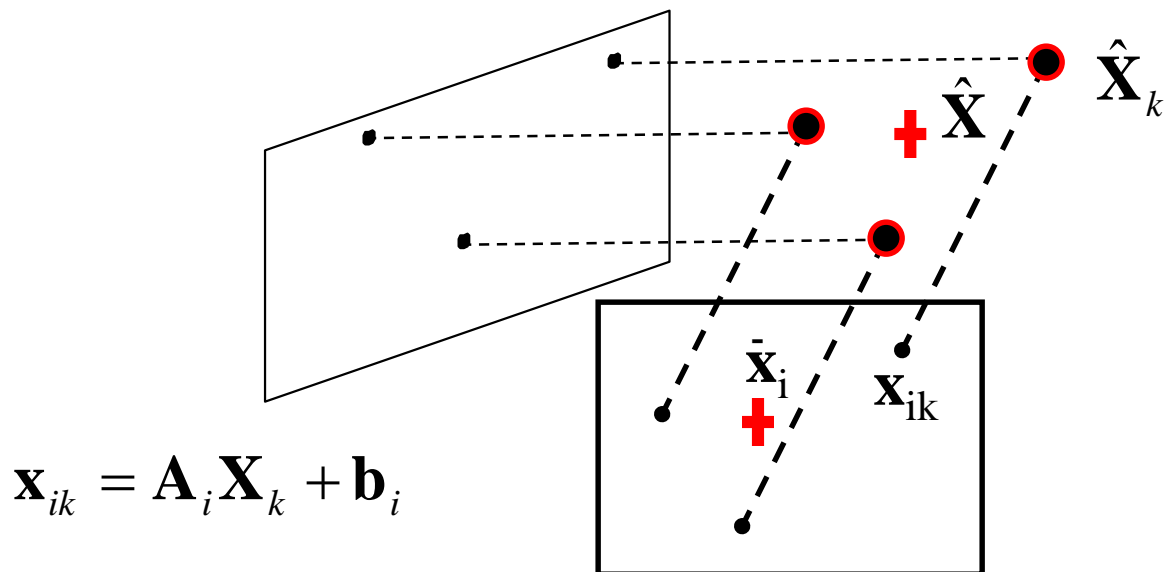
$$\hat{\mathbf{x}}_{ij} = \mathbf{x}_{ij} - \frac{1}{n} \sum_{k=1}^n \mathbf{x}_{ik} = \mathbf{A}_i \mathbf{X}_j + \mathbf{b}_i - \frac{1}{n} \sum_{k=1}^n (\mathbf{A}_i \mathbf{X}_k + \mathbf{b}_i)$$



# A factorization method - Centering the data

Centering: subtract the centroid of the image points

$$\begin{aligned}\hat{\mathbf{x}}_{ij} &= \mathbf{x}_{ij} - \frac{1}{n} \sum_{k=1}^n \mathbf{x}_{ik} = \mathbf{A}_i \mathbf{X}_j + \mathbf{b}_i - \frac{1}{n} \sum_{k=1}^n (\mathbf{A}_i \mathbf{X}_k + \mathbf{b}_i) \\ &= \mathbf{A}_i \left( \mathbf{X}_j - \frac{1}{n} \sum_{k=1}^n \mathbf{X}_k \right) = \mathbf{A}_i \hat{\mathbf{X}}_j\end{aligned}$$



$$\mathbf{x}_{ik} = \mathbf{A}_i \mathbf{X}_k + \mathbf{b}_i$$

# A factorization method - Centering the data

Centering: subtract the centroid of the image points

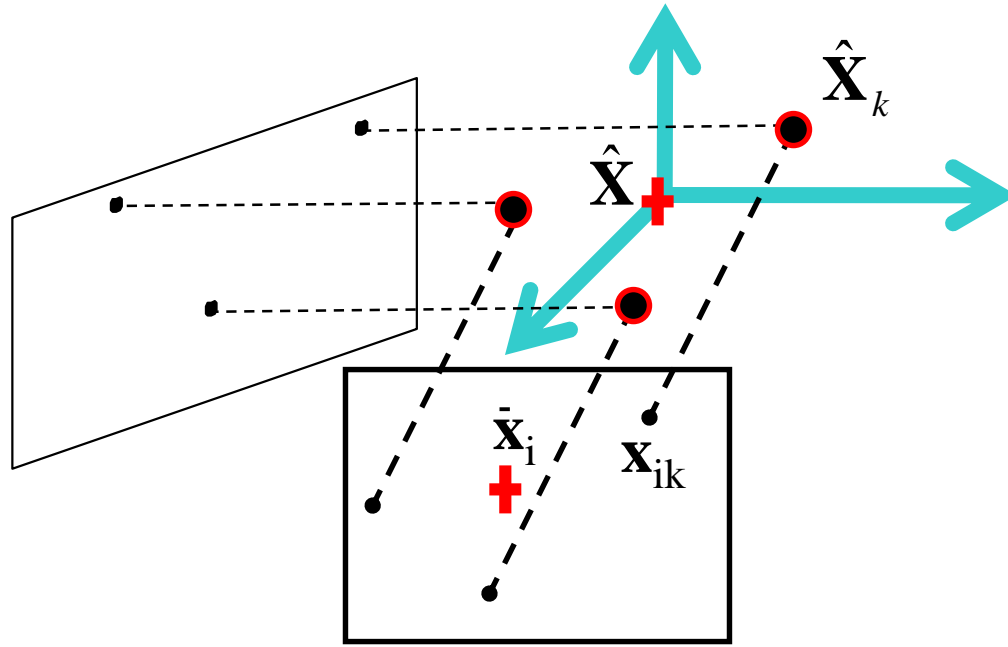
$$\begin{aligned}\hat{\mathbf{x}}_{ij} &= \mathbf{x}_{ij} - \frac{1}{n} \sum_{k=1}^n \mathbf{x}_{ik} = \mathbf{A}_i \mathbf{X}_j + \mathbf{b}_i - \frac{1}{n} \sum_{k=1}^n (\mathbf{A}_i \mathbf{X}_k + \mathbf{b}_i) \\ &= \mathbf{A}_i \left( \mathbf{X}_j - \frac{1}{n} \sum_{k=1}^n \mathbf{X}_k \right) = \mathbf{A}_i \hat{\mathbf{X}}_j\end{aligned}$$

After centering, each normalized point  $\mathbf{x}_{ij}$  is related to the 3D point  $\mathbf{X}_j$  by

$$\hat{\mathbf{x}}_{ij} = \mathbf{A}_i \hat{\mathbf{X}}_j$$



# A factorization method - Centering the data




Centroid of points in 3D = center of the world reference system


$$\hat{\mathbf{X}}_{ij} = \mathbf{A}_i \hat{\mathbf{X}}_j = \mathbf{A}_i \mathbf{X}_j$$

# A factorization method - factorization

Let's create a  $2m \times n$  data (measurement) matrix:

$$\mathbf{D} = \begin{bmatrix} \hat{\mathbf{x}}_{11} & \hat{\mathbf{x}}_{12} & \cdots & \hat{\mathbf{x}}_{1n} \\ \hat{\mathbf{x}}_{21} & \hat{\mathbf{x}}_{22} & \cdots & \hat{\mathbf{x}}_{2n} \\ & & \ddots & \\ \hat{\mathbf{x}}_{m1} & \hat{\mathbf{x}}_{m2} & \cdots & \hat{\mathbf{x}}_{mn} \end{bmatrix}$$

  
points ( $n$ )

  
cameras  
( $2m$ )

# A factorization method - factorization

Let's create a  $2m \times n$  data (measurement) matrix:

$$\mathbf{D} = \begin{bmatrix} \hat{\mathbf{x}}_{11} & \hat{\mathbf{x}}_{12} & \cdots & \hat{\mathbf{x}}_{1n} \\ \hat{\mathbf{x}}_{21} & \hat{\mathbf{x}}_{22} & \cdots & \hat{\mathbf{x}}_{2n} \\ \vdots & \vdots & \ddots & \vdots \\ \hat{\mathbf{x}}_{m1} & \hat{\mathbf{x}}_{m2} & \cdots & \hat{\mathbf{x}}_{mn} \end{bmatrix} = \begin{bmatrix} \mathbf{A}_1 \\ \mathbf{A}_2 \\ \vdots \\ \mathbf{A}_m \end{bmatrix} \begin{bmatrix} \mathbf{X}_1 & \mathbf{X}_2 & \cdots & \mathbf{X}_n \end{bmatrix}$$

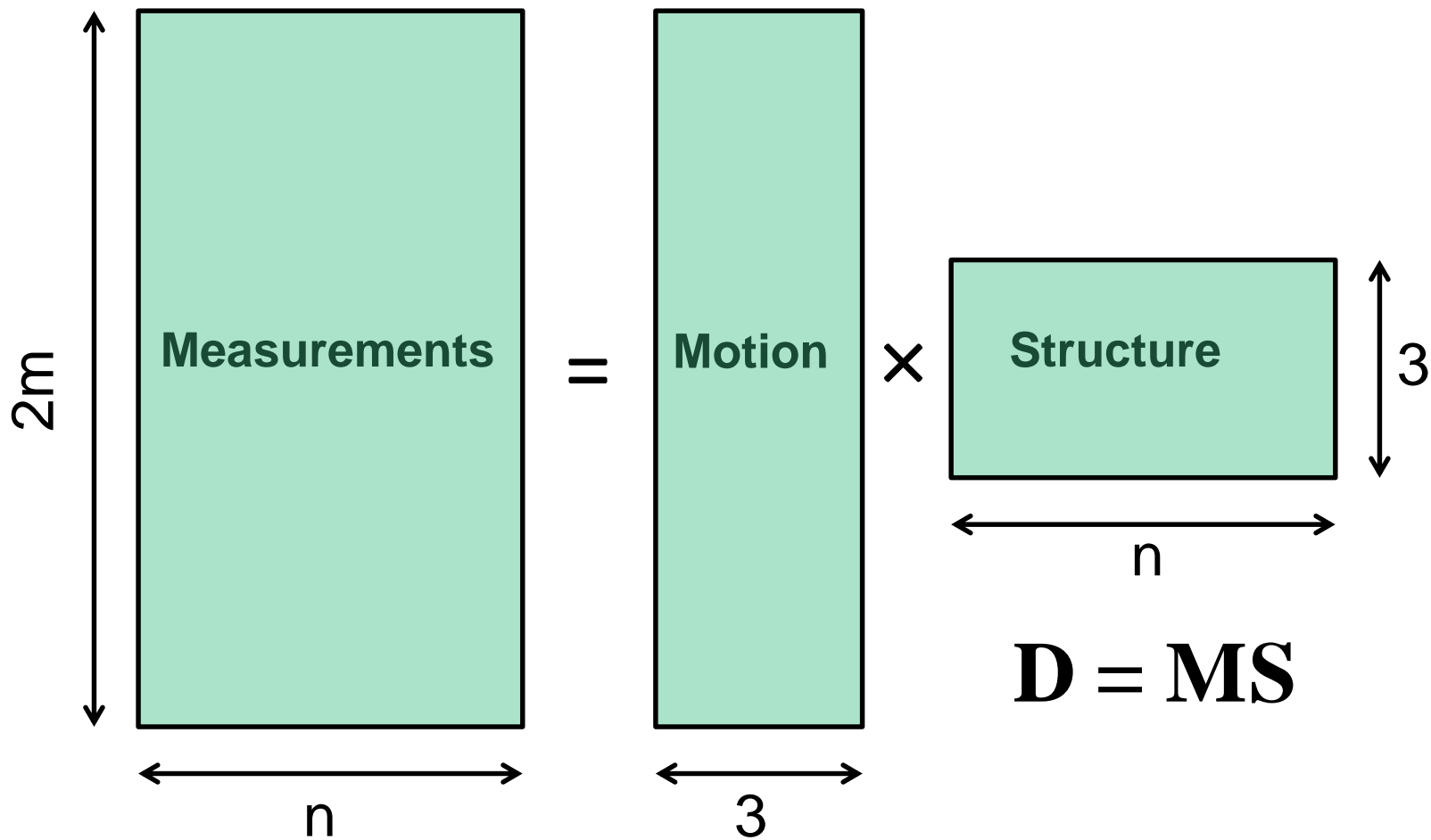
$(2m \times n)$   $\mathbf{M}$   $\mathbf{S}$

$\text{cameras}$   
 $(2m \times 3)$

$\text{points } (3 \times n)$

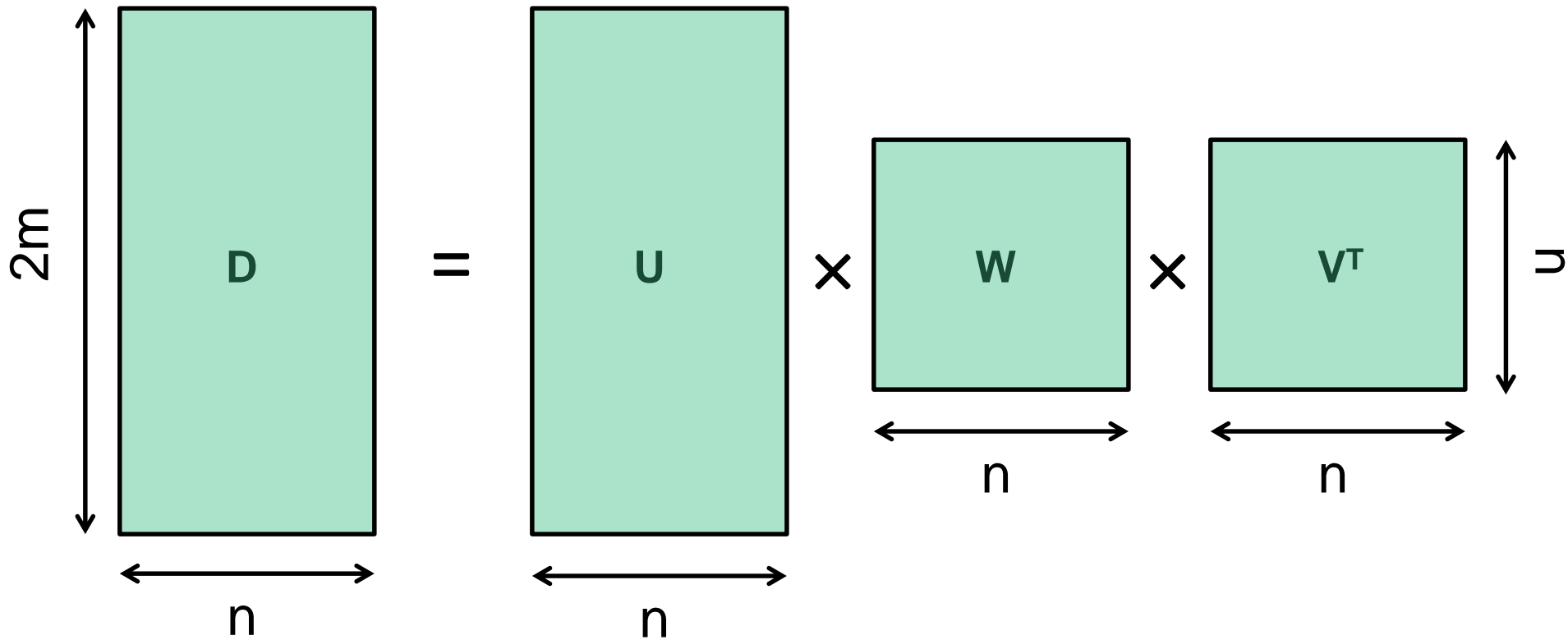
The measurement matrix  $\mathbf{D} = \mathbf{M} \mathbf{S}$  has rank 3  
(it's a product of a  $2m \times 3$  matrix and  $3 \times n$  matrix)

# Factorizing the Measurement Matrix



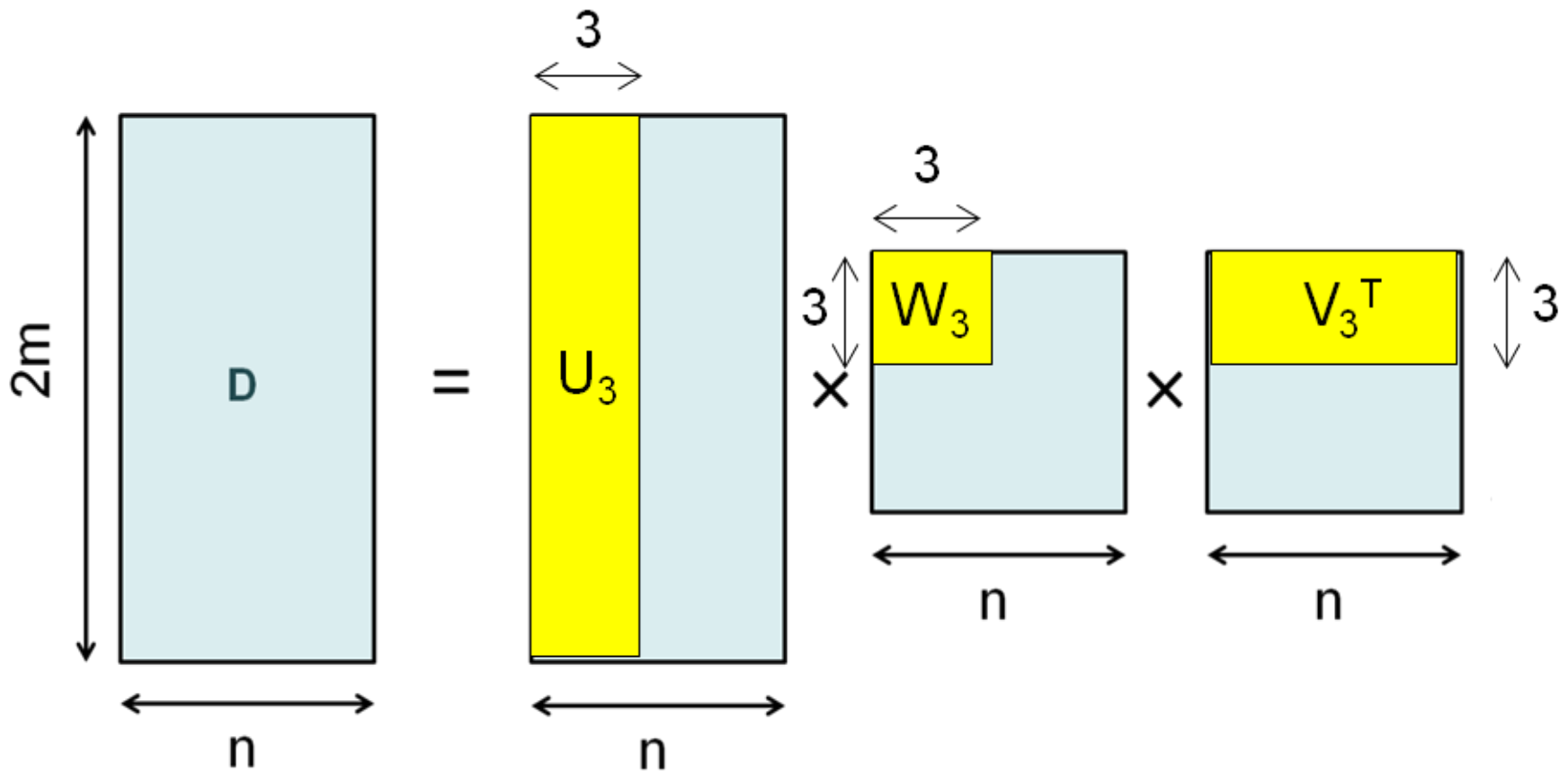
# Factorizing the Measurement Matrix

- Singular value decomposition of  $D$ :

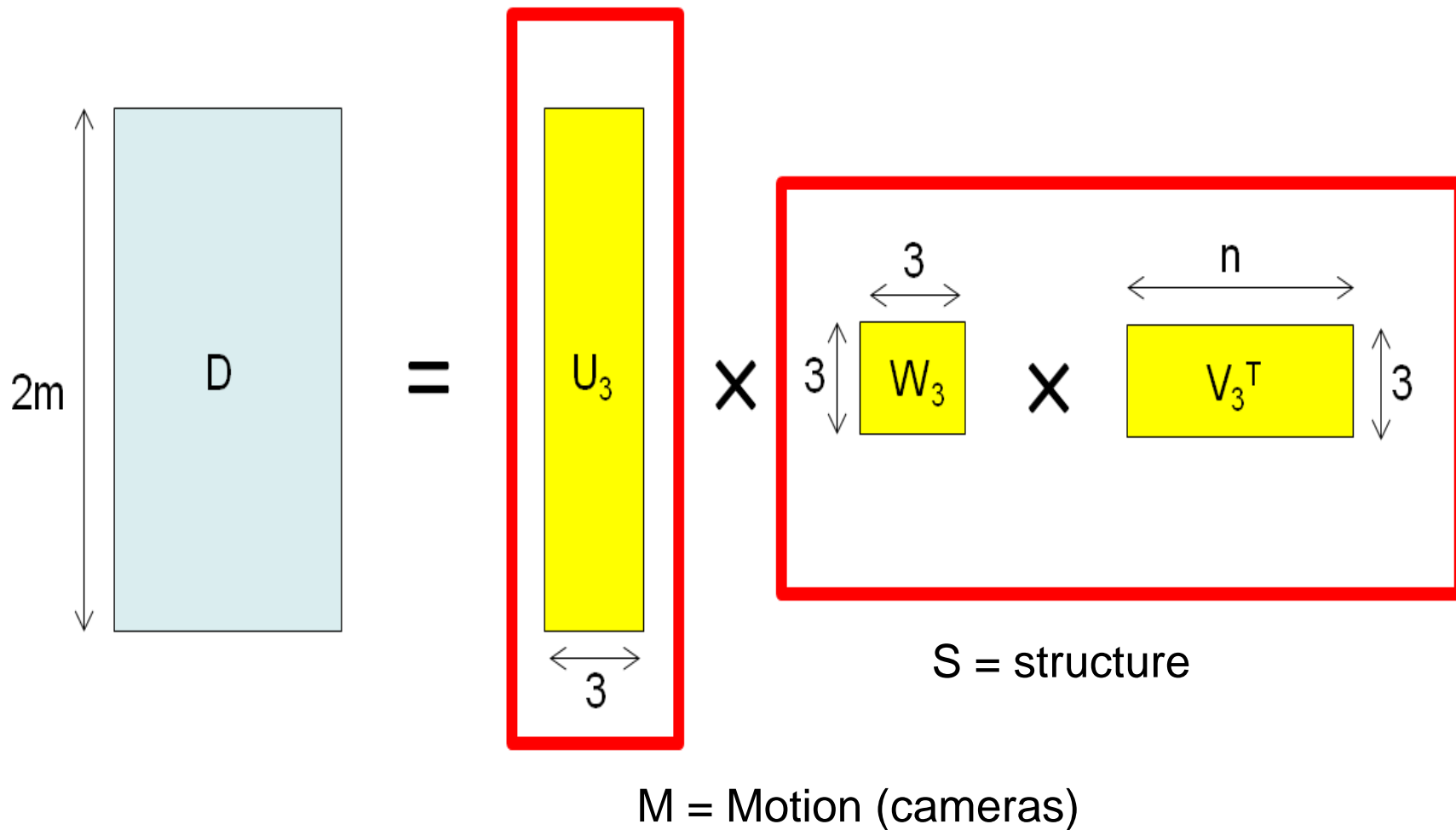


# Factorizing the Measurement Matrix

Since  $\text{rank}(D)=3$ , there are only 3 non-zero singular values



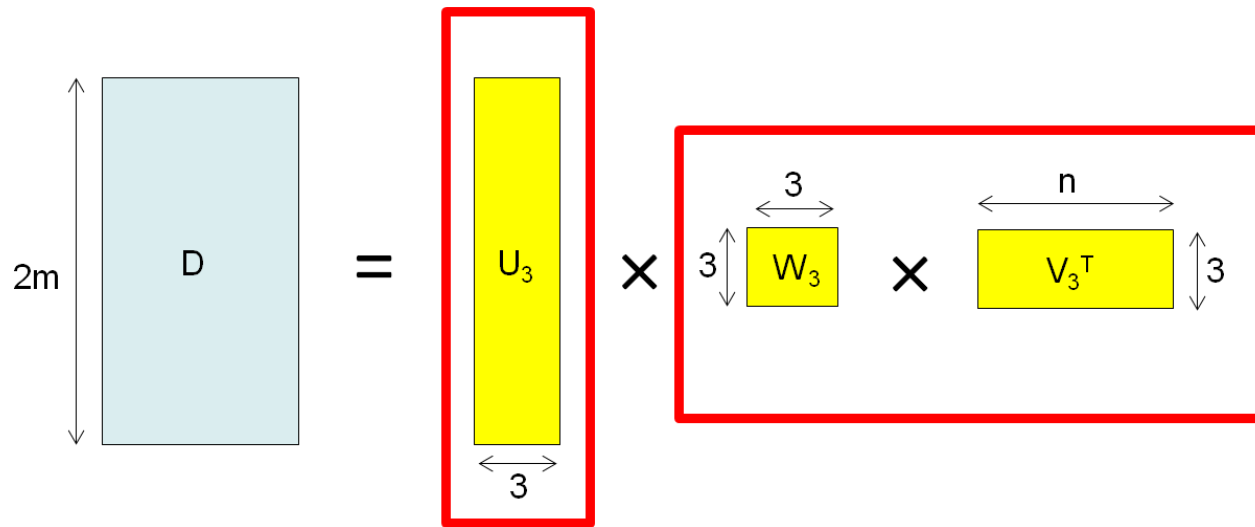
# Factorizing the Measurement Matrix



# Factorizing the Measurement Matrix

What is the issue here?  $\mathbf{D}$  has rank  $> 3$  because of:

- measurement noise
- affine approximation



**Theorem:** When  $\mathbf{D}$  has a rank greater than  $p$ ,  $\mathbf{U}_p \mathbf{W}_p \mathbf{V}_p^T$  is the best possible rank- $p$  approximation of  $\mathbf{A}$  in the sense of the Frobenius norm.

$$\mathbf{D} = \mathbf{U}_3 \mathbf{W}_3 \mathbf{V}_3^T \quad \begin{cases} \mathbf{A}_0 = \mathbf{U}_3 \\ \mathbf{P}_0 = \mathbf{W}_3 \mathbf{V}_3^T \end{cases}$$

$$\|\mathbf{A}\|_F = \sqrt{\sum_{i=1}^m \sum_{j=1}^n |a_{ij}|^2} = \sqrt{\sum_{i=1}^{\min\{m, n\}} \sigma_i^2}$$



# Affine Ambiguity

$$\mathbf{D} = \mathbf{M} \mathbf{C} \times \mathbf{C}^{-1} \mathbf{S}$$

$\underbrace{\mathbf{M} \mathbf{C}}_{\mathbf{M}'}$        $\underbrace{\mathbf{C}^{-1} \mathbf{S}}_{\mathbf{S}'}$

- The decomposition is not unique. We get the same  $\mathbf{D}$  by using any  $3 \times 3$  matrix  $\mathbf{C}$  and applying the transformations:

$$\mathbf{M} \rightarrow \mathbf{M} \mathbf{C}$$

$$\mathbf{S} \rightarrow \mathbf{C}^{-1} \mathbf{S}$$

- Additional constraints must be enforced to resolve this ambiguity

# Reconstruction results



1



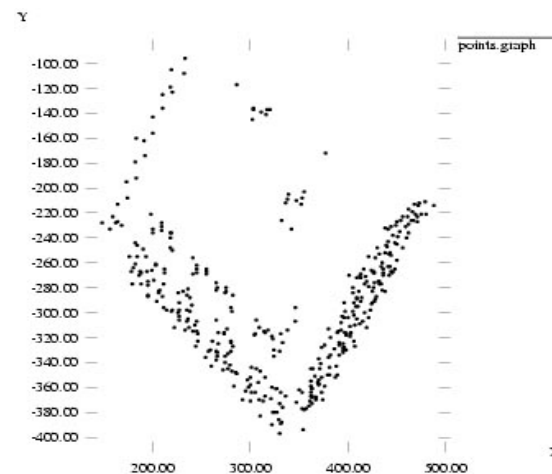
60



120



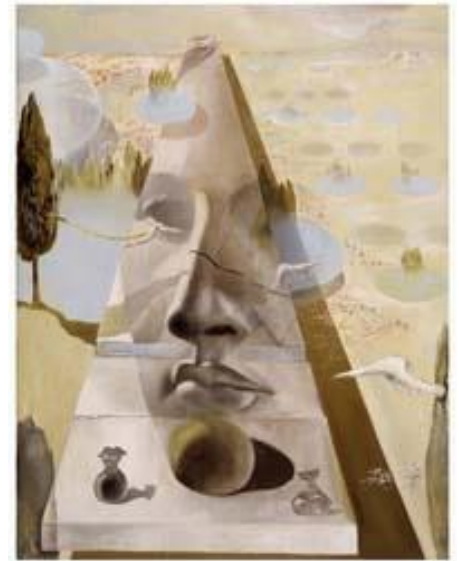
150



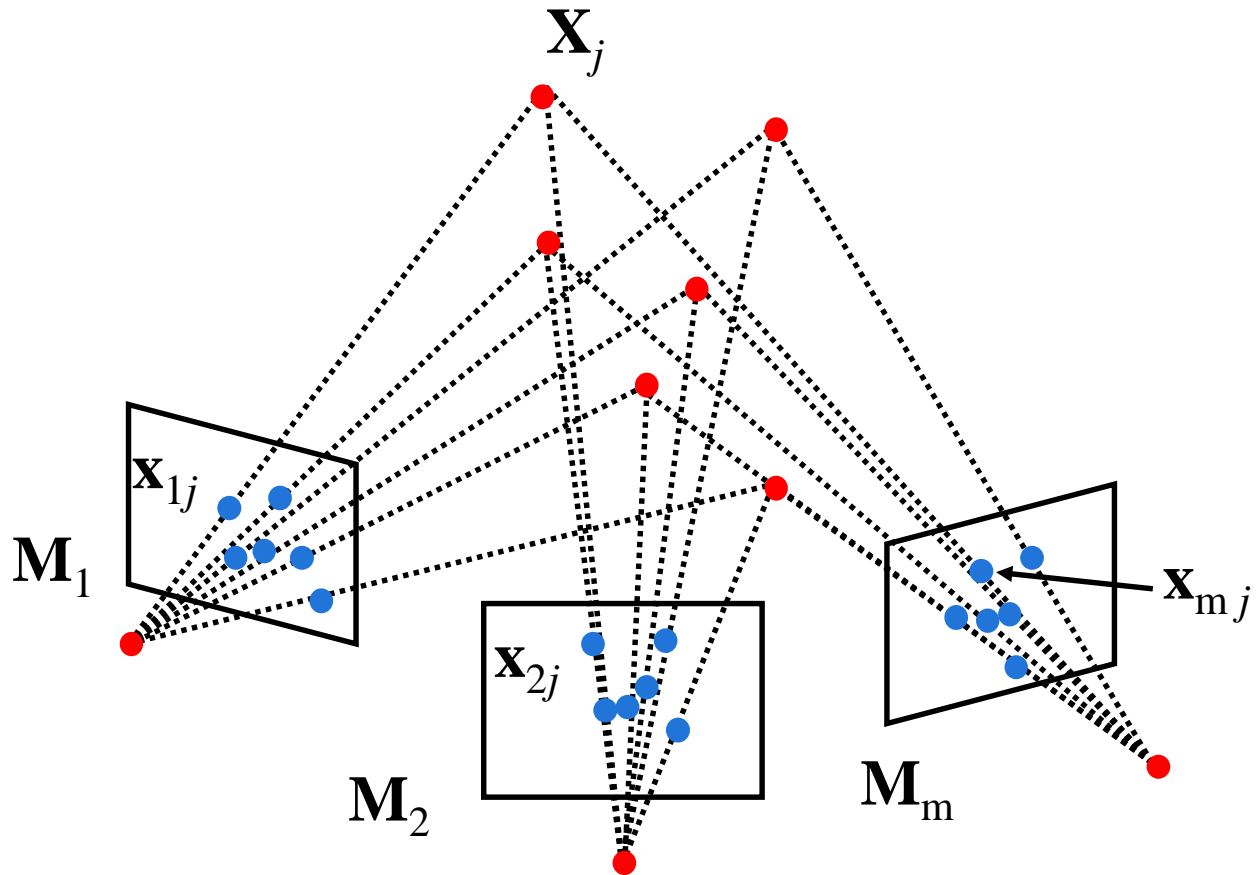
# Lecture 6

## Multi-view geometry

- The SFM problem
- Affine SFM
- Perspective SFM
- Self-calibration



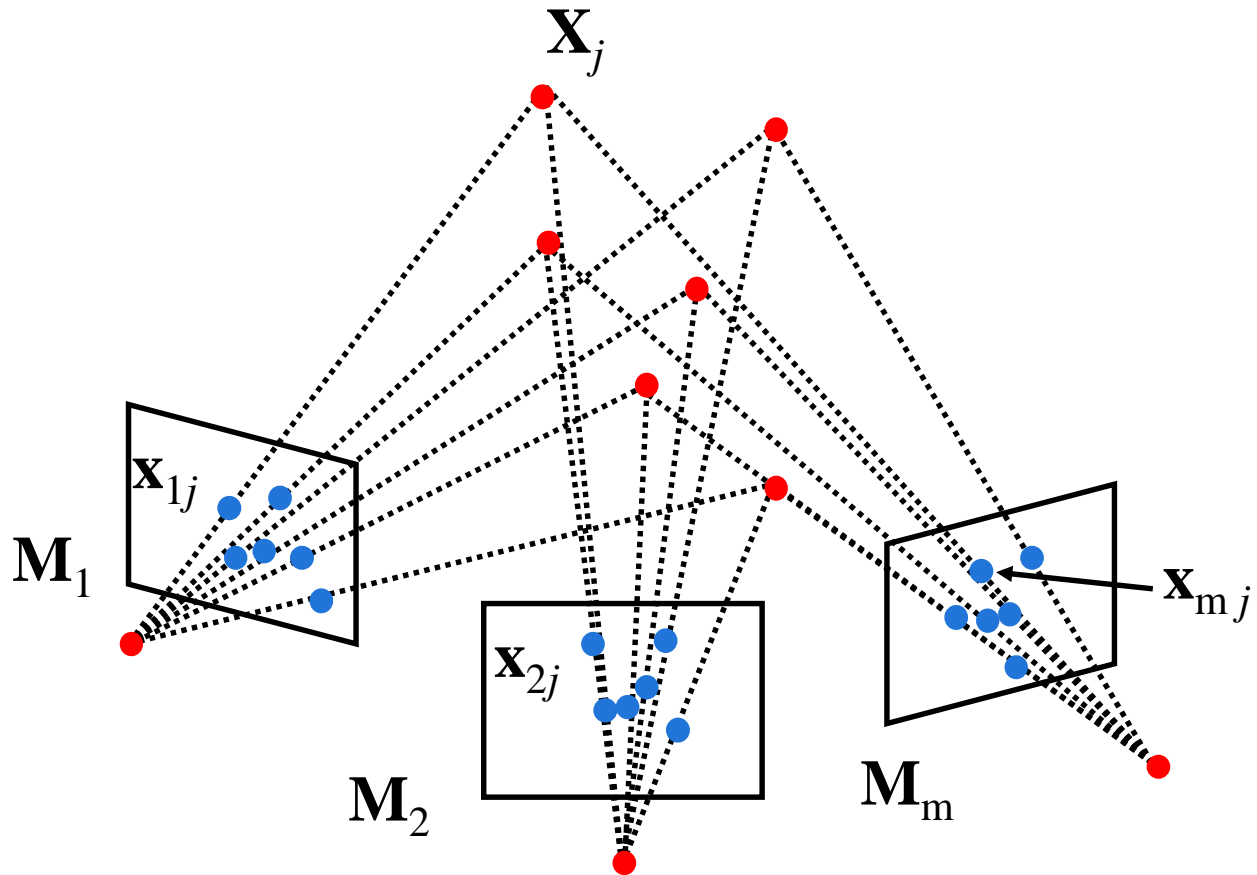
# Structure from motion problem



From the  $m \times n$  correspondences  $x_{ij}$ , estimate:

- $m$  projection matrices  $M_i$
- $n$  3D points  $X_j$
- Upgrade to metric reconstruction

# Structure from motion problem



$m$  cameras  $M_1 \dots M_m$

$$M_i = \begin{bmatrix} a_{11} & a_{12} & a_{13} & b_1 \\ a_{21} & a_{22} & a_{23} & b_2 \\ a_{31} & a_{32} & a_{33} & 1 \end{bmatrix}$$

# The Structure-from-Motion Problem

Given  $m$  images of  $n$  fixed points  $X_j$  we can write

$$x_{ij} = M_i X_j \quad \text{for } i = 1, \dots, m \quad \text{and } j = 1, \dots, n.$$

**Problem:** estimate the  $m$   $3 \times 4$  matrices  $M_i$  and the  $n$  positions  $X_j$  from the  $m \times n$  correspondences  $x_{ij}$ .

- With no calibration info, cameras and points can only be recovered up to a  $4 \times 4$  projective (16 parameters)
- Given two cameras, how many points are needed?
- How many equations and how many unknowns?

$2m \times n$  equations in  $11m + 3n - 16$  unknowns

# Structure-from-Motion Algorithms

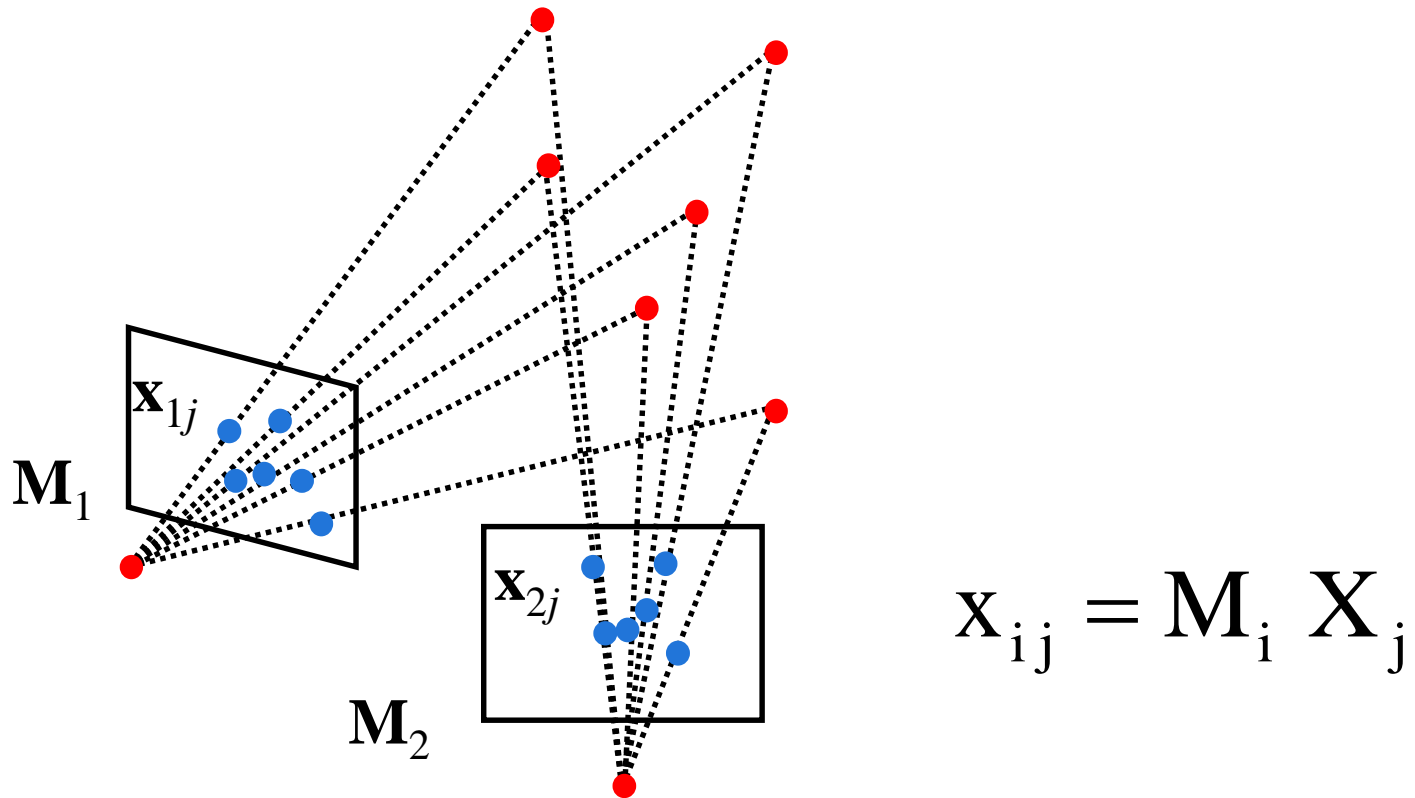
- Algebraic approach (by fundamental matrix)
- Factorization method (by SVD)
- Bundle adjustment

# Algebraic approach (2-view case)

1. Compute the fundamental matrix  $F$  from two views (eg. 8 point algorithm)
2. Use  $F$  to estimate projective cameras
3. Use these cameras to triangulate and estimate points in 3D



# Algebraic approach (2-view case)



Apply a projective transformation  $H$  such that:

$$\mathbf{M}_1 \mathbf{H}^{-1} = \begin{bmatrix} \mathbf{I} & \mathbf{0} \end{bmatrix} \quad \mathbf{M}_2 \mathbf{H}^{-1} = \begin{bmatrix} \mathbf{A} & \mathbf{b} \end{bmatrix}$$

Canonical perspective cameras

# Algebraic approach (2-view case)

$$\left\{ \begin{array}{l} M_1 H^{-1} = [I \quad 0] \\ M_2 H^{-1} = [A \quad b] \\ \tilde{\mathbf{X}} = H \mathbf{X} \end{array} \right. \quad \begin{array}{l} \mathbf{x} = M_1 H^{-1} H \mathbf{X} = [I \mid 0] \tilde{\mathbf{X}} \\ \mathbf{x}' = M_2 H^{-1} H \mathbf{X} = [A \mid b] \tilde{\mathbf{X}} \end{array}$$

$$\mathbf{x}' = [A \mid b] \tilde{\mathbf{X}} = [A \mid b] \begin{bmatrix} \tilde{X}_1 \\ \tilde{X}_2 \\ \tilde{X}_3 \\ 1 \end{bmatrix} = A[I \mid 0] \begin{bmatrix} \tilde{X}_1 \\ \tilde{X}_2 \\ \tilde{X}_3 \\ 1 \end{bmatrix} + b = A \boxed{[I \mid 0] \tilde{\mathbf{X}}} + b = A\mathbf{x} + b$$

$$\mathbf{x}' \times \mathbf{b} = (A\mathbf{x} + \mathbf{b}) \times \mathbf{b} = A\mathbf{x} \times \mathbf{b}$$

$$\mathbf{x}'^T \cdot (\mathbf{x}' \times \mathbf{b}) = \mathbf{x}'^T \cdot (A\mathbf{x} \times \mathbf{b}) = 0$$

$$\mathbf{x}'^T (\mathbf{b} \times A\mathbf{x}) = 0$$

# Cross product as matrix multiplication

$$\mathbf{a} \times \mathbf{b} = \begin{bmatrix} 0 & -a_z & a_y \\ a_z & 0 & -a_x \\ -a_y & a_x & 0 \end{bmatrix} \begin{bmatrix} b_x \\ b_y \\ b_z \end{bmatrix} = [\mathbf{a}_\times] \mathbf{b}$$

# Algebraic approach (2-view case)

$$\begin{aligned} \mathbf{x} &= M_1 H^{-1} H \mathbf{X} = [\mathbf{I} \mid \mathbf{0}] \tilde{\mathbf{X}} \\ \mathbf{x}' &= M_2 H^{-1} H \mathbf{X} = [\mathbf{A} \mid \mathbf{b}] \tilde{\mathbf{X}} \end{aligned} \quad \left\{ \begin{array}{l} M_1 H^{-1} = [\mathbf{I} \quad \mathbf{0}] \\ M_2 H^{-1} = [\mathbf{A} \quad \mathbf{b}] \\ \tilde{\mathbf{X}} = H \mathbf{X} \end{array} \right.$$

$$\mathbf{x}' = [\mathbf{A} \mid \mathbf{b}] \tilde{\mathbf{X}} = [\mathbf{A} \mid \mathbf{b}] \begin{bmatrix} \tilde{X}_1 \\ \tilde{X}_2 \\ \tilde{X}_3 \\ 1 \end{bmatrix} = \mathbf{A}[\mathbf{I} \mid \mathbf{0}] \begin{bmatrix} \tilde{X}_1 \\ \tilde{X}_2 \\ \tilde{X}_3 \\ 1 \end{bmatrix} + \mathbf{b} = \mathbf{A}[\mathbf{I} \mid \mathbf{0}] \tilde{\mathbf{X}} + \mathbf{b} = \mathbf{A}\mathbf{x} + \mathbf{b}$$

$$\mathbf{x}' \times \mathbf{b} = (\mathbf{A}\mathbf{x} + \mathbf{b}) \times \mathbf{b} = \mathbf{A}\mathbf{x} \times \mathbf{b}$$

$$\mathbf{x}'^T \cdot (\mathbf{x}' \times \mathbf{b}) = \mathbf{x}'^T \cdot (\mathbf{A}\mathbf{x} \times \mathbf{b}) = 0$$

$$\mathbf{x}'^T (\mathbf{b} \times \mathbf{A}\mathbf{x}) = 0$$

$$\mathbf{x}'^T [\mathbf{b}_\times] \mathbf{A} \mathbf{x} = 0 \quad \text{is this familiar?}$$

$$\mathbf{F} = [\mathbf{b}_\times] \mathbf{A}$$

$$\mathbf{x}'^T \mathbf{F} \mathbf{x} = 0$$

# Compute cameras

$$\mathbf{x}'^T \mathbf{F} \mathbf{x} = 0 \quad \mathbf{F} = [\mathbf{b}_\times] \mathbf{A}$$

Compute  $\mathbf{b}$ :

$$\mathbf{F} \cdot \mathbf{b} = [\mathbf{b}_\times] \mathbf{A} \cdot \mathbf{b} = \mathbf{b} \times \mathbf{A} \cdot \mathbf{b} = 0$$

→  $\left\{ \begin{array}{l} \mathbf{F} \text{ is singular} \\ \text{Compute } \mathbf{b} \text{ as least sq.} \\ \text{solution of } \mathbf{F} \mathbf{b} = 0, \text{ with} \\ |\mathbf{b}| = 1 \text{ using SVD} \end{array} \right.$

Compute  $\mathbf{A}$ :  $\mathbf{A} = \mathbf{A}' = -[\mathbf{b}_\times] \mathbf{F}$

Indeed, let's verify that  $[\mathbf{b}_\times] \mathbf{A}'$  is still equal to  $\mathbf{F}$

$$\text{Indeed: } [\mathbf{b}_\times] \mathbf{A}' = -[\mathbf{b}_\times][\mathbf{b}_\times] \mathbf{F} = (\mathbf{b} \mathbf{b}^T - |\mathbf{b}|^2 \mathbf{I}) \mathbf{F} = \mathbf{b} \mathbf{b}^T \mathbf{F} + |\mathbf{b}|^2 \mathbf{F} = 0 + 1 \cdot \mathbf{F} = \mathbf{F}$$

$$\mathbf{M}_1^p = \begin{bmatrix} \mathbf{I} & \mathbf{0} \end{bmatrix}$$

$$\mathbf{M}_2^p = \begin{bmatrix} -[\mathbf{b}_\times] \mathbf{F} & \mathbf{b} \end{bmatrix}$$

# Algebraic approach (2-view case)

1. Compute the fundamental matrix  $F$  from two views (eg. 8 point algorithm)
2. Compute  $b$  and  $A$  from  $F$
3. Use  $b$  and  $A$  to estimate projective cameras
4. Use these cameras to triangulate and estimate points in 3D

# Interpretation of $\mathbf{b}$

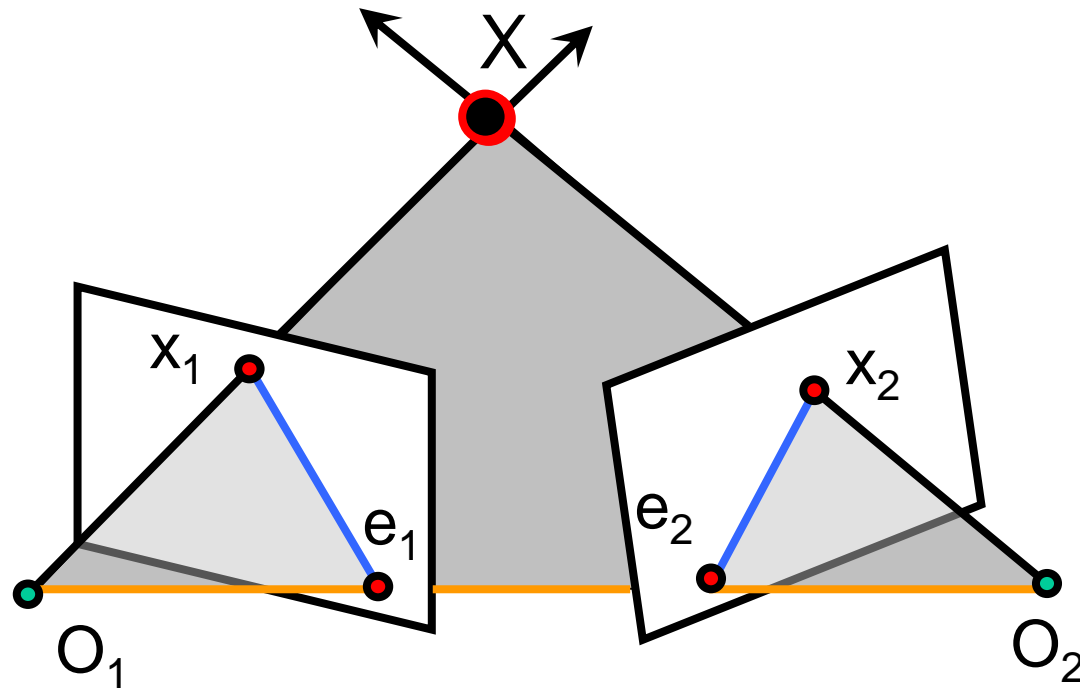
$$\mathbf{x}'^T \mathbf{F} \mathbf{x} = 0 \quad \mathbf{F} = [\mathbf{b}_x] \mathbf{A}$$

$$\mathbf{F} \cdot \mathbf{b} = 0$$

$$\mathbf{A} = -[\mathbf{b}_x] \mathbf{F}$$

What's  $\mathbf{b}$ ??

# Epipolar Constraint [lecture 6]



$F x_2$  is the epipolar line associated with  $x_2$  ( $l_1 = F x_2$ )

$F^T x_1$  is the epipolar line associated with  $x_1$  ( $l_2 = F^T x_1$ )

$F$  is singular (rank two)

$$F e_2 = 0 \quad \text{and} \quad F^T e_1 = 0$$

$F$  is 3x3 matrix; 7 DOF



# Interpretation of $\mathbf{b}$

$$\mathbf{x}'^T \mathbf{F} \mathbf{x} = 0 \quad \mathbf{F} = [\mathbf{b}_x] \mathbf{A}$$

$$\mathbf{F} \cdot \mathbf{b} = 0$$

$$\mathbf{A} = -[\mathbf{b}_x] \mathbf{F}$$

**b** is an epipole!

$$M^p_1 = \begin{bmatrix} \mathbf{I} & \mathbf{0} \end{bmatrix}$$

$$M^p_2 = \begin{bmatrix} -[\mathbf{e}_x] \mathbf{F} & \mathbf{e} \end{bmatrix}$$

# Structure-from-Motion Algorithms

- Algebraic approach (by fundamental matrix)
- Factorization method (by SVD)
- Bundle adjustment

# Limitations of the approaches seen so far

- Factorization methods assume all points are visible.

This not true if:

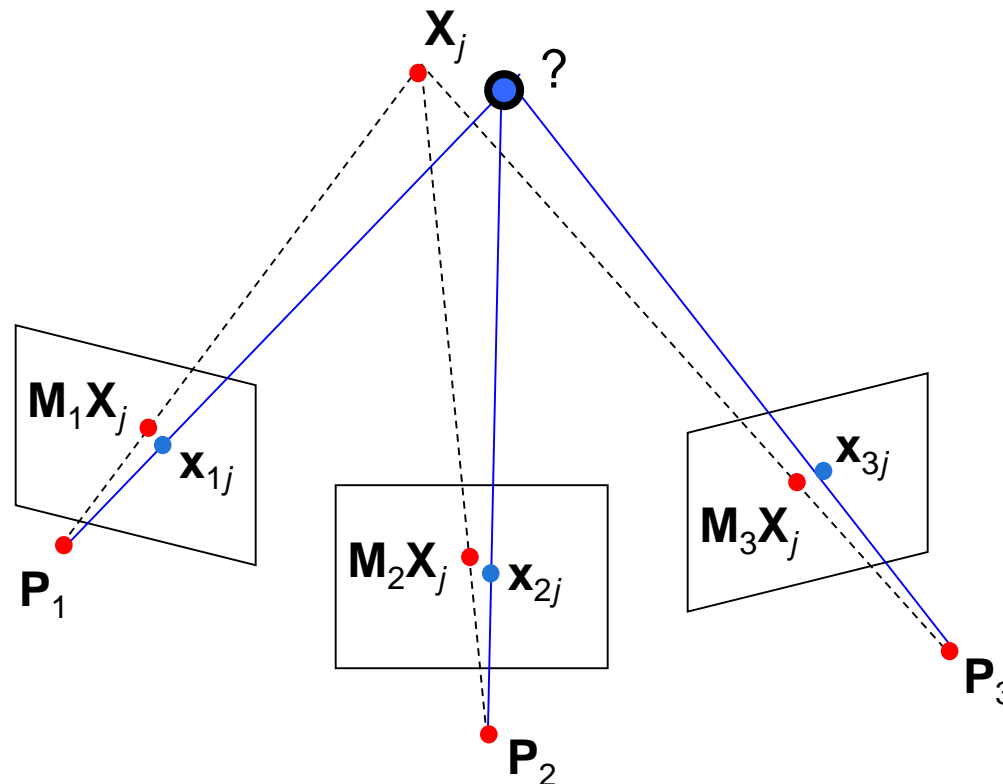
- occlusions occur
  - failure in establishing correspondences
- 
- Algebraic methods work with 2 views

# Bundle adjustment

Non-linear method for refining structure and motion

Minimizing re-projection error

$$E(\mathbf{M}, \mathbf{X}) = \sum_{i=1}^m \sum_{j=1}^n D(\mathbf{x}_{ij}, \mathbf{M}_i \mathbf{X}_j)^2$$



# Bundle adjustment

Non-linear method for refining structure and motion

Minimizing re-projection error

$$E(\mathbf{M}, \mathbf{X}) = \sum_{i=1}^m \sum_{j=1}^n D(\mathbf{x}_{ij}, \mathbf{M}_i \mathbf{X}_j)^2$$

- **Advantages**

- Handle large number of views
- Handle missing data

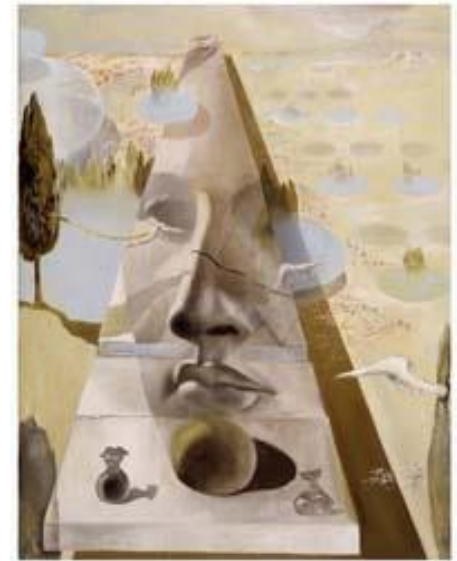
- **Limitations**

- Large minimization problem (parameters grow with number of views)
- requires good initial condition

→ Used as the final step of SFM

# Lecture 6

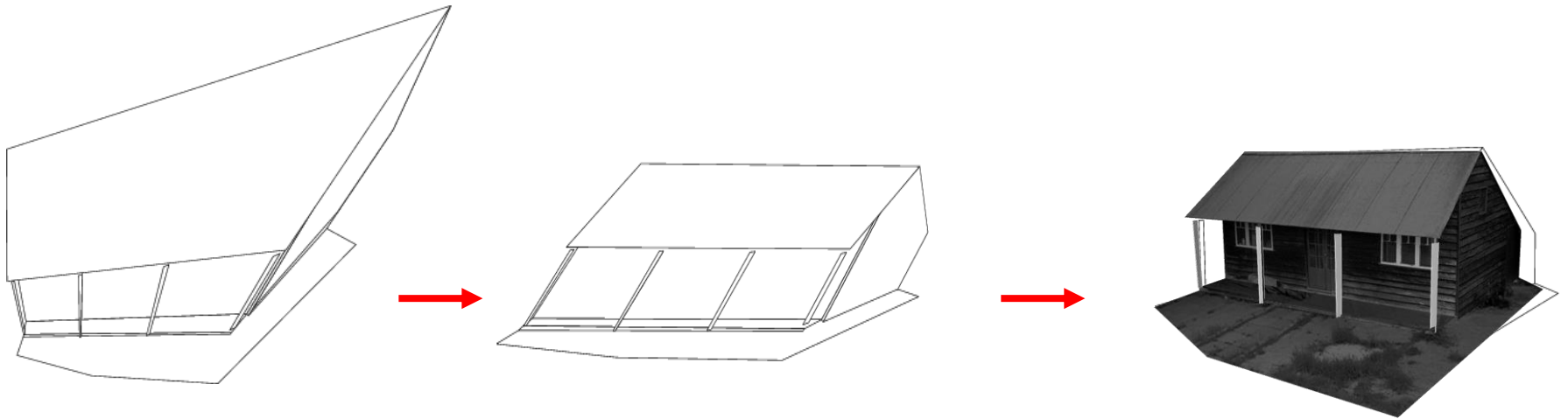
## Multi-view geometry



- The SFM problem
- Affine SFM
- Perspective SFM
- Self-calibration

Reading: [HZ] Chapters: 10,18,19  
[FP] Chapter: 13

Recovering the metric reconstruction from the perspective (or affine) one is called **self-calibration**



# SFM problem - summary

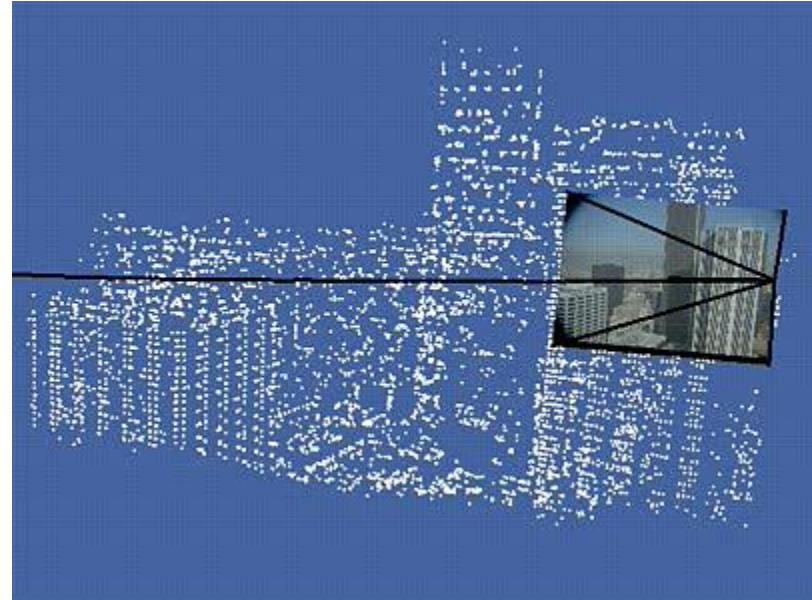
1. Estimate structure and motion up perspective transformation
  1. Algebraic
  2. factorization method
  3. bundle adjustment
2. Convert from perspective to metric (self-calibration)
3. Bundle adjustment

**\*\* or \*\***

1. Bundle adjustment with self-calibration constraints



# Results and applications



Courtesy of Oxford **Visual Geometry Group**

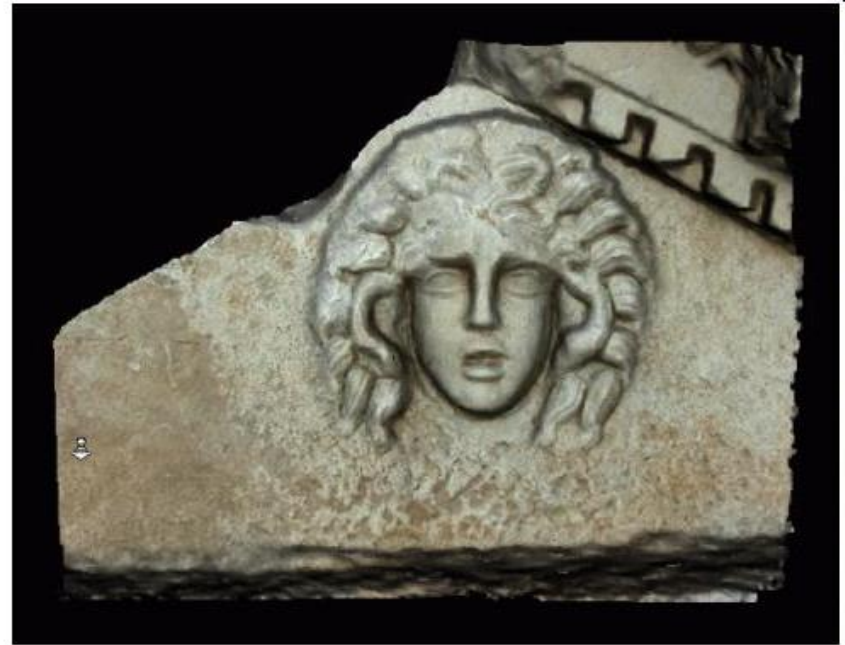
Lucas & Kanade, 81  
Chen & Medioni, 92  
Debevec et al., 96  
Levoy & Hanrahan, 96  
Fitzgibbon & Zisserman, 98  
Triggs et al., 99  
Pollefeys et al., 99  
Kutulakos & Seitz, 99

Levoy et al., 00  
Hartley & Zisserman, 00  
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Nistér, 04  
Brown & Lowe, 04  
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Golparvar-Fard, et al. JAEI 10  
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Microsoft's PhotoSynth  
Snavely et al., 06-08  
Schindler et al., 08  
Agarwal et al., 09  
Frahm et al., 10

# Results and applications

M. Pollefeys et al 98---



# Results and applications

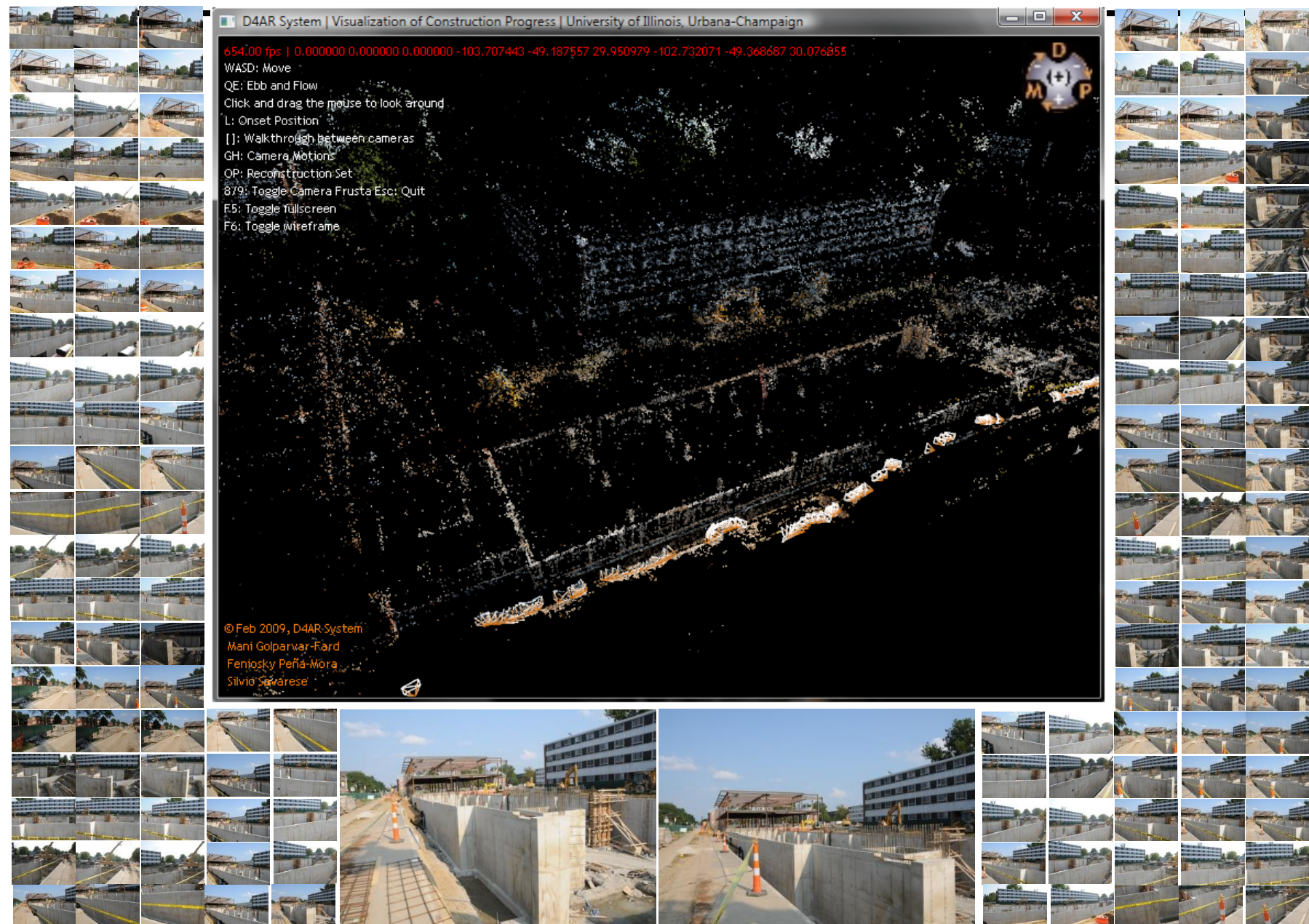


Noah Snavely, Steven M. Seitz, Richard Szeliski, "[Photo tourism: Exploring photo collections in 3D](#)," ACM Transactions on Graphics (SIGGRAPH Proceedings), 2006,

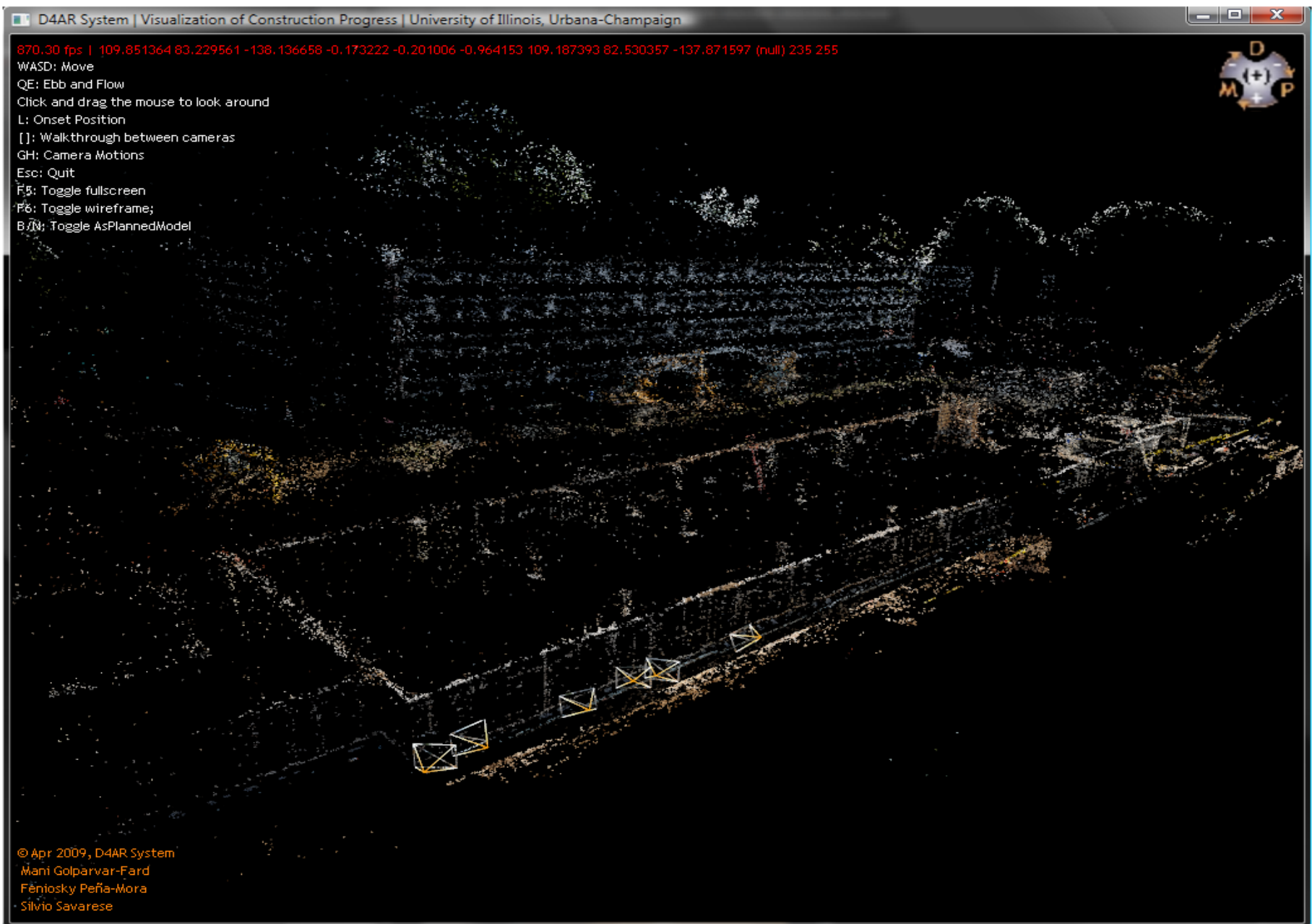


# Incremental reconstruction of construction sites

Initial pair – 2168 & Complete Set 62,323 points, 160 images



# Reconstructed scene + Site photos







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# Next lecture

Self-calibration

Volumetric stereo

